

# Deformable Face Models in ‘the Wild’

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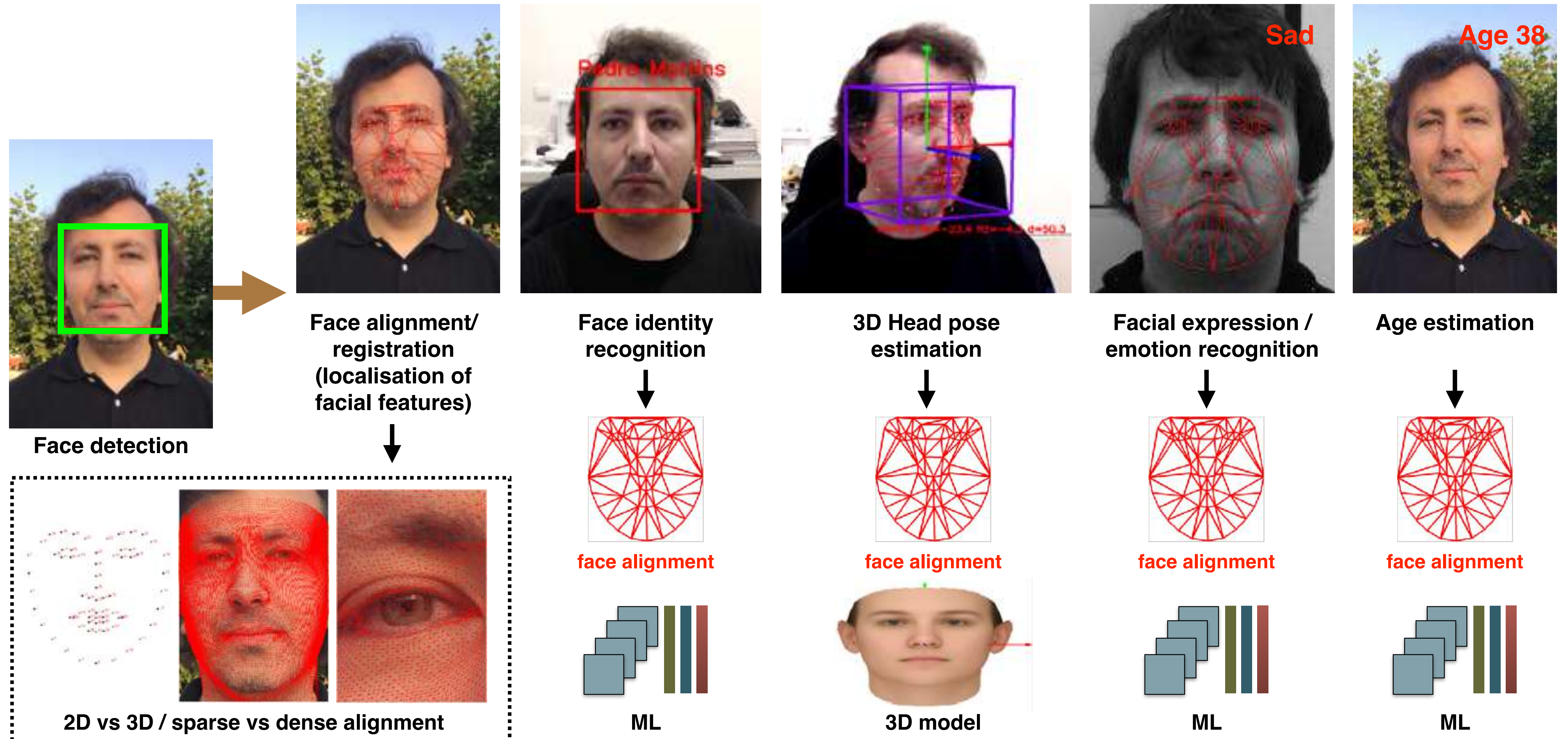


Press Space to Start Capture

Fps 0,00



# Introduction - Face Tasks

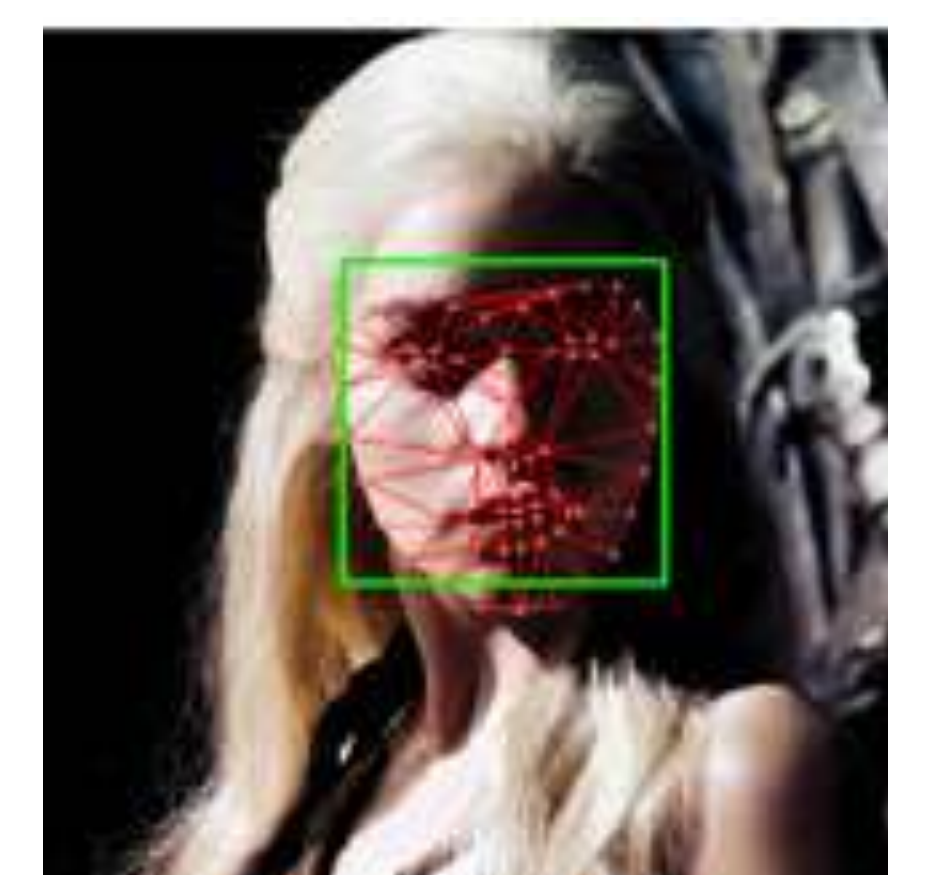
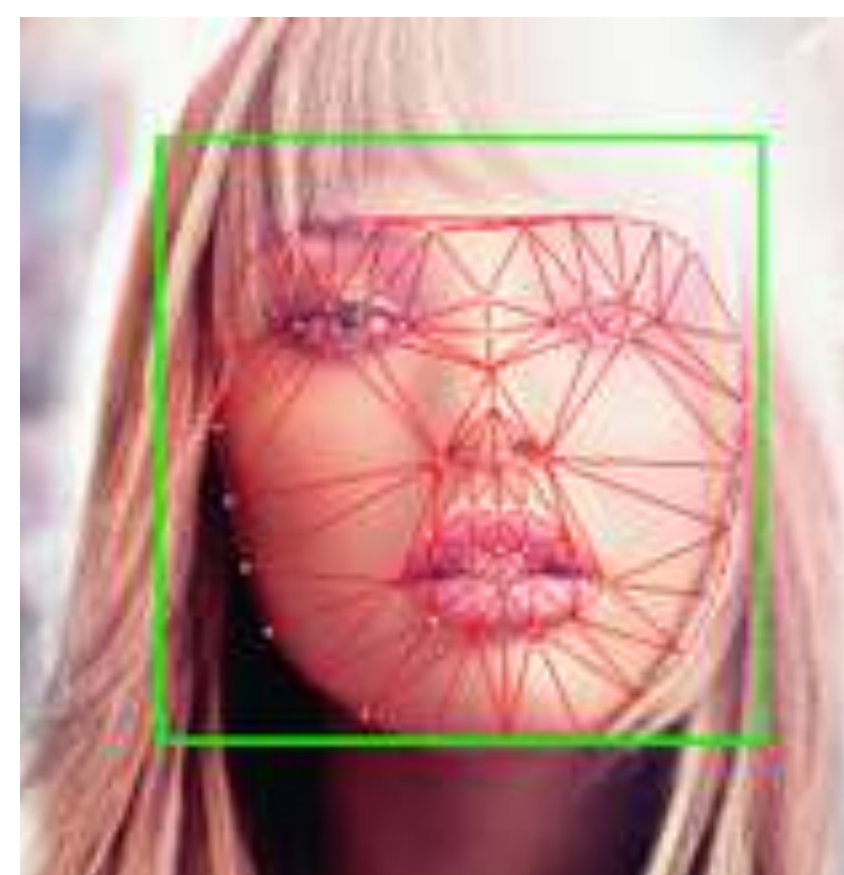
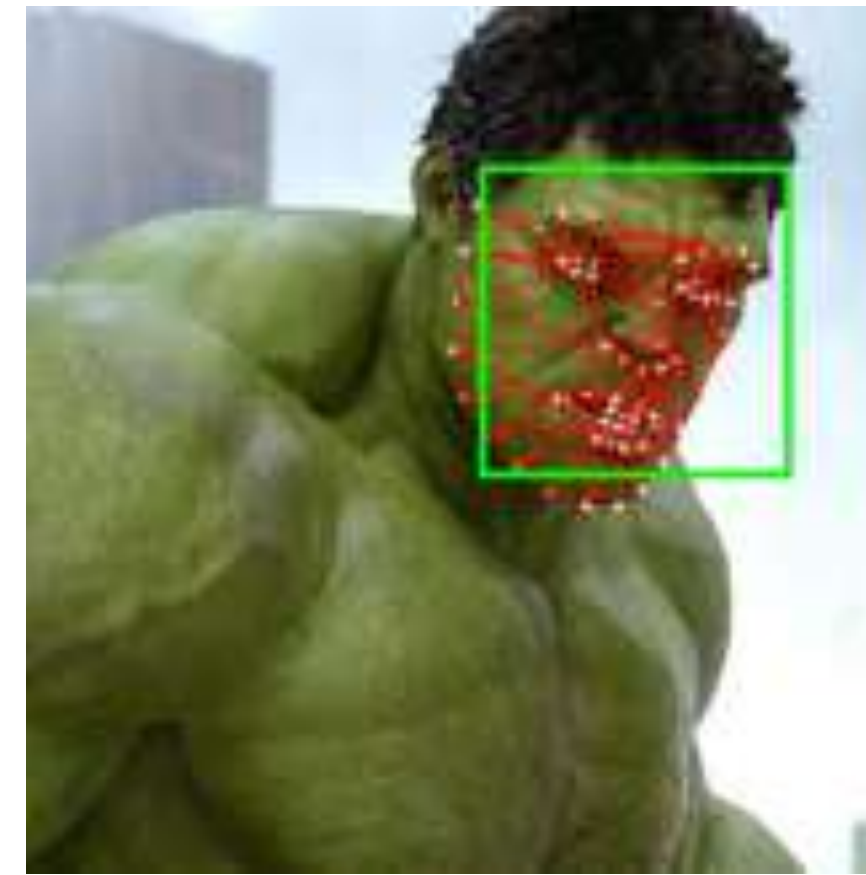
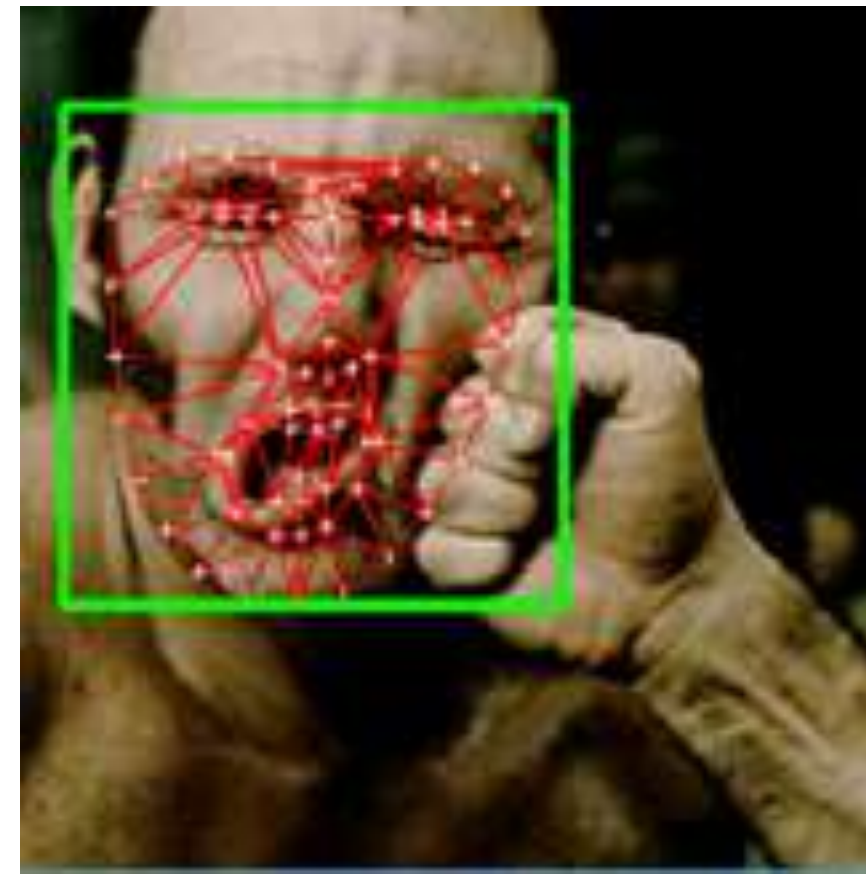


# Face Alignment - How Hard Can It Be?



- Must be able to deal with variations in identity, facial expression, pose, occlusion, illumination, camera parameters, ...

# Face Alignment - How Hard Can It Be?



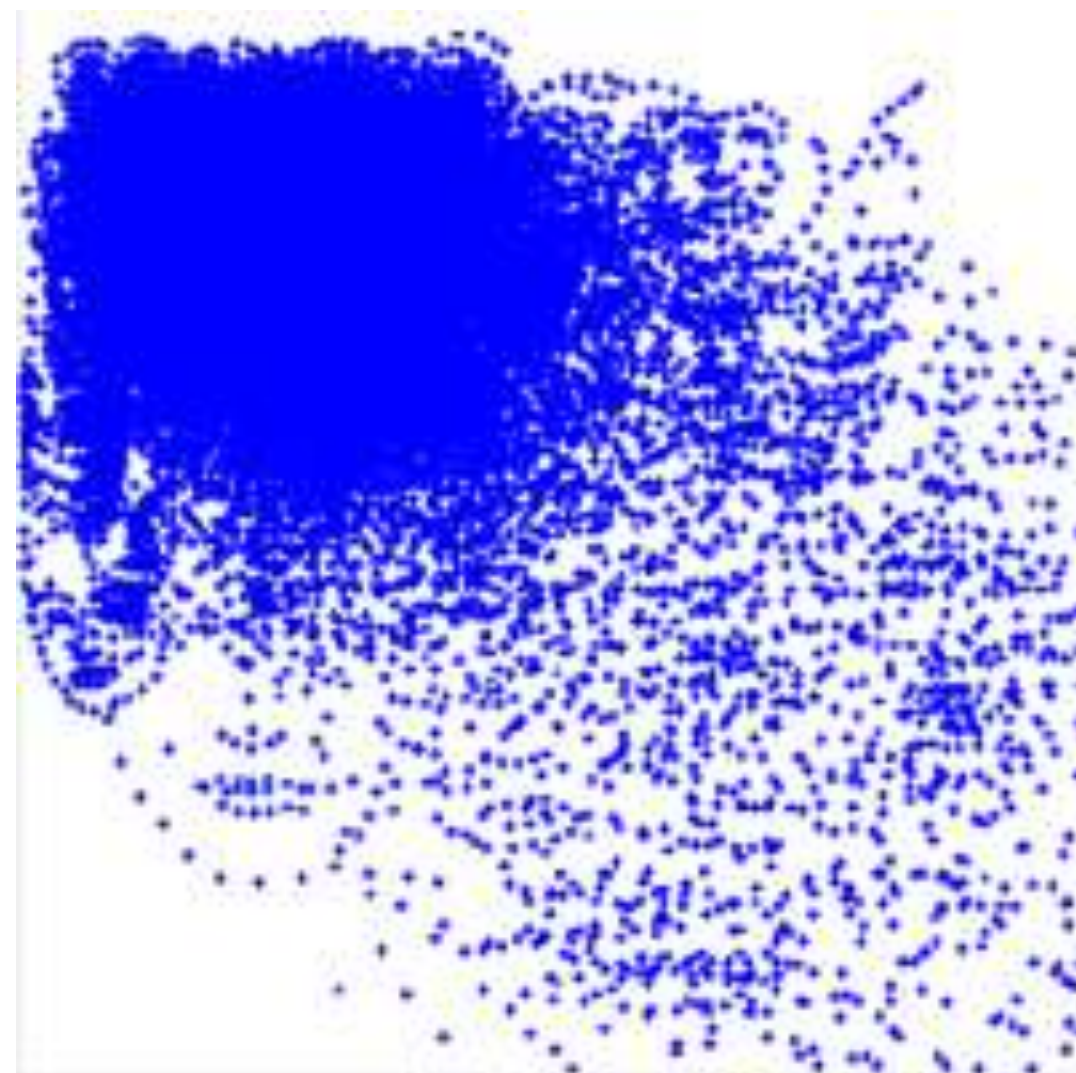
- Must be able to deal with variations in identity, facial expression, pose, occlusion, illumination, camera parameters, ...

# Linear Shape Model

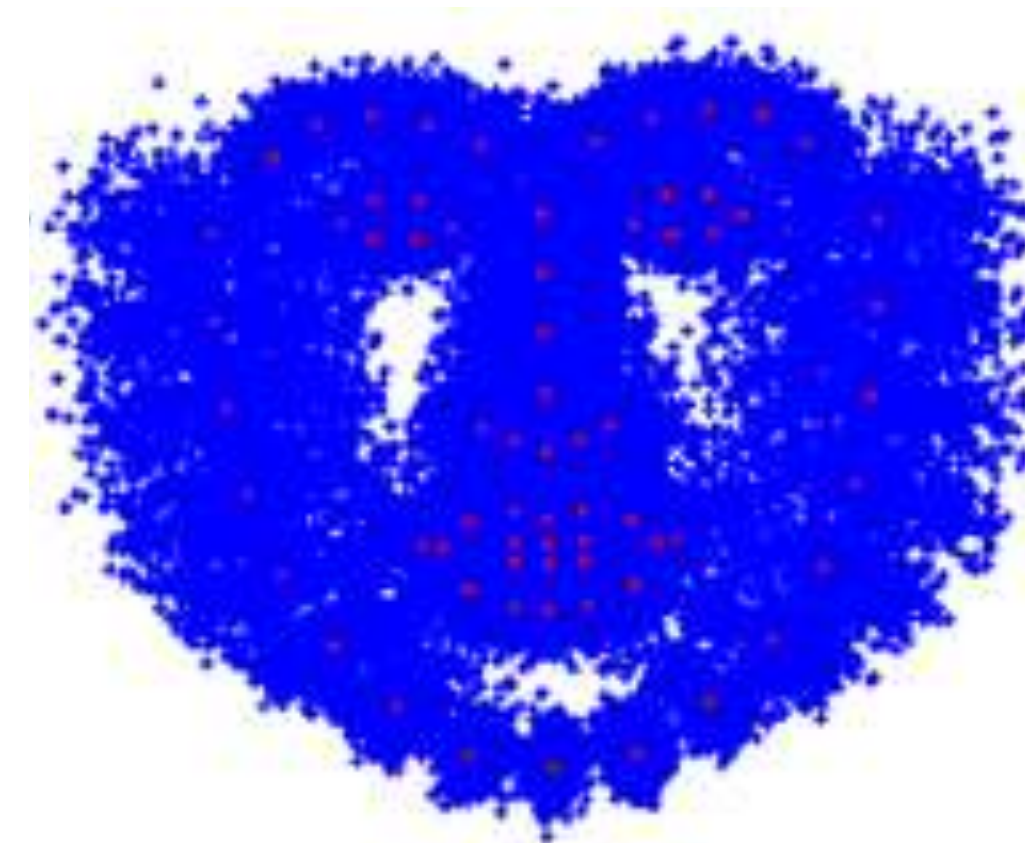
'In the Wild' Image Database



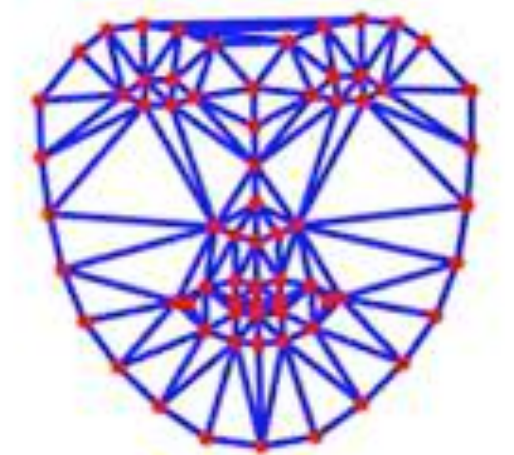
RAW Shape Data



Procrustes Alignment



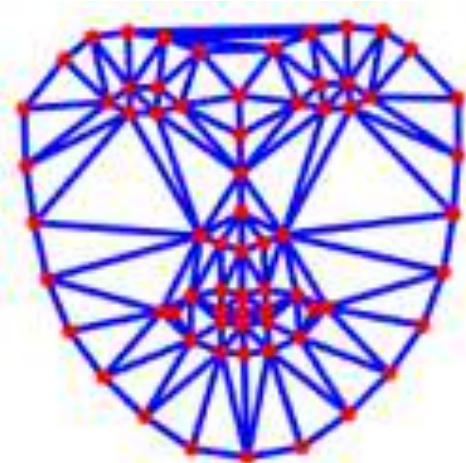
Shape Model



$$\mathcal{B}(s; \mathbf{b}) = \mathbf{s}_0 + \sum_{i=1}^n \phi_i b_i$$

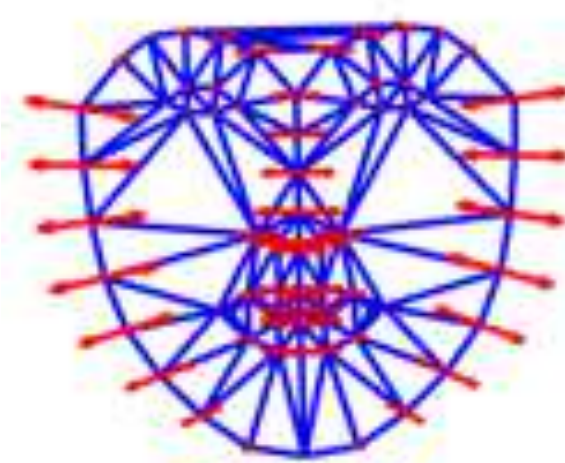
↑  
shape parameters

Mean Shape

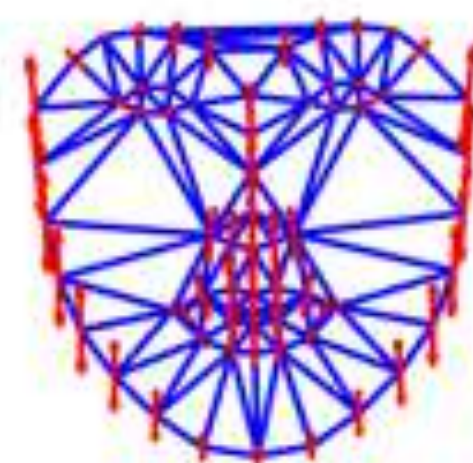


$\mathbf{s}_0$

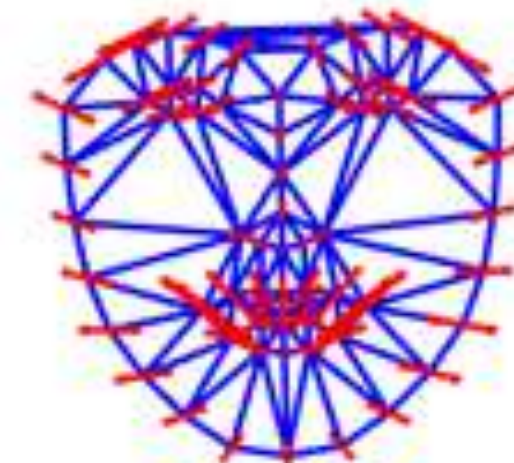
Shape Basis



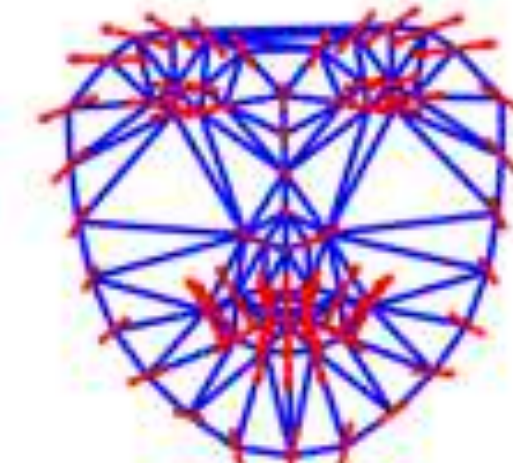
$\phi_1$



$\phi_2$



$\phi_3$



$\phi_4$

Similarity Transform

$$\mathcal{S}(s; \mathbf{q}) = \mathbf{s} + \sum_{j=1}^4 \psi_j q_j$$

↑  
pose parameters

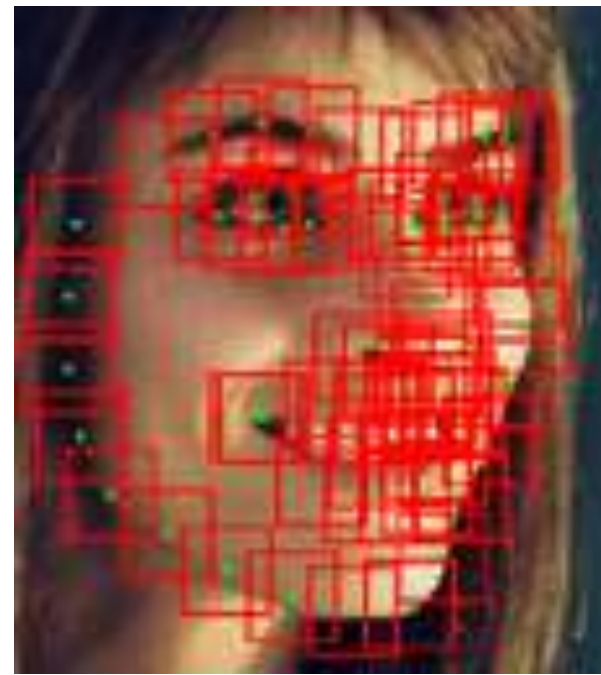
Full Shape Model

$$\mathbf{s} = \mathcal{S}(\mathcal{B}(\mathbf{b}); \mathbf{q}) \quad 6$$

# Local (Patch) Appearance Regions



Similarity Warp  
( $s, \theta, t_x, t_y$ )



Local Appearance Regions



Image + Landmarks

Normalized Image

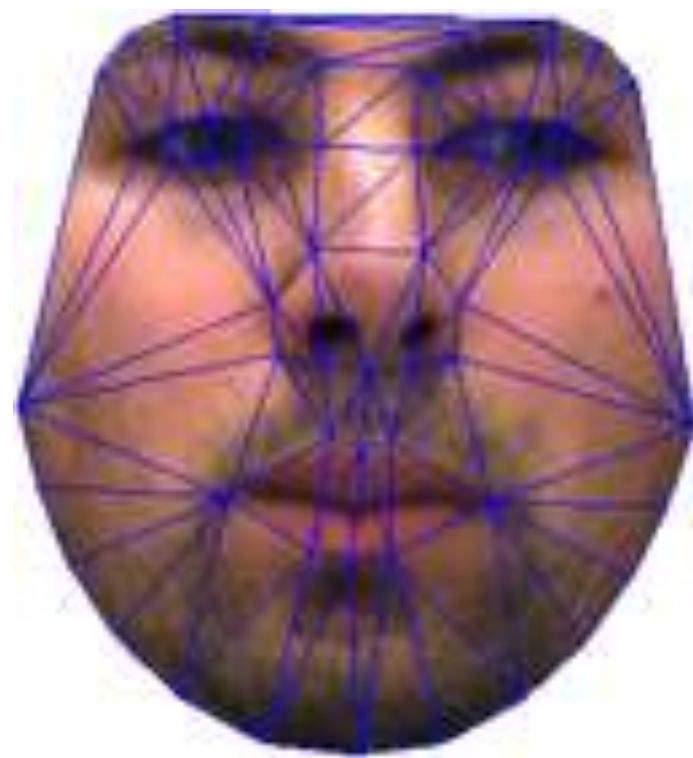
Local Patches

Sampled Local Patches

# Piecewise Affine Warp

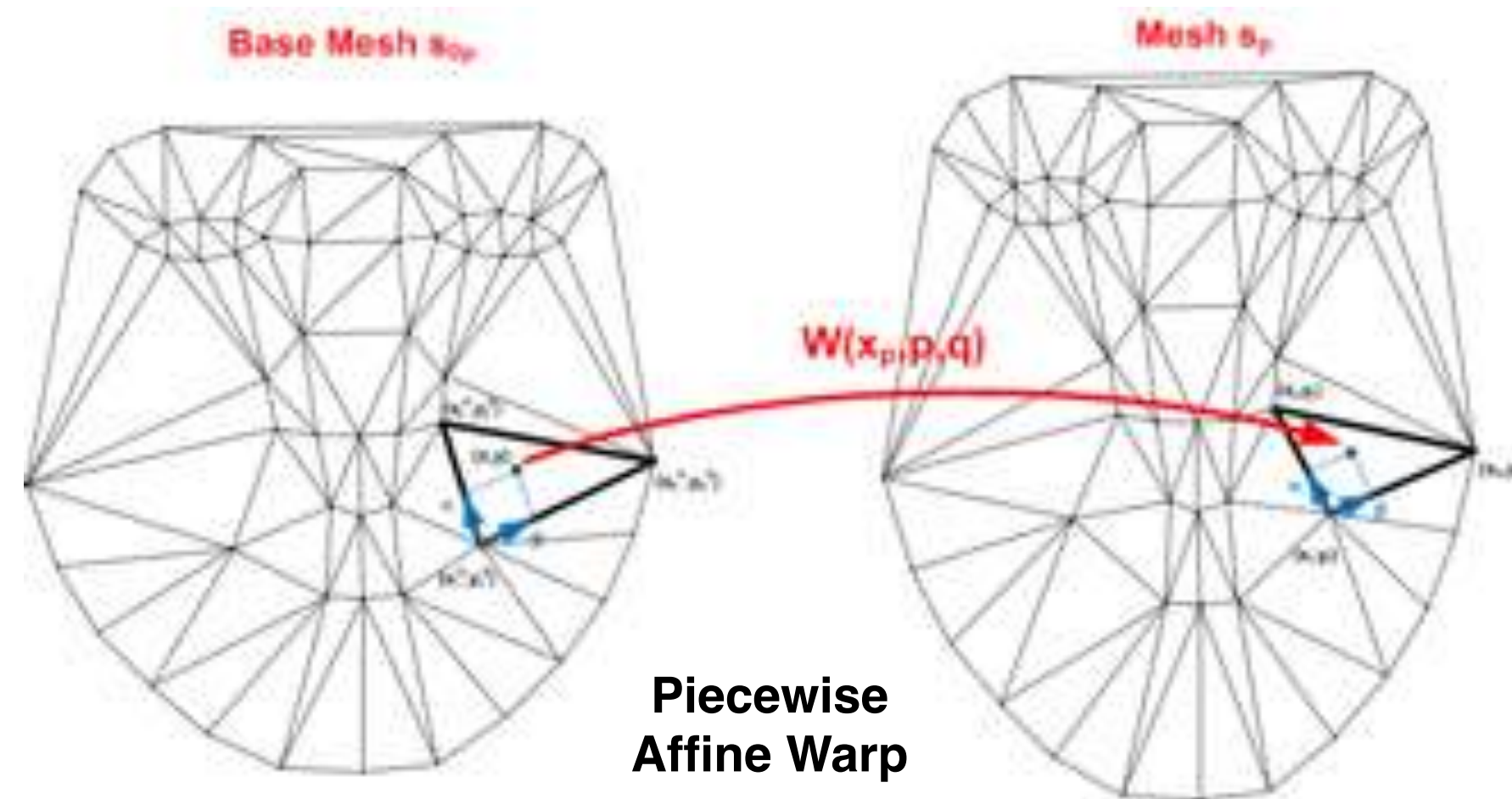
$$\mathbf{W}(\mathbf{x}, \mathbf{p}) = \mathbf{x}_i + \alpha (\mathbf{x}_j - \mathbf{x}_i) + \beta (\mathbf{x}_k - \mathbf{x}_i), \quad \{\mathbf{x}_i, \mathbf{x}_j, \mathbf{x}_k\} \sim \mathbf{s}$$

Warped Image



$\mathbf{I}(\mathbf{W}(\mathbf{x}, \mathbf{p}))$

$$\mathbf{s} = (x_1 \dots x_v, y_1 \dots y_v)^T$$



$\mathbf{W}(\mathbf{x}, \mathbf{p})$

Source Image



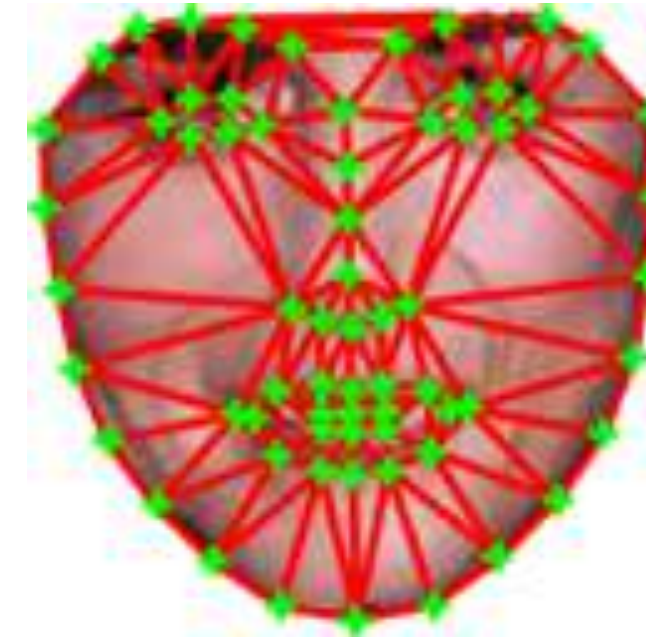
$\mathbf{I}(\mathbf{x})$

$$\mathbf{s} = \mathbf{s}_0 + \sum_{i=1}^n p_i \phi_i$$

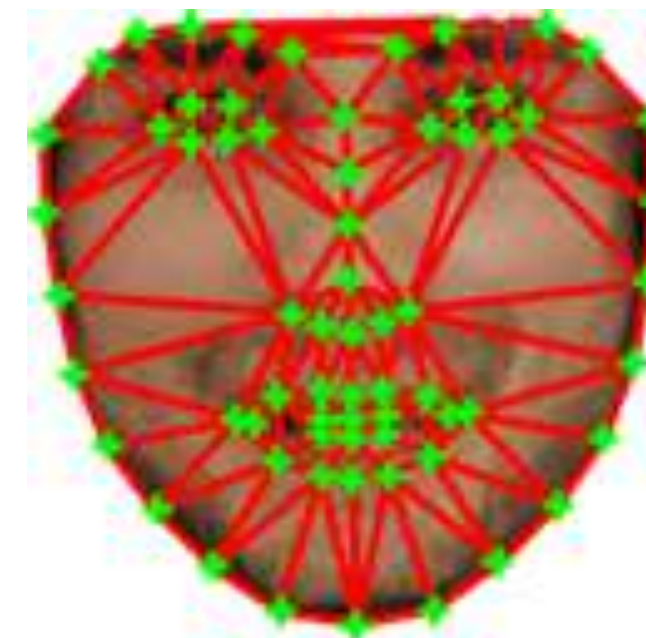
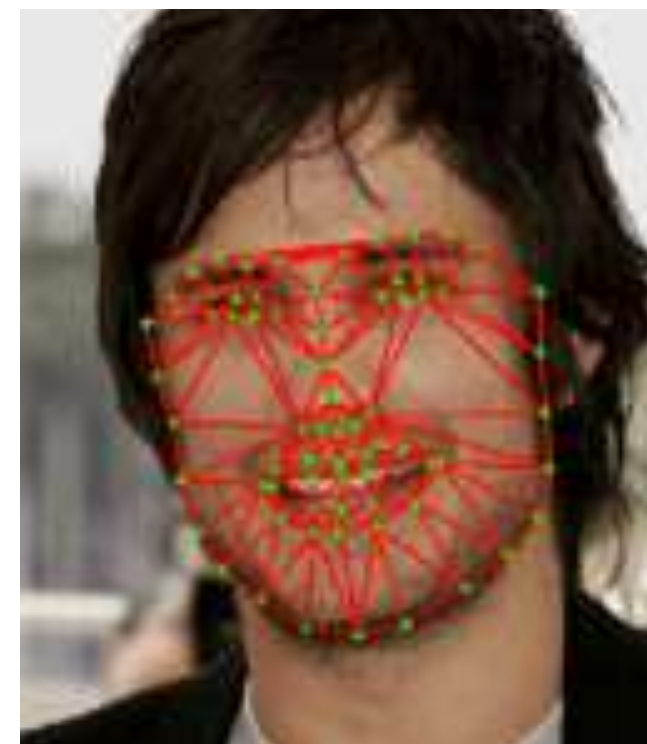
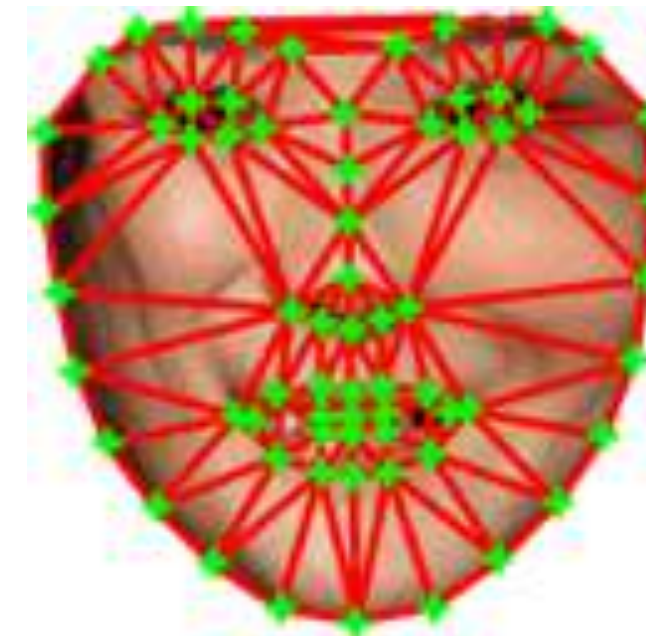


# Holistic Regions (Piecewise Affine Warp)

$I(\mathbf{x})$



$I(\mathbf{W}(\mathbf{x}, \mathbf{p}))$



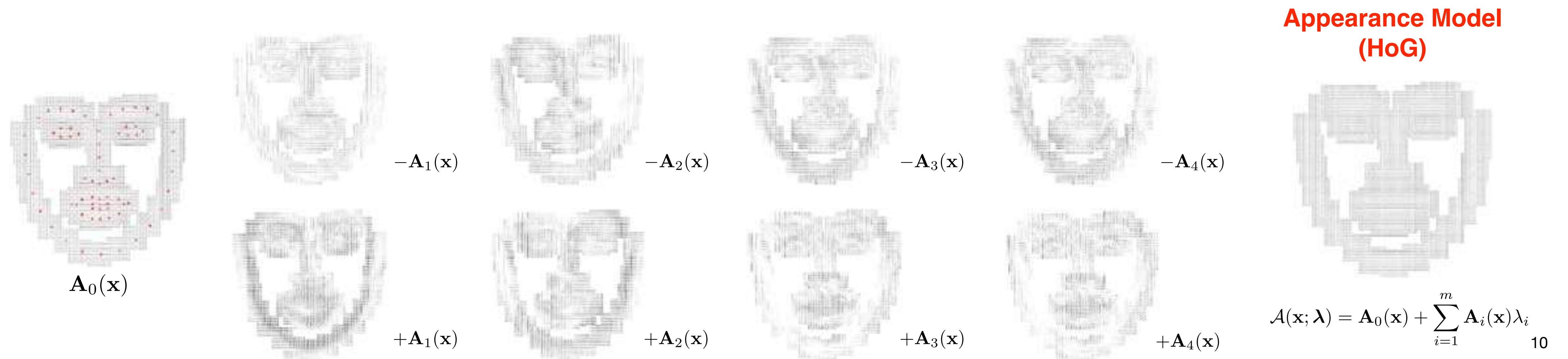
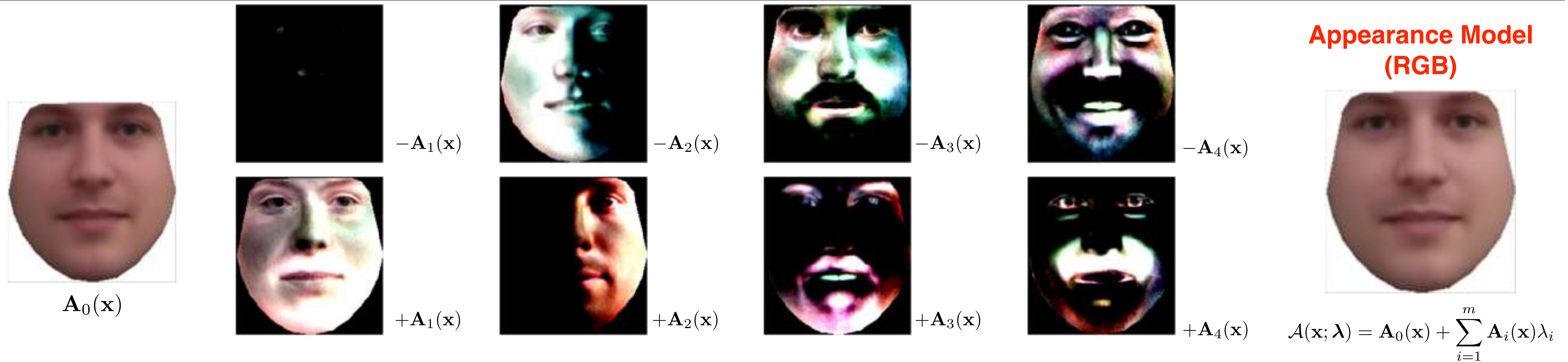
Landmarks

Delaunay Triangulation

Base Mesh

Warped Example

# Linear Appearance Model



# Active Appearance Models (AAMs) - 2D Fitting

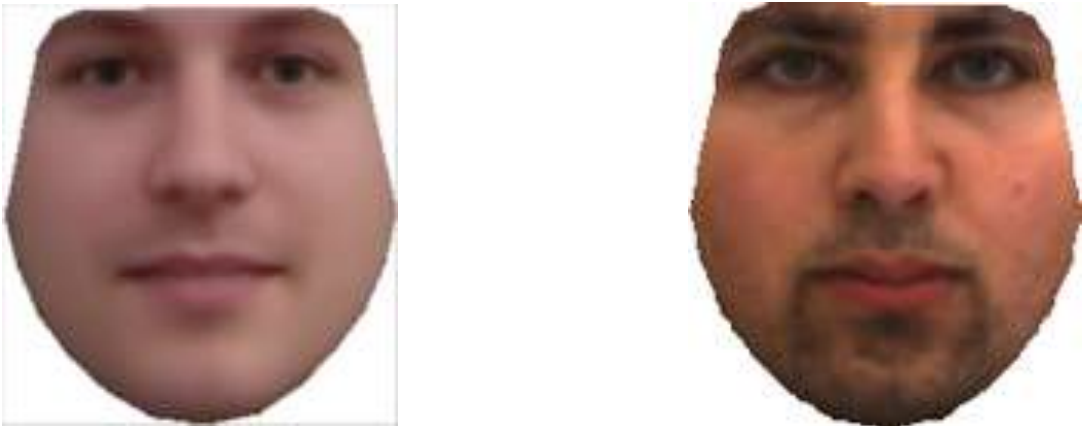


$$\arg \min_{\mathbf{p}, \lambda} \sum_{\mathbf{x} \in \mathbf{s}_0} \left[ \mathbf{A}_0(\mathbf{x}) + \sum_{i=1}^m \lambda_i \mathbf{A}_i(\mathbf{x}) - \mathbf{I}(\mathbf{W}(\mathbf{x}, \mathbf{p})) \right]^2$$



# Active Appearance Models (AAMs)

Fitting Goal



$$\arg \min_{\mathbf{p}, \boldsymbol{\lambda}} \sum_{\mathbf{x} \in \mathbf{s}_0} \left[ \mathbf{A}_0(\mathbf{x}) + \sum_{i=1}^m \lambda_i \mathbf{A}_i(\mathbf{x}) - \mathbf{I}(\mathbf{W}(\mathbf{x}, \mathbf{p})) \right]^2$$

Error Image



Solution

$$\begin{bmatrix} \Delta \mathbf{p} \\ \Delta \boldsymbol{\lambda} \end{bmatrix} = \mathbf{H}^{-1} \sum_{\mathbf{x} \in \mathbf{s}_0} \mathbf{J}(\mathbf{x}, \mathbf{p}, \boldsymbol{\lambda})^T \left( \mathbf{A}_0(\mathbf{x}) + \sum_{i=1}^m \lambda_i \mathbf{A}_i(\mathbf{x}) - \mathbf{I}(\mathbf{W}(\mathbf{x}, \mathbf{p})) \right)$$



10 ~ 20 shape 'images'

4 pose 'images'

60 ~ 80 appearance 'images'



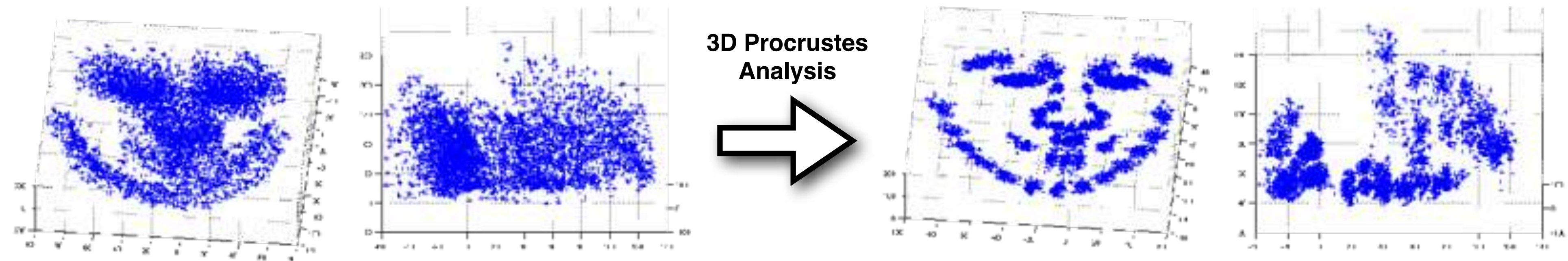
# 3D Shape Data



Left Camera

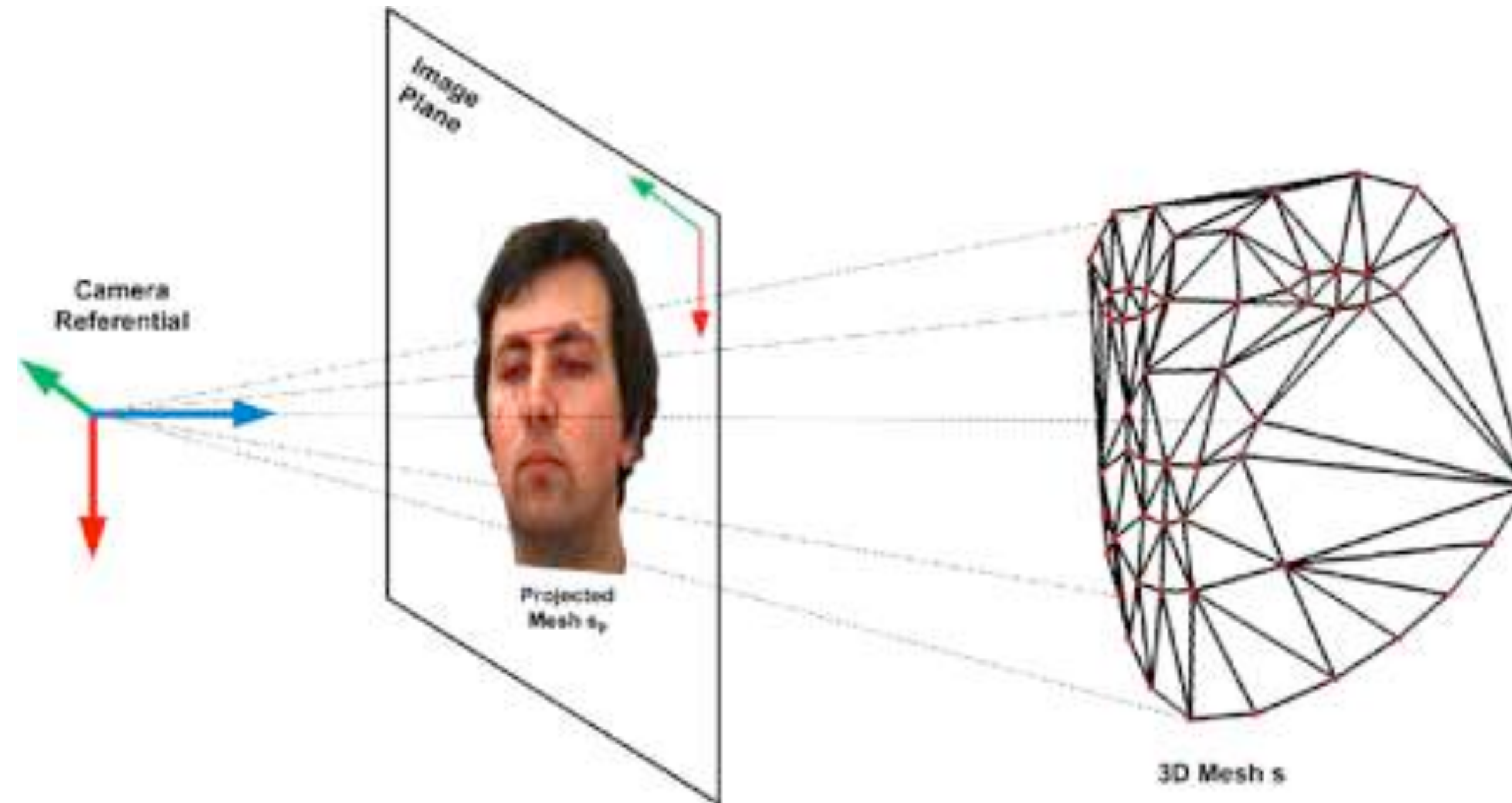
Right Camera

3D Shape



3D Procrustes Analysis

# 3D Shape Model - Perspective Projection

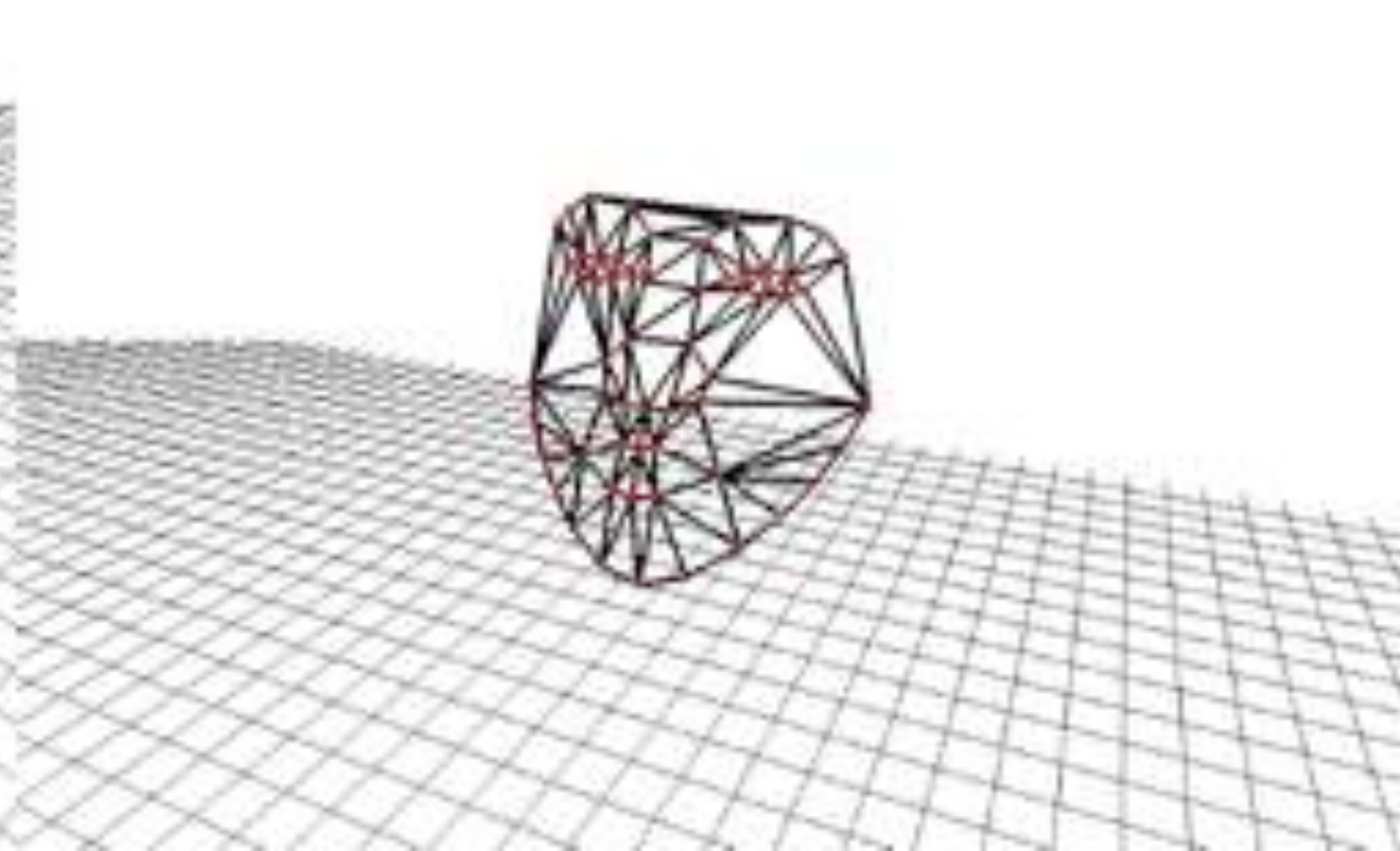
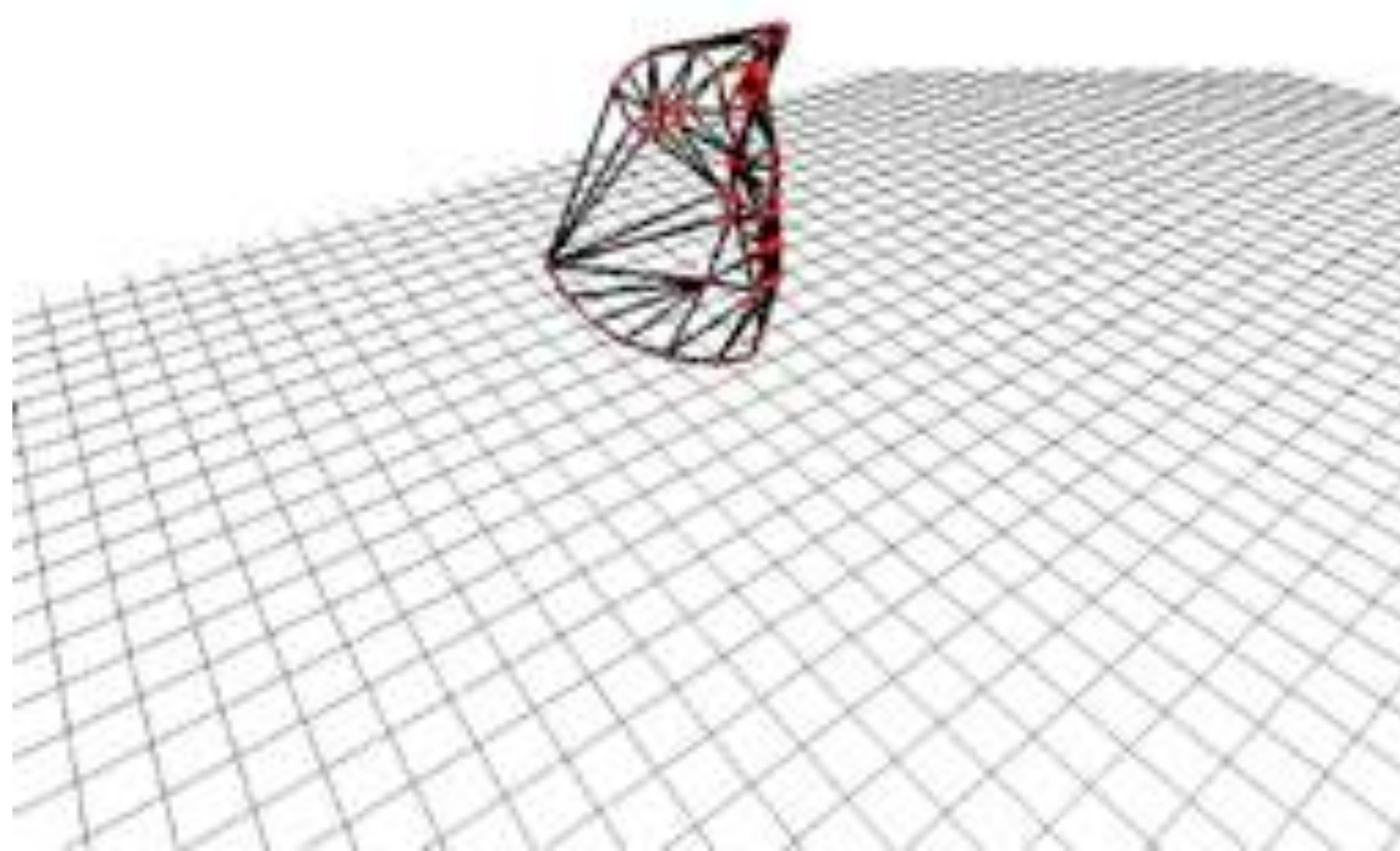
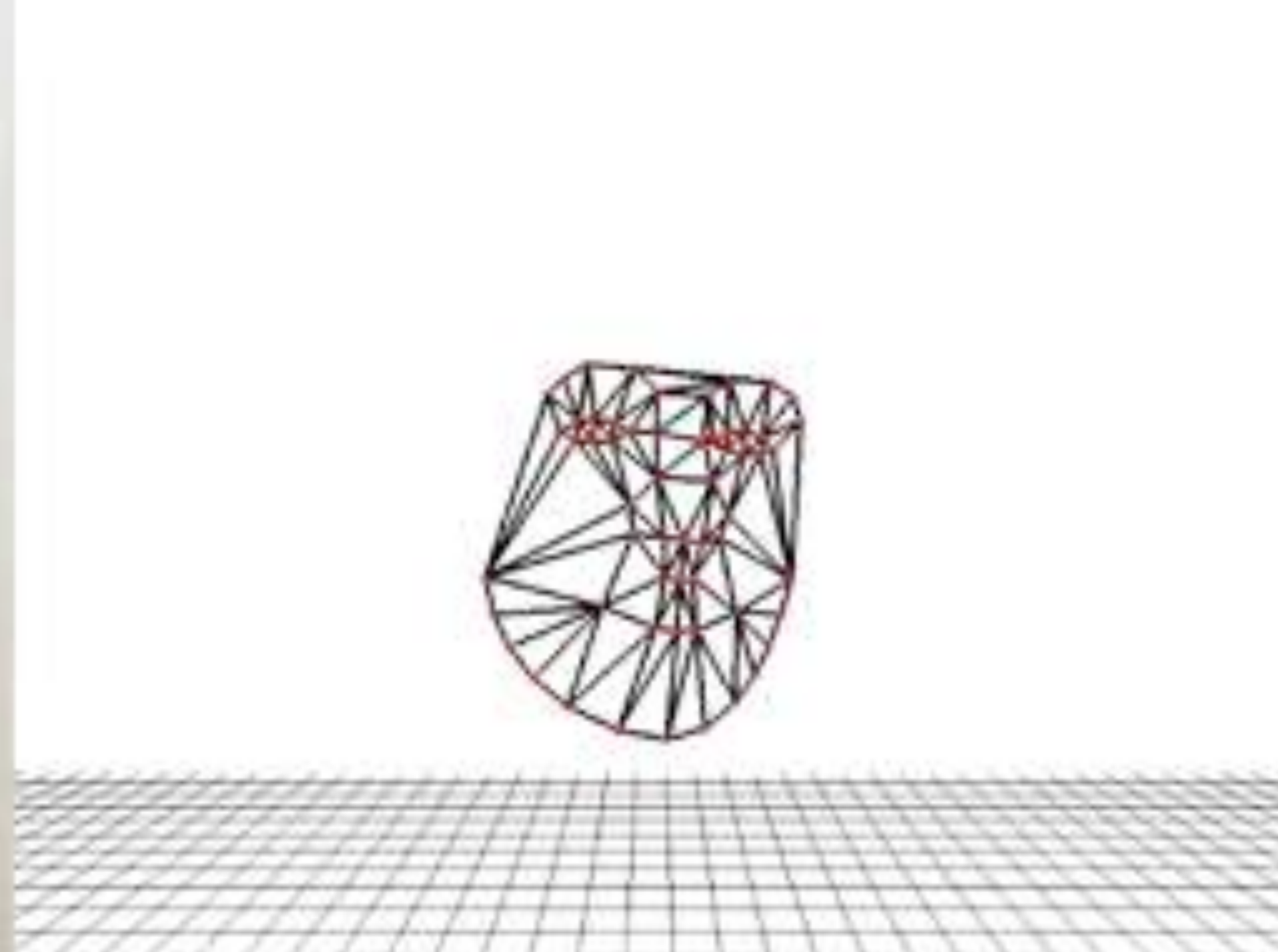


**Full Perspective Projection**

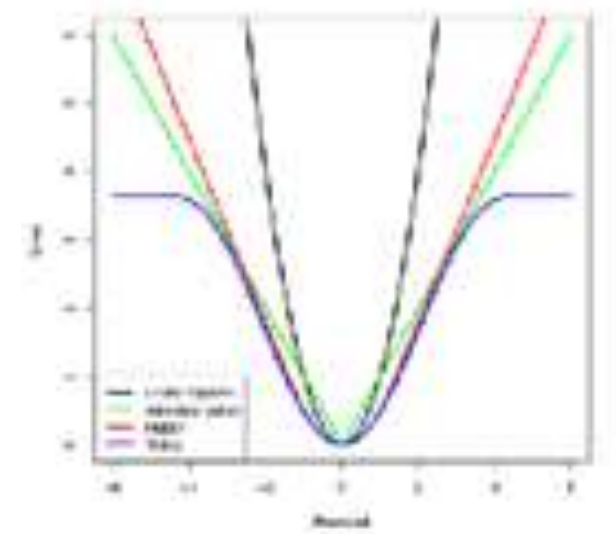
**3D Point Distribution Model (PDM)**

$$\begin{bmatrix} w(x_1 \cdots x_v) \\ w(y_1 \cdots y_v) \\ w \cdots w \end{bmatrix} = \underbrace{\begin{bmatrix} f_x & \alpha_s & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{bmatrix}}_{\mathbf{K}} \begin{bmatrix} \mathbf{R}_0 & | & \mathbf{t}_0 \end{bmatrix} \begin{bmatrix} s^{x_1} \cdots s^{x_v} \\ s^{y_1} \cdots s^{y_v} \\ s^{z_1} \cdots s^{z_v} \\ 1 \cdots 1 \end{bmatrix} \leftarrow s = s_0 + \sum_{i=1}^n p_i \phi_i + \underbrace{\sum_{j=1}^6 q_j \psi_j^{(t)} + \int_0^{t-1} \sum_{j=1}^6 q_j \psi_j^{(t)} \partial t}_{s_\psi}$$

↑ Pose Parameters
 ↑ Previous pose updates



# Robust 2.5D Model Fitting



$$\arg \min_{\mathbf{p}, \lambda} \sum_{\mathbf{x} \in \mathbf{s}_0}$$

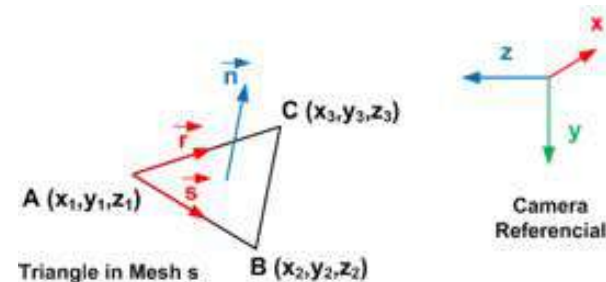
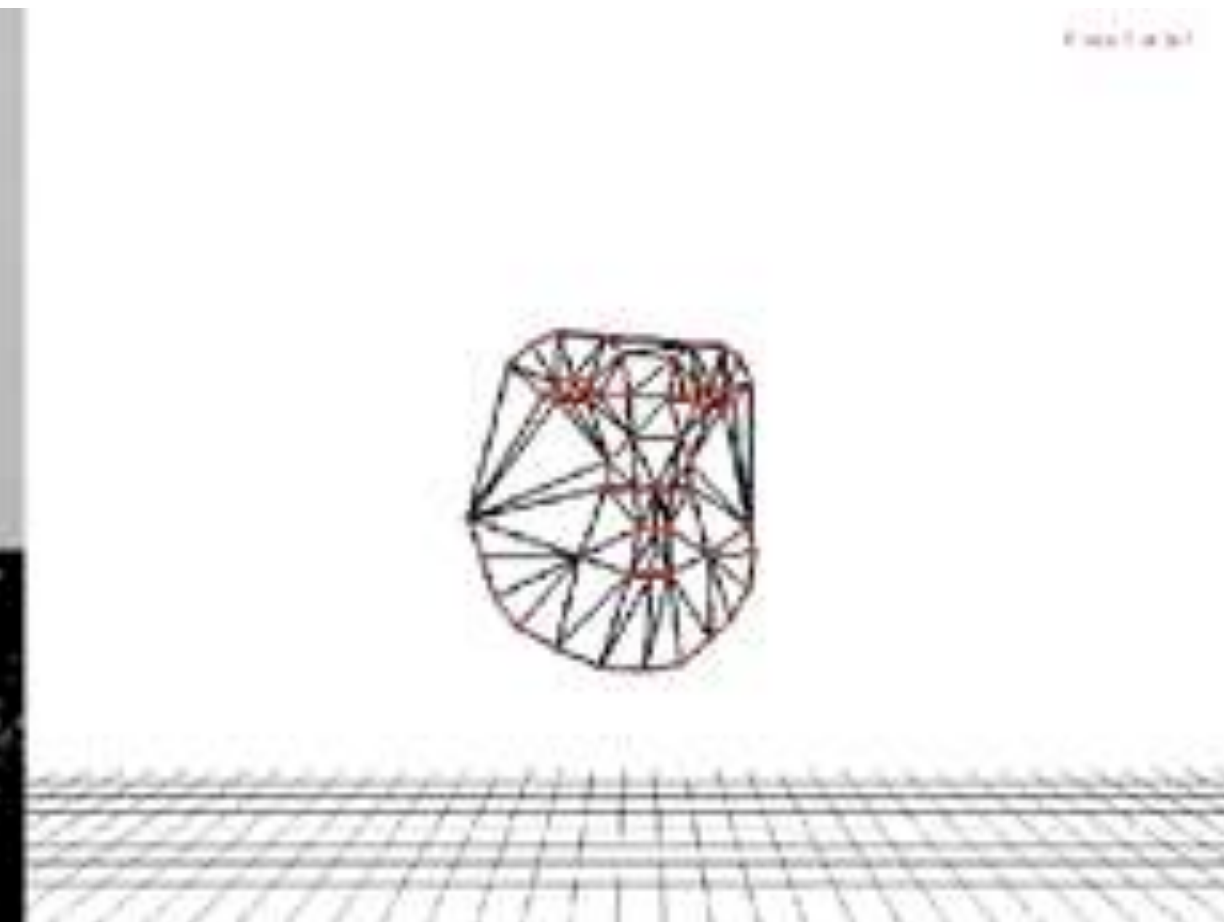
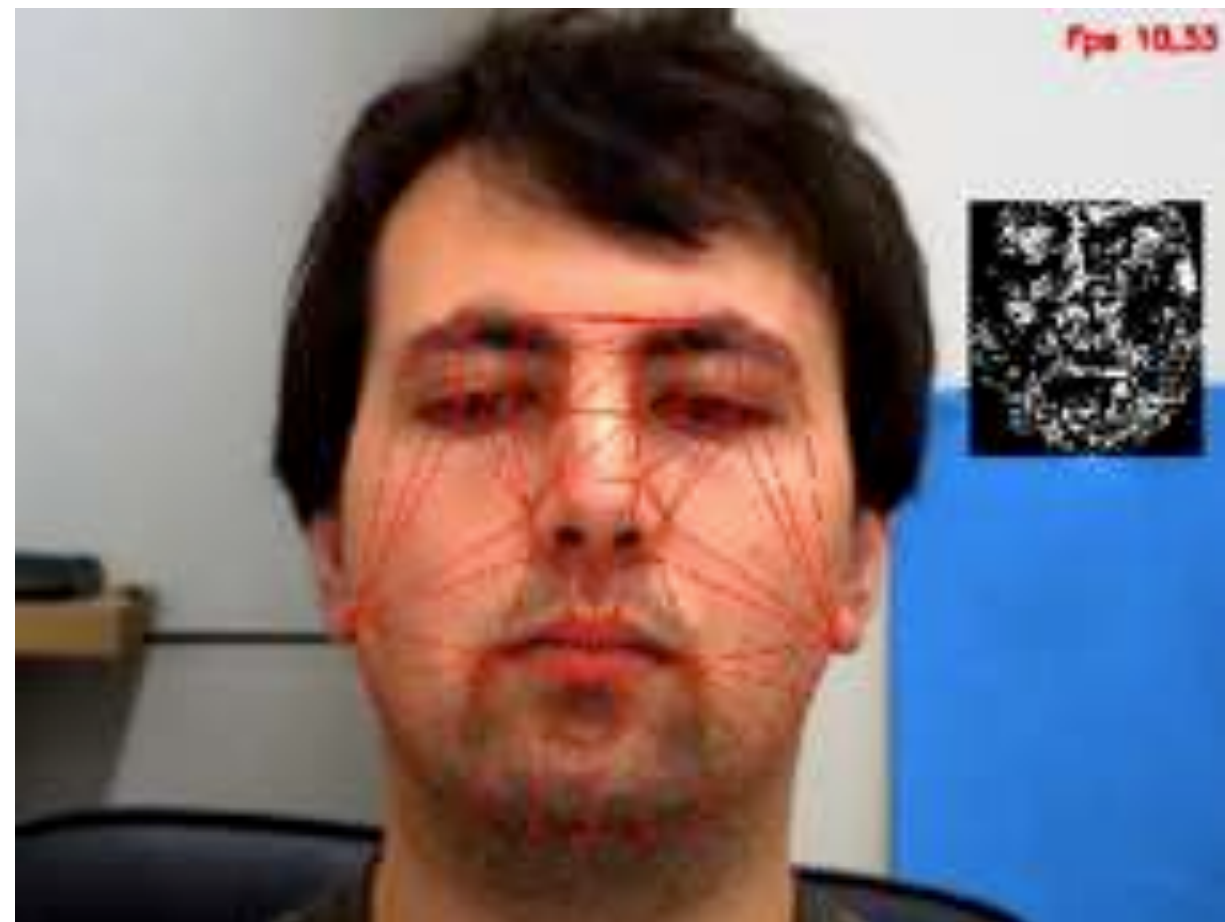
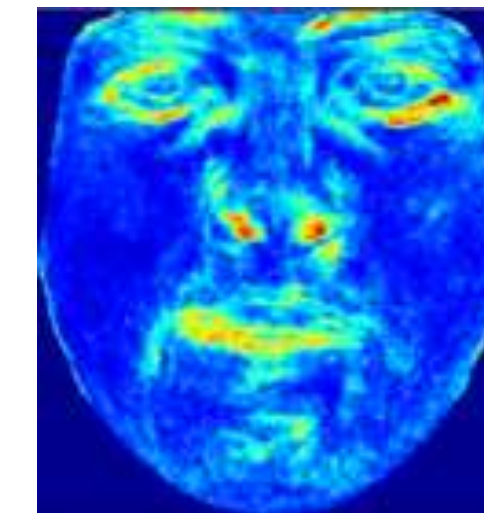


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~~2~~

$$\arg \min_{\mathbf{p}, \lambda} \sum_{\mathbf{x} \in \mathbf{s}_0} \rho(\mathbf{E}(\mathbf{x}), \underline{\sigma}) \longrightarrow$$

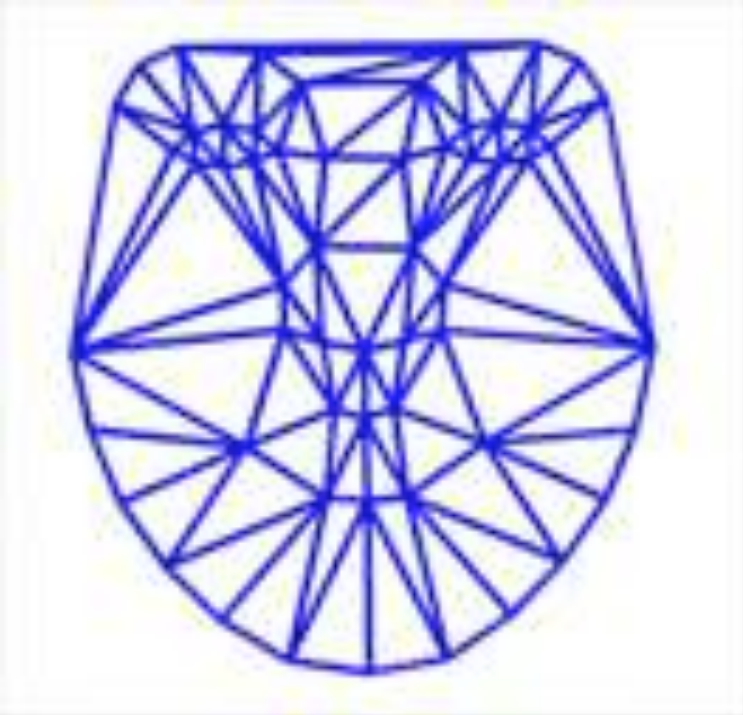




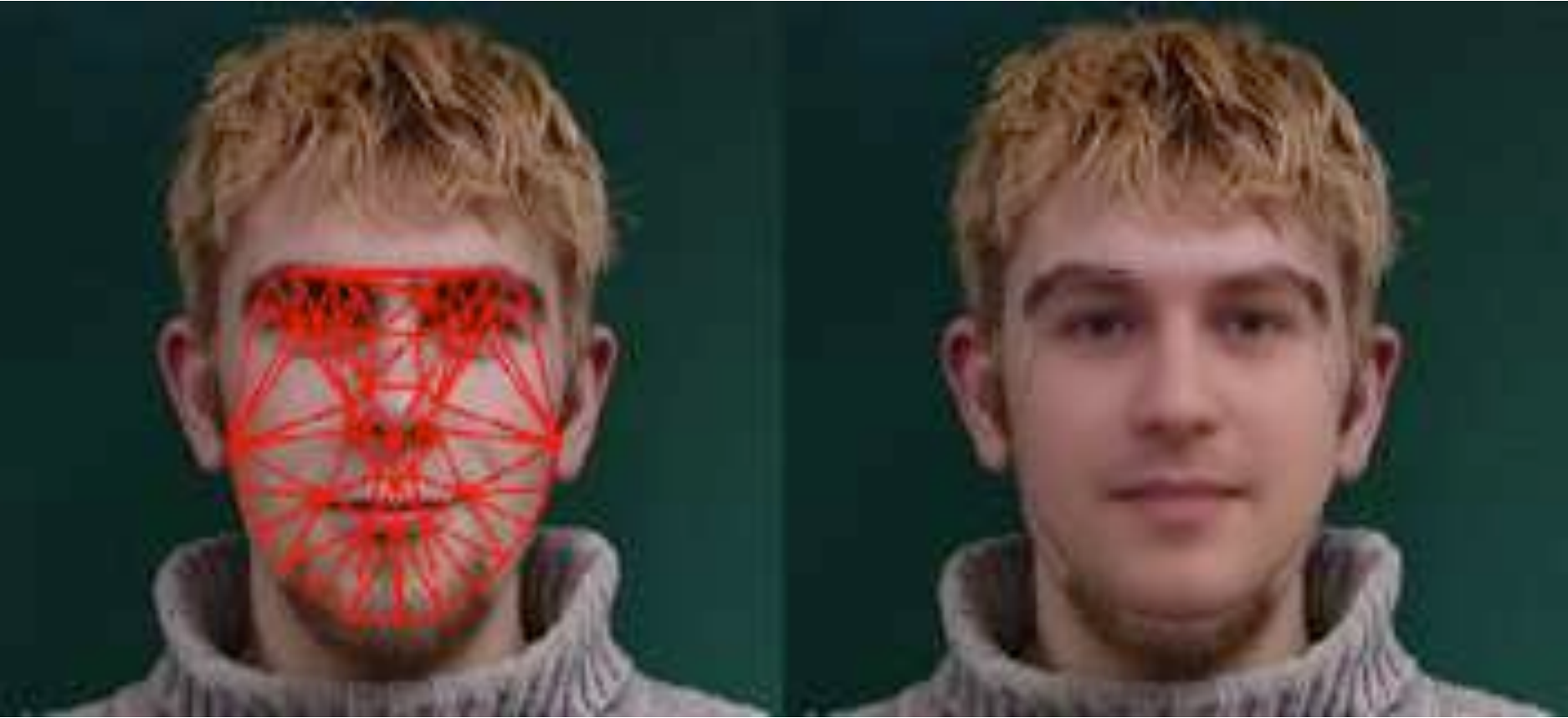
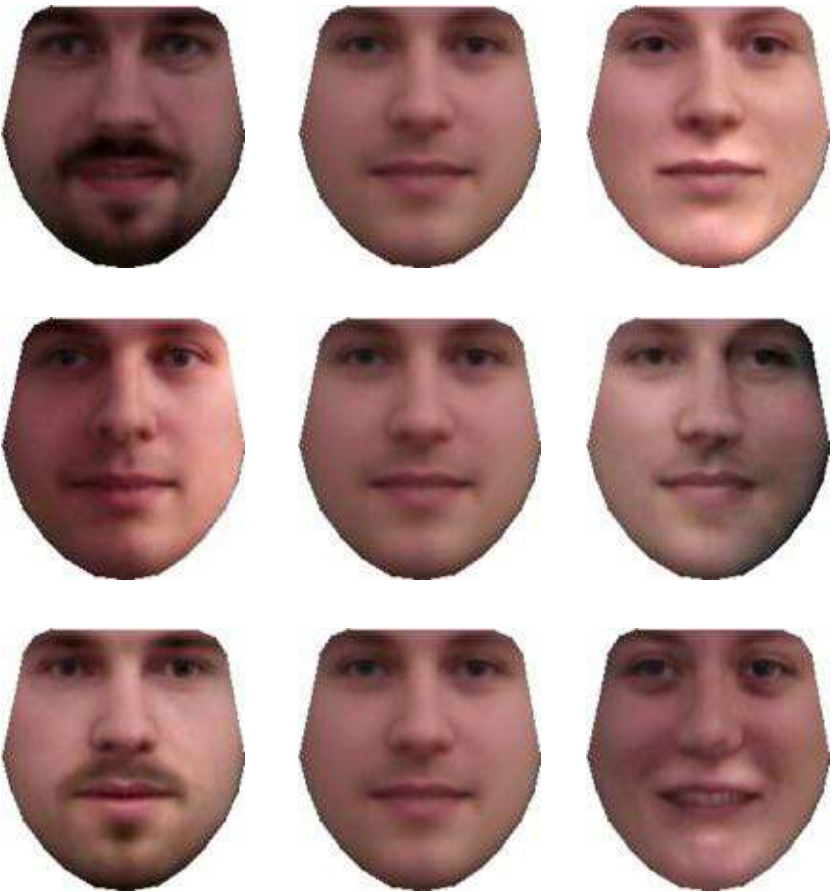
# Generative vs Discriminative Face Alignment

- **Generative / Holistic Appearance Model**

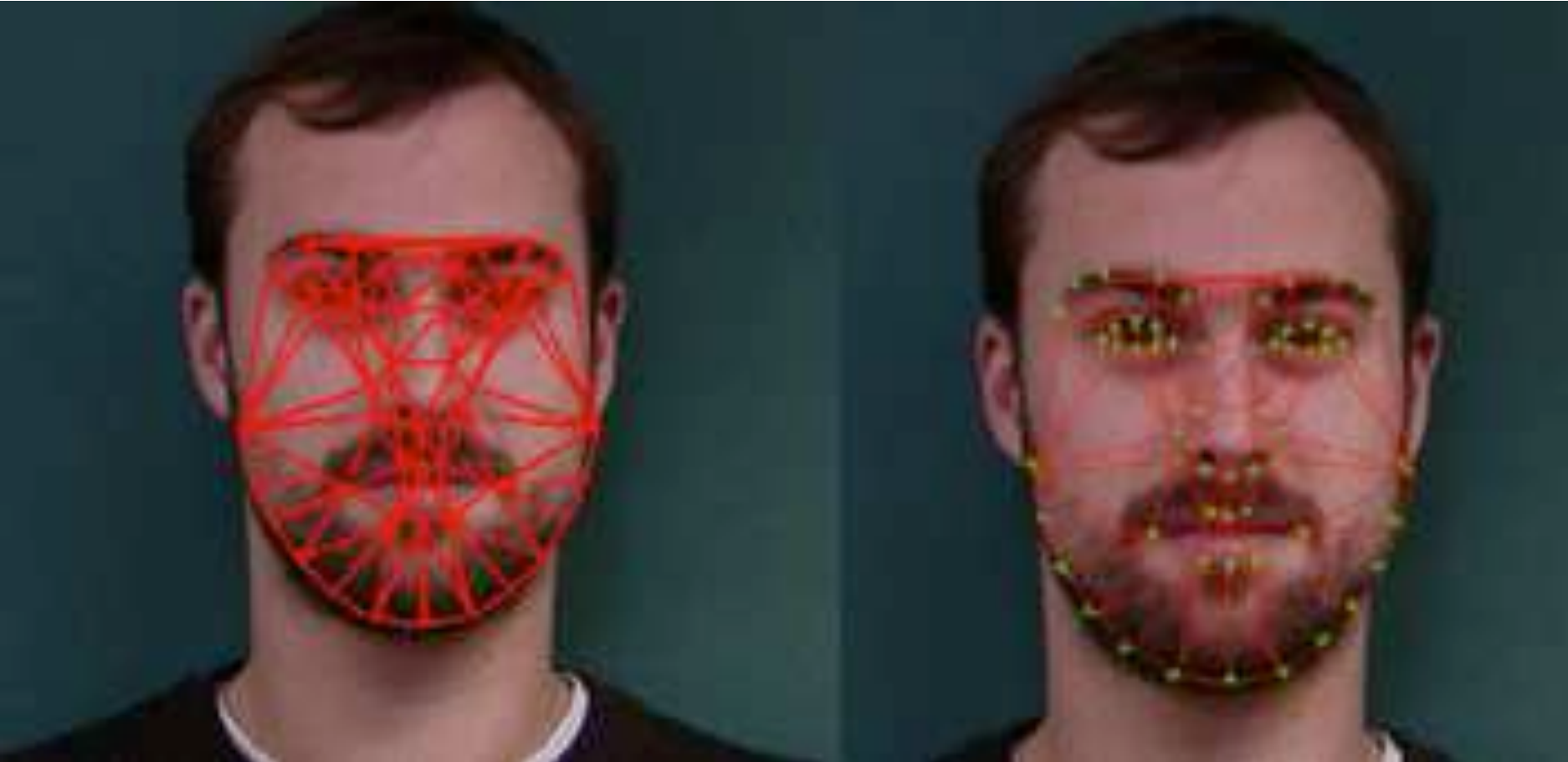
Shape Model



Point Distribution Model (PDM)



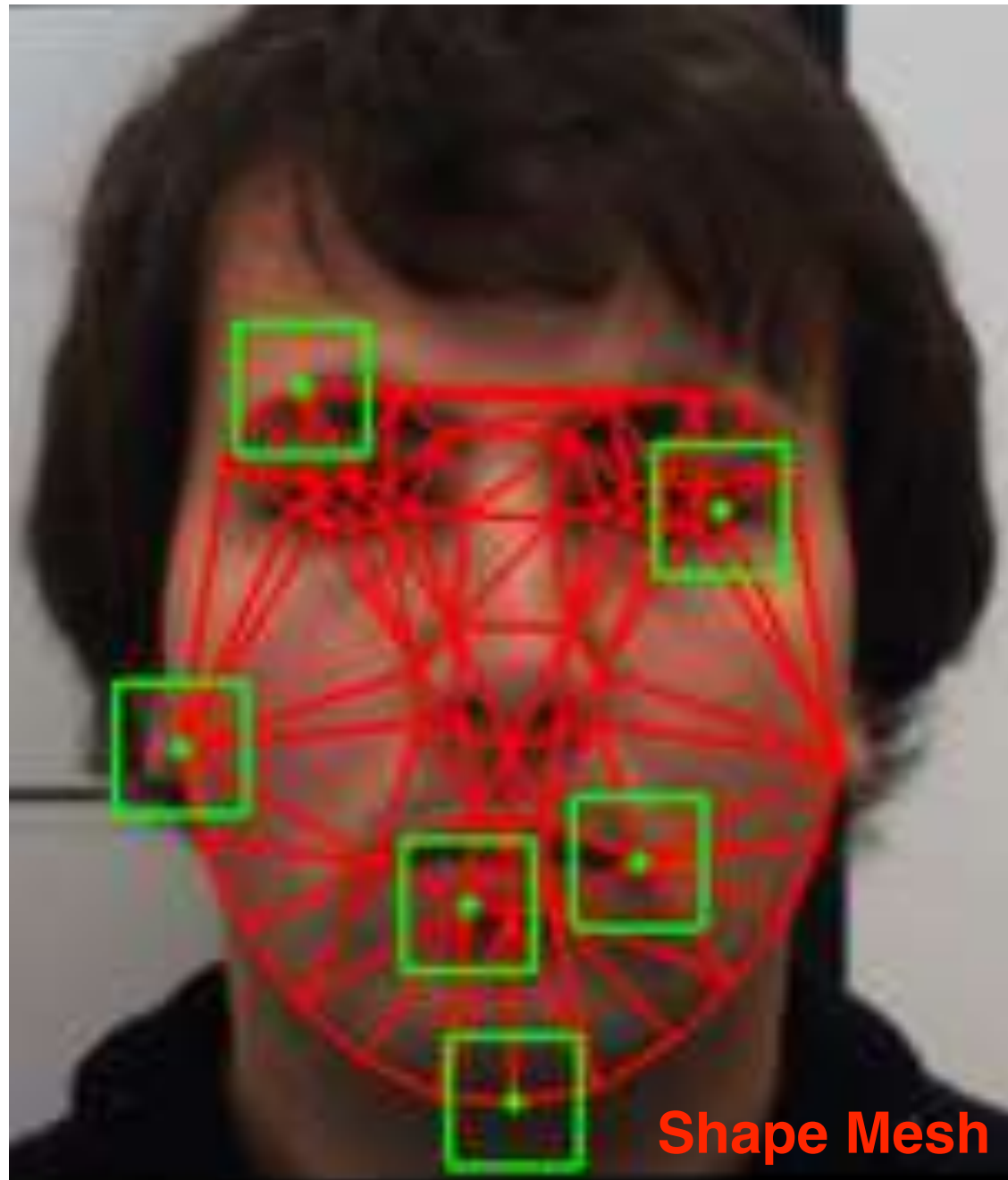
- **Discriminative / Patch Based Appearance Model**



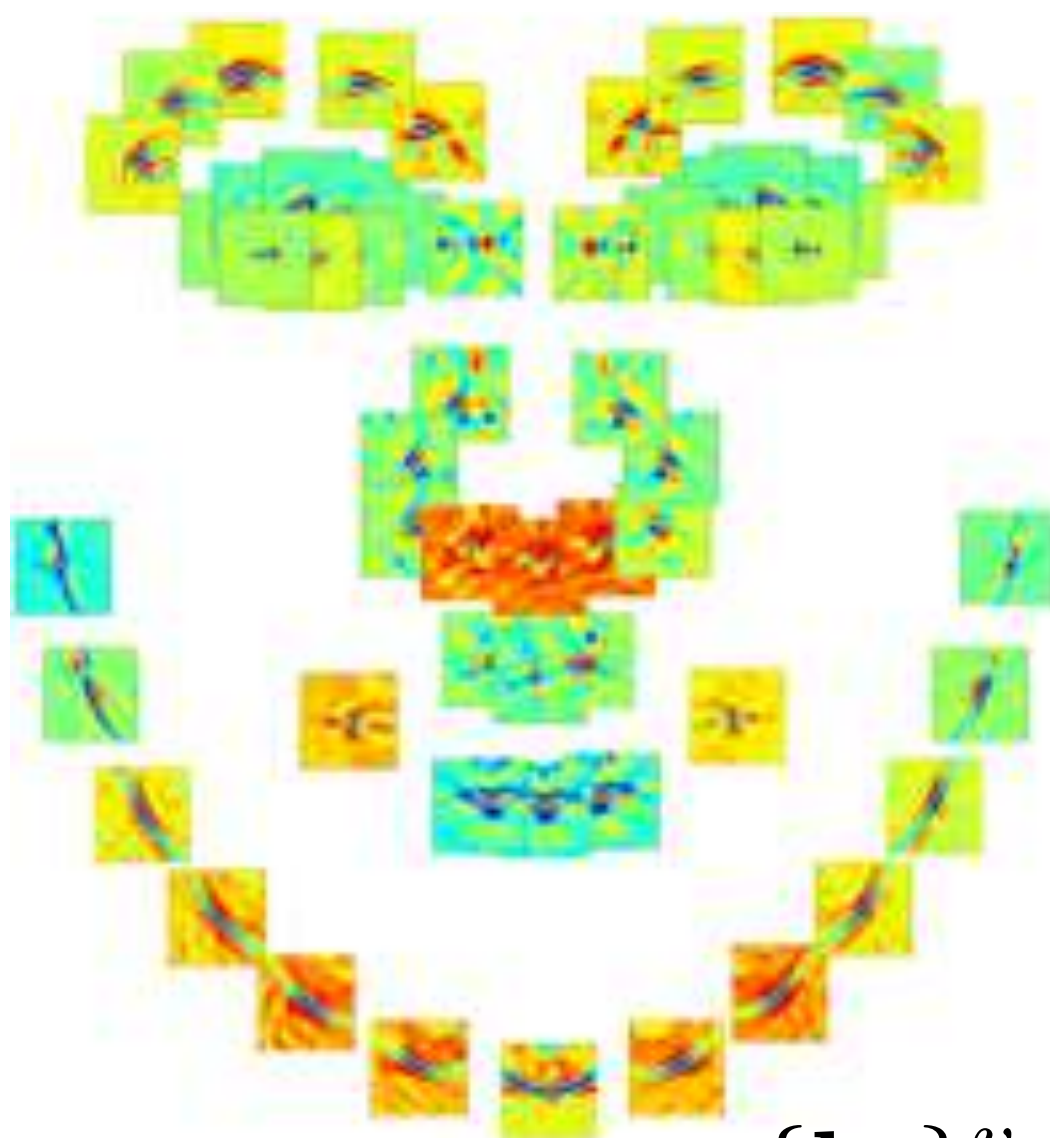
# Constrained Local Model (CLM)

$$\arg \max_{\mathbf{p}} \sum_{i=1}^v \text{Data Term} \quad \text{Regularization Term}$$

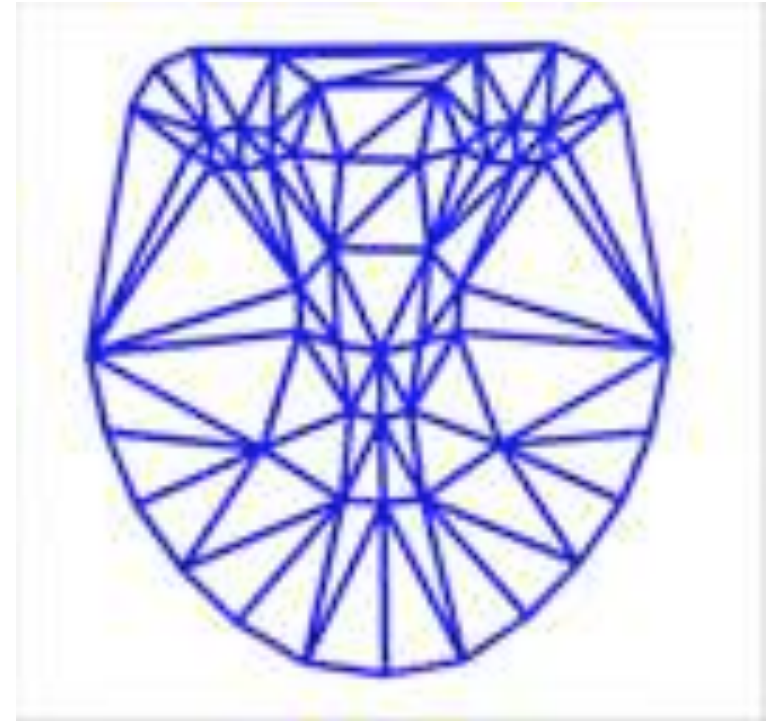
$$\arg \max_{\mathbf{p}} \sum_{i=1}^v \mathbf{I}(\mathbf{s}_i) * \mathbf{h}_i - \lambda_0 \mathbf{p}^T \Sigma_{\mathbf{p}}^{-1} \mathbf{p}$$



Local Search Regions



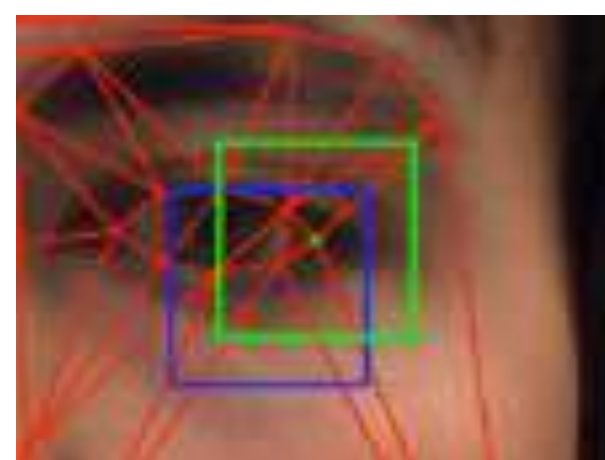
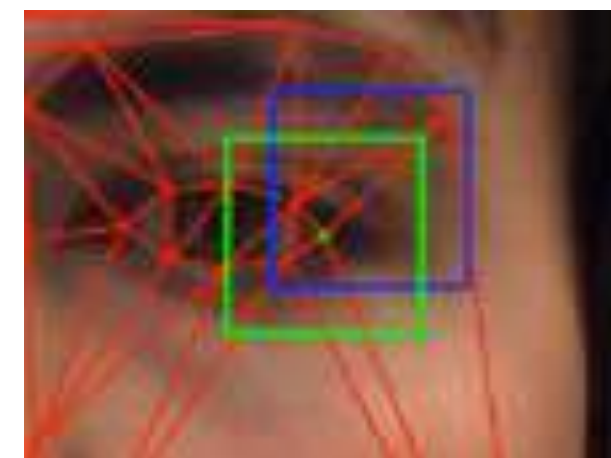
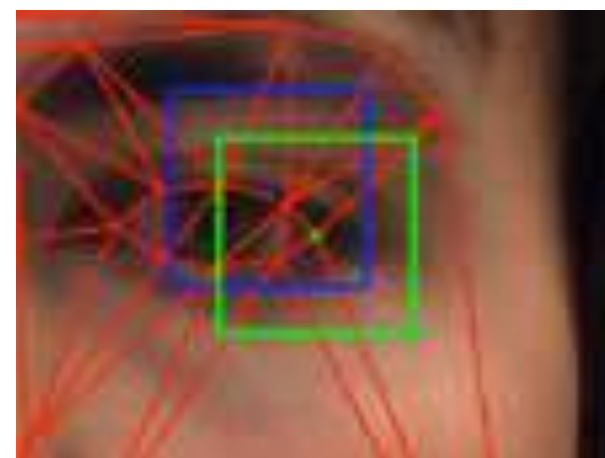
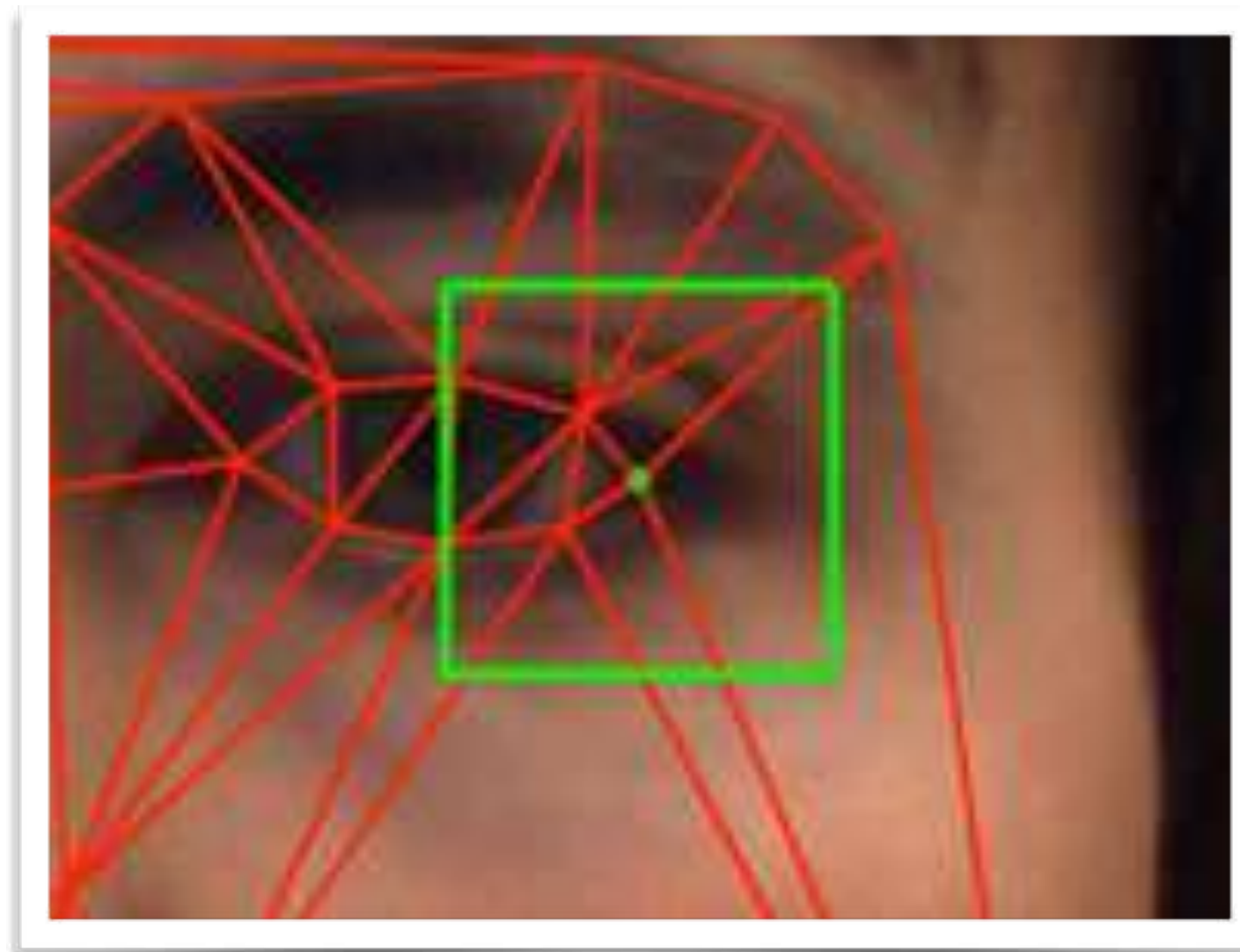
Local Detectors



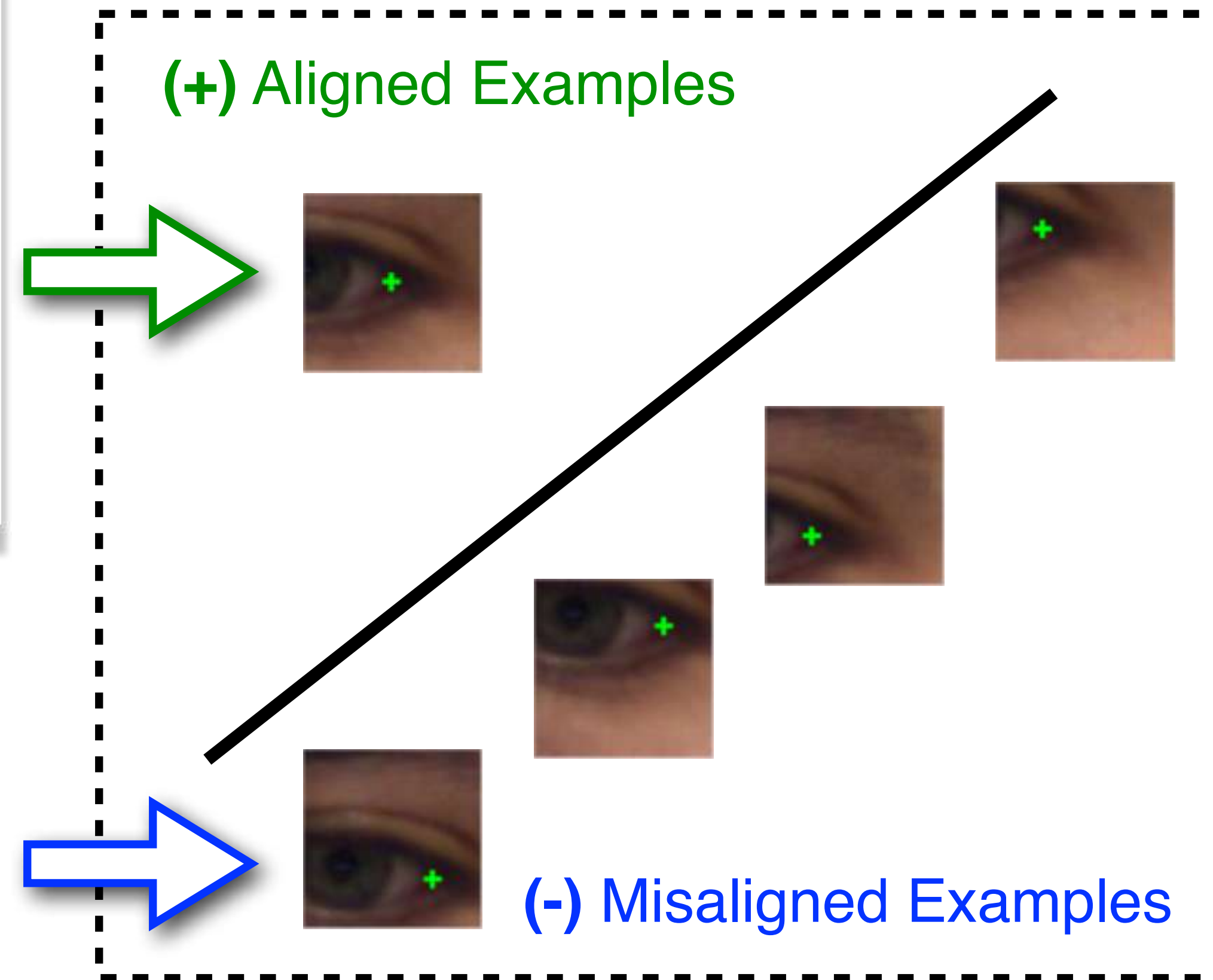
$$\mathbf{s} = \mathbf{s}_0 + \sum_{i=1}^n p_i \phi_i$$

Shape Model

# Local Landmark Detectors - SVM



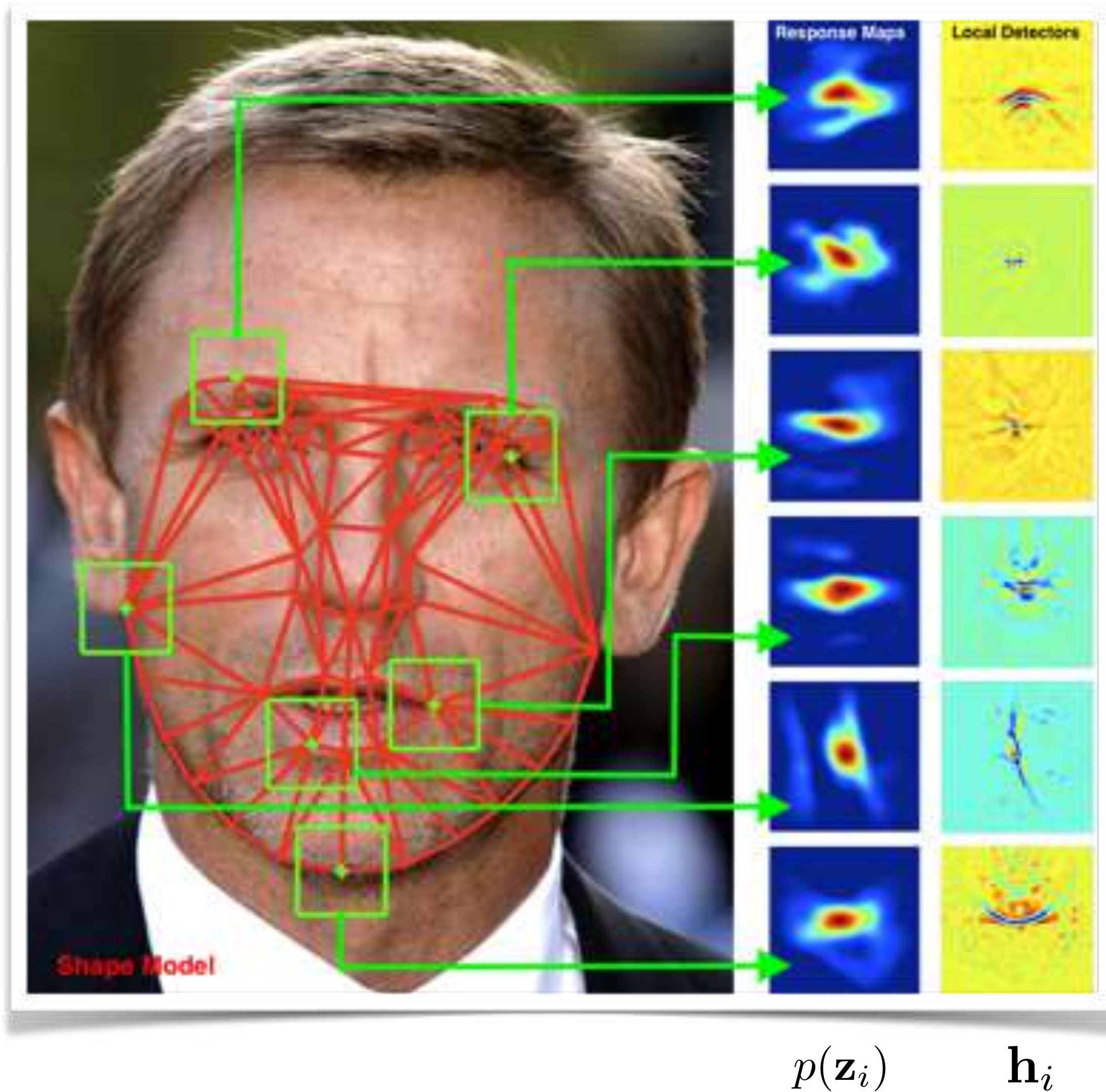
## Linear SVM



$$D_i^{\text{linear}}(\mathbf{I}(\mathbf{y}_i)) = \mathbf{w}_i^T \mathbf{I}(\mathbf{y}_i) + b_i$$

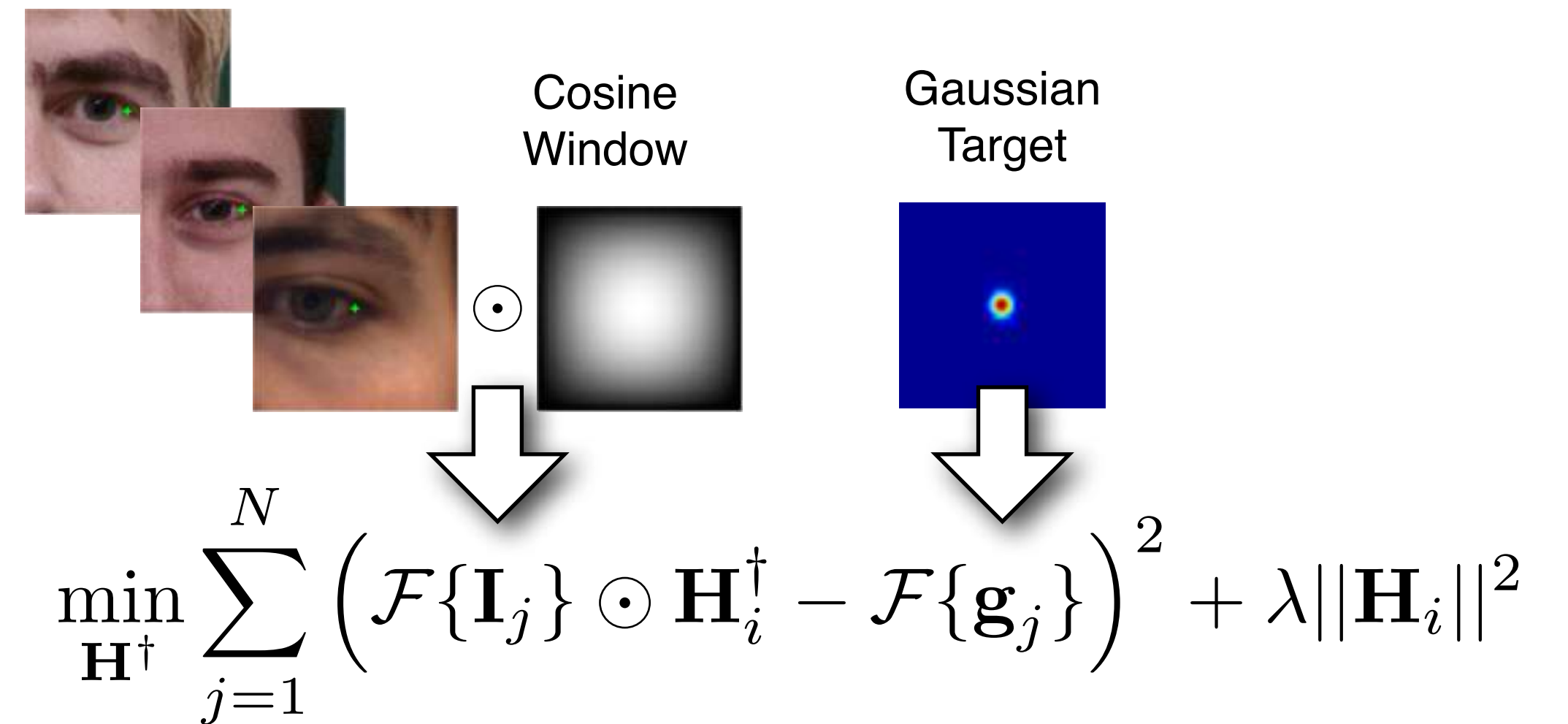
$i = 1, \dots, v$  landmarks

# Local Landmark Detectors (MOSSE Filters)



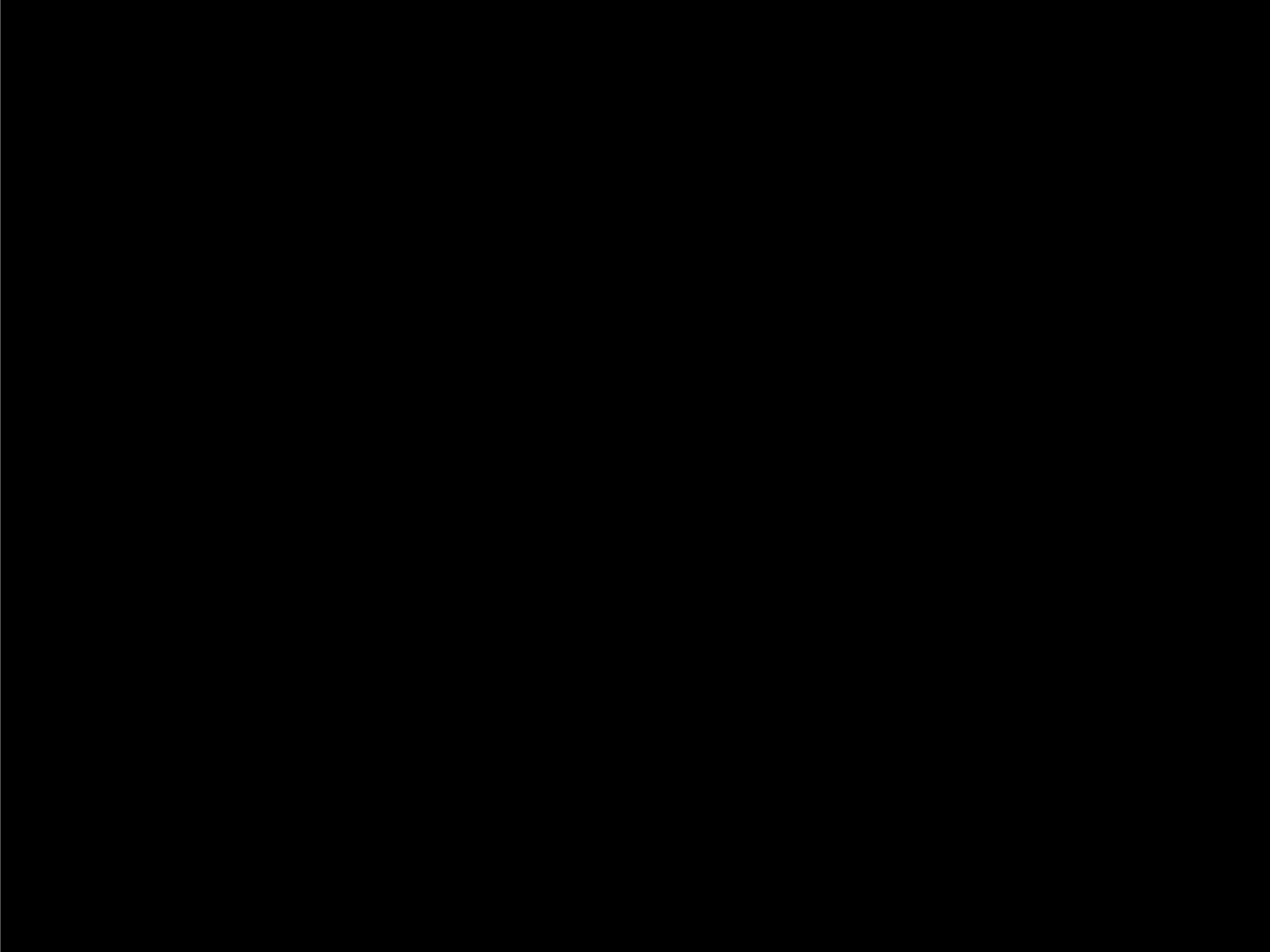
## Regression Problem

$$\arg \min_{\mathbf{h}_i} \sum_{j=1}^N (\mathbf{h}_i * \mathbf{I}_j - \mathbf{g}_j)^2 + \lambda \|\mathbf{h}_i\|^2$$



solution (spatial domain)

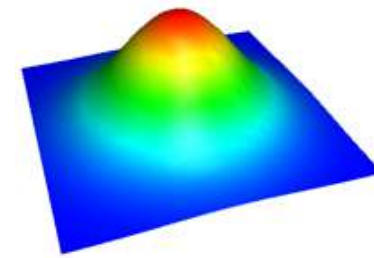
$$\mathbf{h}_i = \mathcal{F}^{-1} \left\{ \frac{\sum_{j=1}^N \mathcal{F}\{\mathbf{g}_j\} \odot \mathcal{F}\{\mathbf{I}_j\}^\dagger}{\sum_{j=1}^N \mathcal{F}\{\mathbf{I}_j\} \odot \mathcal{F}\{\mathbf{I}_j\}^\dagger + \lambda} \right\}^\dagger$$



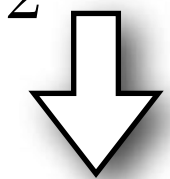
# Bayesian Inference CLM

$$\hat{\mathbf{b}} = \arg \max_{\mathbf{b}} p(\mathbf{b}|\mathbf{y}) \propto p(\mathbf{y}|\mathbf{b})p(\mathbf{b})$$

Likelihood Term



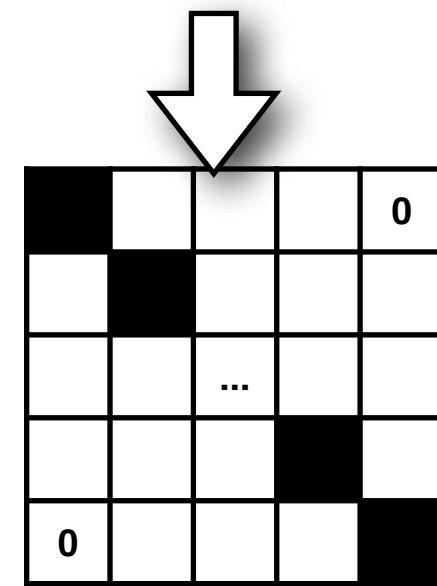
$$p(\mathbf{y}|\mathbf{b}) \propto \exp\left(-\frac{1}{2}(\mathbf{y} - (\mathbf{s}_0 + \Phi\mathbf{b}))^T \Sigma_{\mathbf{y}}^{-1} (\mathbf{y} - (\mathbf{s}_0 + \Phi\mathbf{b}))\right)$$



Shape  
Observation



$(\mathbf{y}, \Sigma_{\mathbf{y}})$



$2v \times 2v$   
Block diagonal

Uncertainty  
Covariance

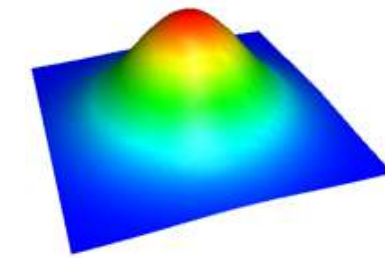
**Linear Dynamic System (LDS)**

$$\begin{aligned} \mathbf{b}_l &= \mathbf{I}_n \mathbf{b}_{l-1} + q, & q &\sim \mathcal{N}(\mathbf{0}, \Lambda) \\ \mathbf{y} - \mathbf{s}_0 &= \Phi \mathbf{b}_l + r, & r &\sim \mathcal{N}(\mathbf{0}, \Sigma_{\mathbf{y}}) \end{aligned}$$

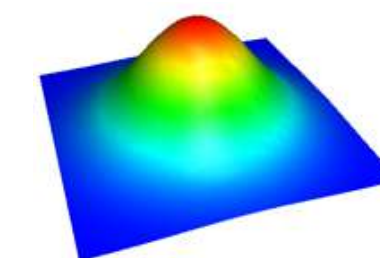
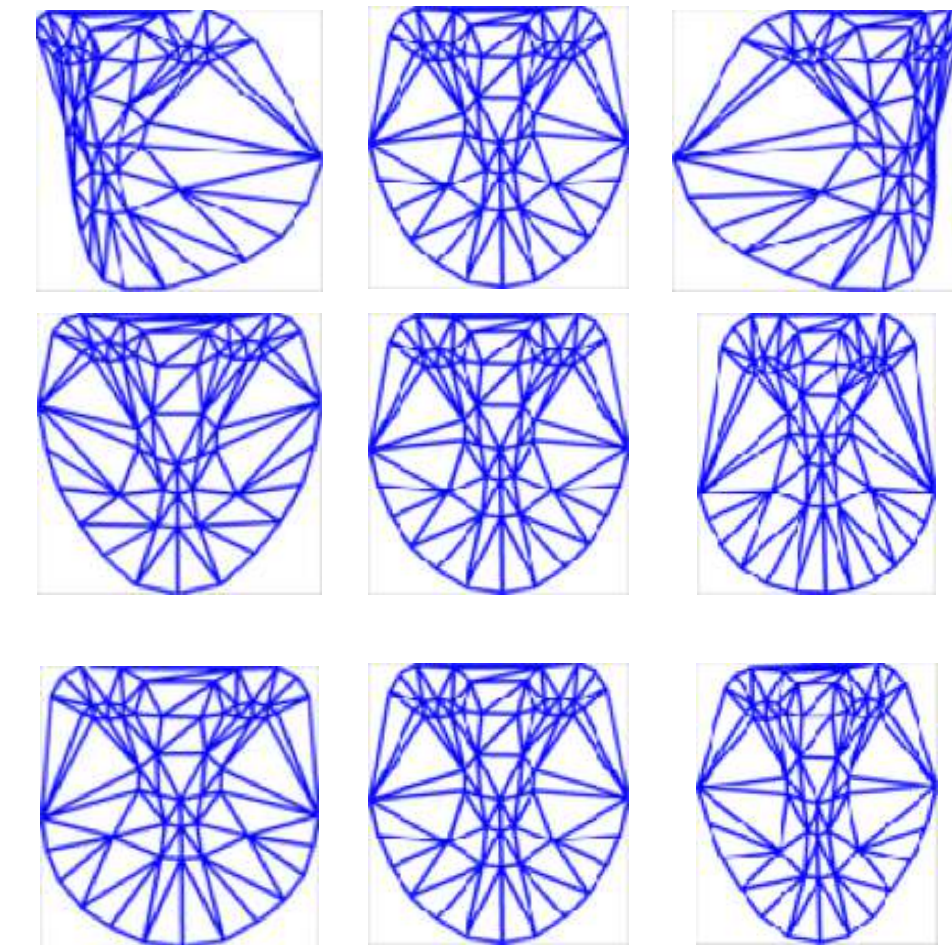
**Posterior Term**

$$p(\mathbf{b}_l | \mathbf{y}_l, \dots, \mathbf{y}_0) \propto \mathcal{N}(\mathbf{b}_l | \boldsymbol{\mu}_l^{\mathbf{F}}, \boldsymbol{\Sigma}_l^{\mathbf{F}})$$

Prior Term

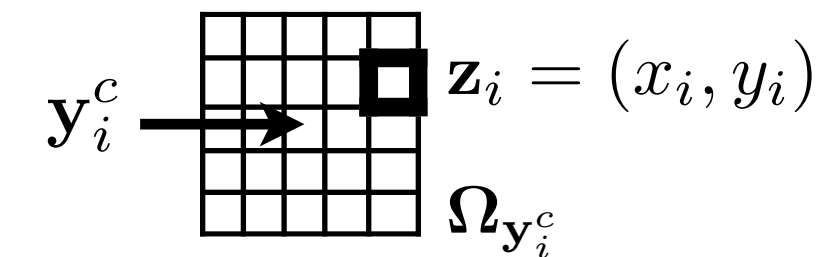
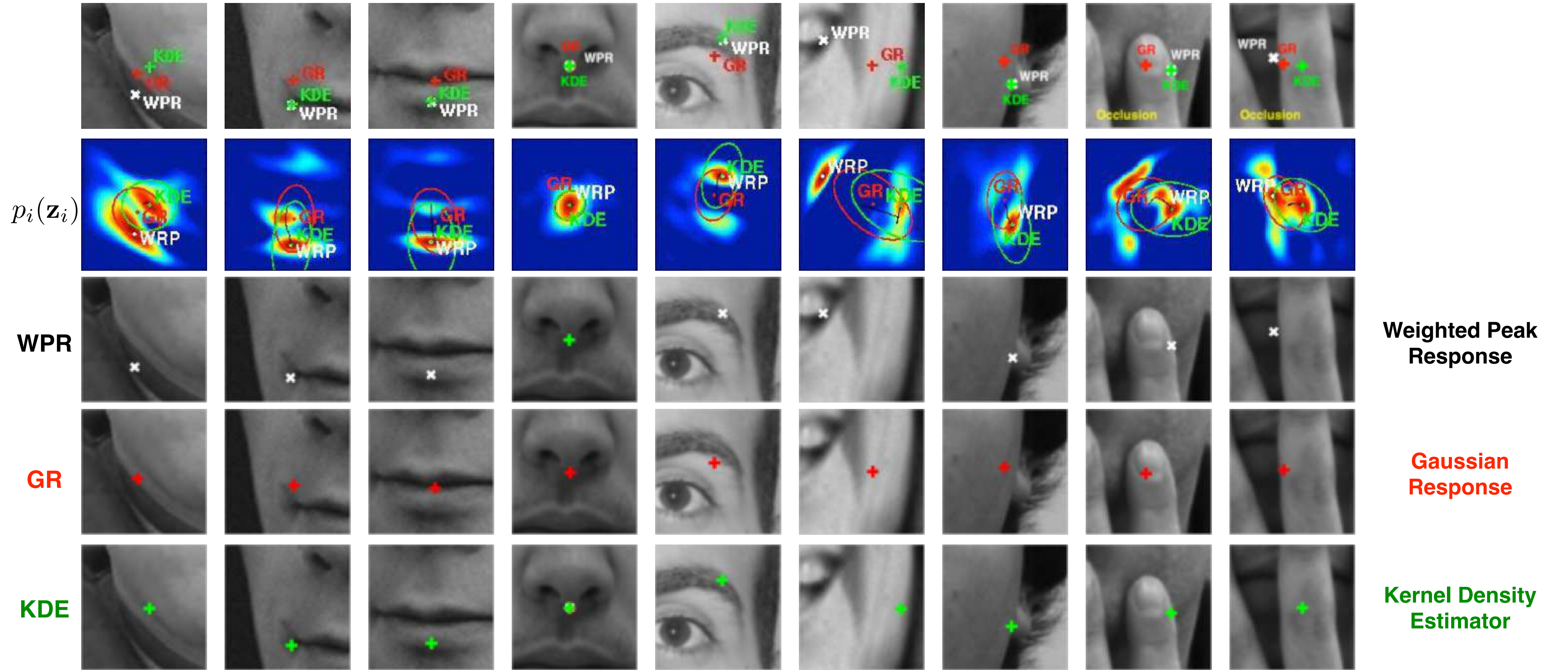


$$p(\mathbf{b}) \propto \mathcal{N}(\mathbf{b} | \mathbf{0}, \Lambda)$$



# Local Optimization Strategies

Patches under occlusion



**Weighted Peak Response**

$$\mathbf{y}_i^{\text{WPR}} = \max_{\mathbf{z}_i \in \Omega_{\mathbf{y}_i^c}} (p_i(\mathbf{z}_i))$$

$$\Sigma_{\mathbf{y}_i}^{\text{WPR}} = \text{diag}(p_i(\mathbf{y}_i^{\text{WPR}})^{-1})$$

**Gaussian Response**

$$\mathbf{y}_i^{\text{GR}} = \frac{1}{d} \sum_{\mathbf{z}_i \in \Omega_{\mathbf{y}_i^c}} p_i(\mathbf{z}_i) \mathbf{z}_i \quad d = \sum_{\mathbf{z}_i \in \Omega_{\mathbf{y}_i^c}} p_i(\mathbf{z}_i)$$

$$\Sigma_{\mathbf{y}_i}^{\text{GR}} = \frac{1}{d-1} \sum_{\mathbf{z}_i \in \Omega_{\mathbf{y}_i^c}} p_i(\mathbf{z}_i) (\mathbf{z}_i - \mathbf{y}_i^{\text{GR}})(\mathbf{z}_i - \mathbf{y}_i^{\text{GR}})^T$$

**Kernel Density Estimator**

$$\mathbf{y}_i^{\text{KDE}(\tau+1)} \leftarrow \frac{\sum_{\mathbf{z}_i \in \Omega_{\mathbf{y}_i^c}} \mathbf{z}_i p_i(\mathbf{z}_i) \mathcal{N}(\mathbf{y}_i^{\text{KDE}(\tau)} | \mathbf{z}_i, \sigma_{h_j}^2 \mathbf{I}_2)}{\sum_{\mathbf{z}_i \in \Omega_{\mathbf{y}_i^c}} p_i(\mathbf{z}_i) \mathcal{N}(\mathbf{y}_i^{\text{KDE}(\tau)} | \mathbf{z}_i, \sigma_{h_j}^2 \mathbf{I}_2)}$$

$$\Sigma_{\mathbf{y}_i}^{\text{KDE}} = \frac{1}{d-1} \sum_{\mathbf{z}_i \in \Omega_{\mathbf{y}_i^c}} p_i(\mathbf{z}_i) (\mathbf{z}_i - \mathbf{y}_i^{\text{KDE}})(\mathbf{z}_i - \mathbf{y}_i^{\text{KDE}})^T$$





# Non-Parametric Bayesian Inference CLM

$$\hat{\mathbf{b}} = \arg \max_{\mathbf{b}} p(\mathbf{b}|\mathbf{y}) \propto p(\mathbf{y}|\mathbf{b})p(\mathbf{b})$$

Posterior Expectation

$$\hat{\mathbf{b}}_k = \frac{1}{N} \sum_{i=1}^N \tilde{\mathbf{b}}_k^{(i)}$$

Kernel Density Estimator (KDE)

$$p(\mathbf{b}_k | \mathbf{y}_k, \dots, \mathbf{y}_0) \approx \sum_{i=1}^N w_k^{(i)} K_h(\mathbf{b}_k - \mathbf{b}_k^{(i)})$$

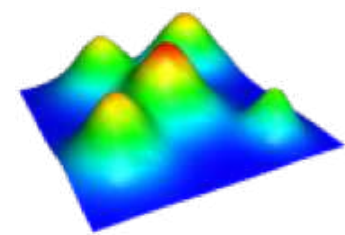
$$\{w_k^{(i)}, \mathbf{b}_k^{(i)}\}_{i=1}^N$$

(i) - Particle (possible shape)  
(k) - Iteration

Inference by a Regularized Particle Filter (RPF)

$$w_k^{(i)} \propto p(\mathbf{y}_k | \mathbf{b}_k^{(i)}) = \rho \left( \prod_{j=1}^v p(a_j = 1 | \mathcal{D}_j, \mathbf{I}(\mathbf{y}_j)); \sigma \right)$$

$$\mathbf{b}_k^{(i)} \sim p(\mathbf{b}_k | \mathbf{b}_{k-1}^{(i)}) \propto \mathcal{N}(\mathbf{b}_k | \mathbf{b}_{k-1}, \Sigma_{\mathbf{b}})$$



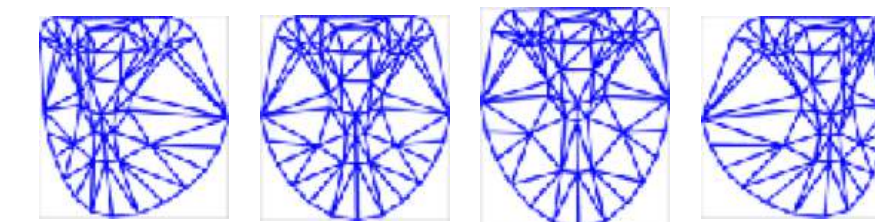
Posterior Term

Posterior

Likelihood

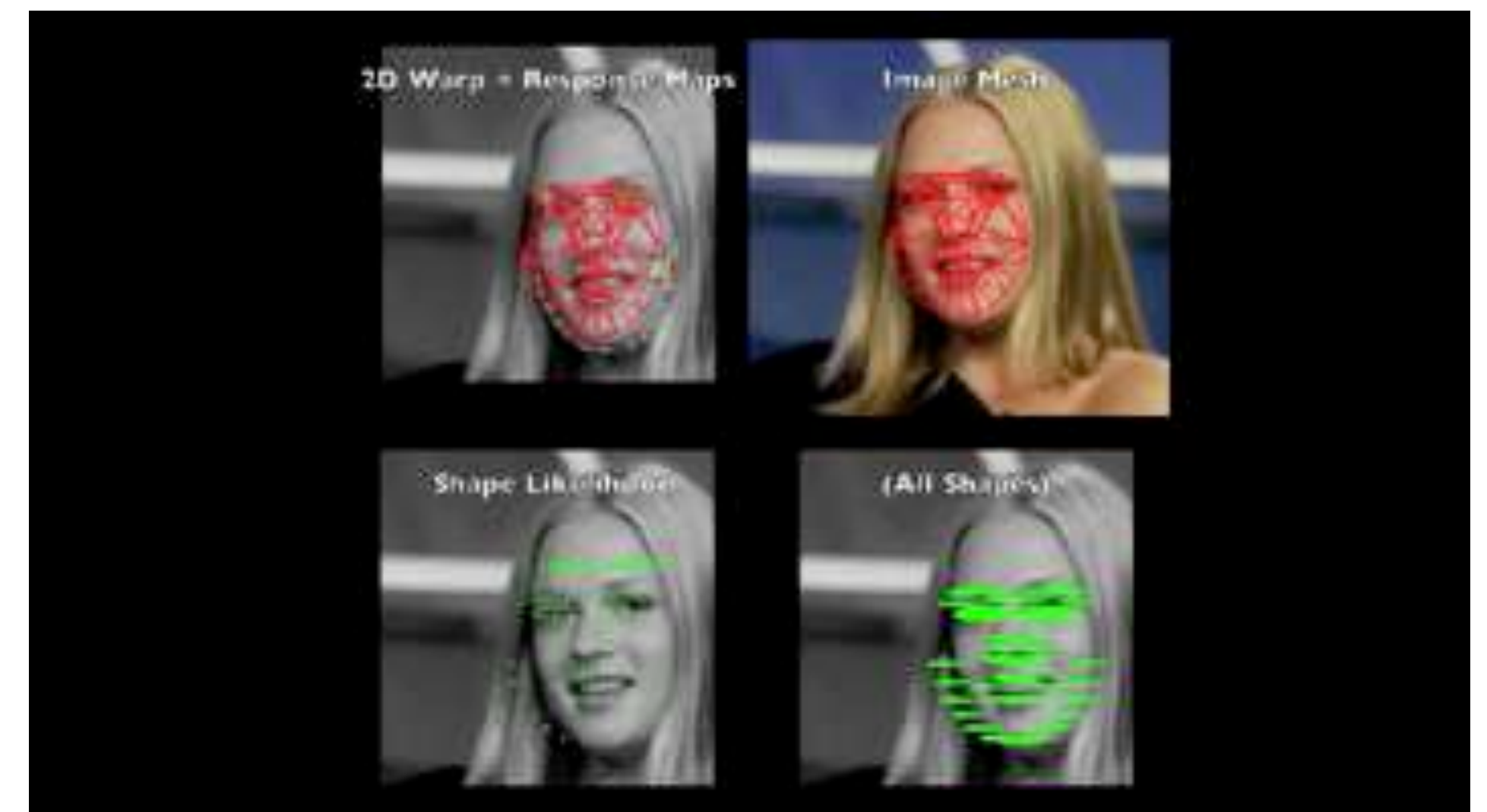
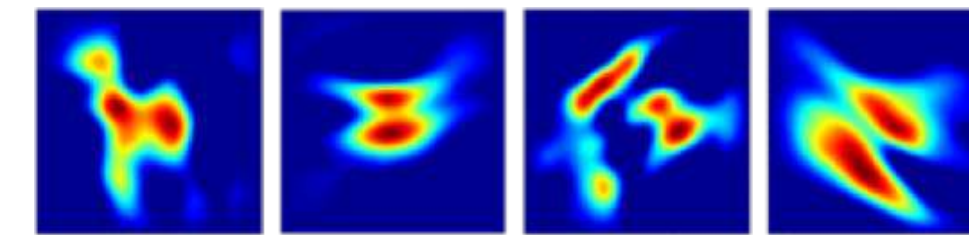
Prior

Prior Term



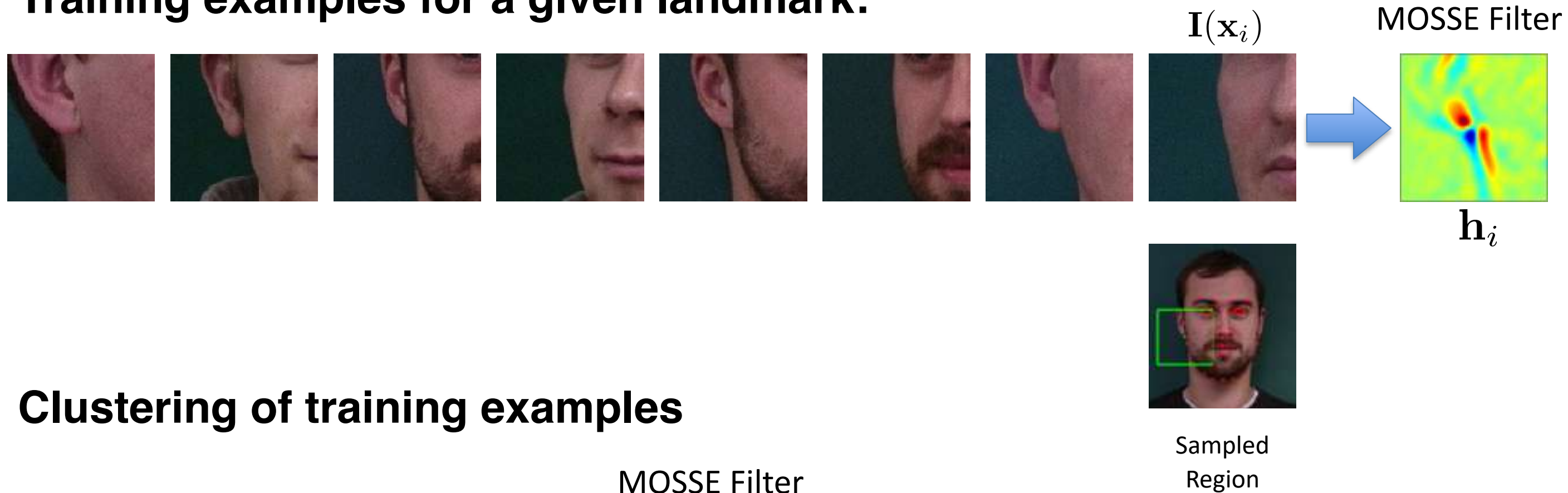
$$p(\mathbf{b}) \propto \mathcal{N}(\mathbf{b} | \mathbf{0}, \Lambda)$$

Multimodal Likelihood

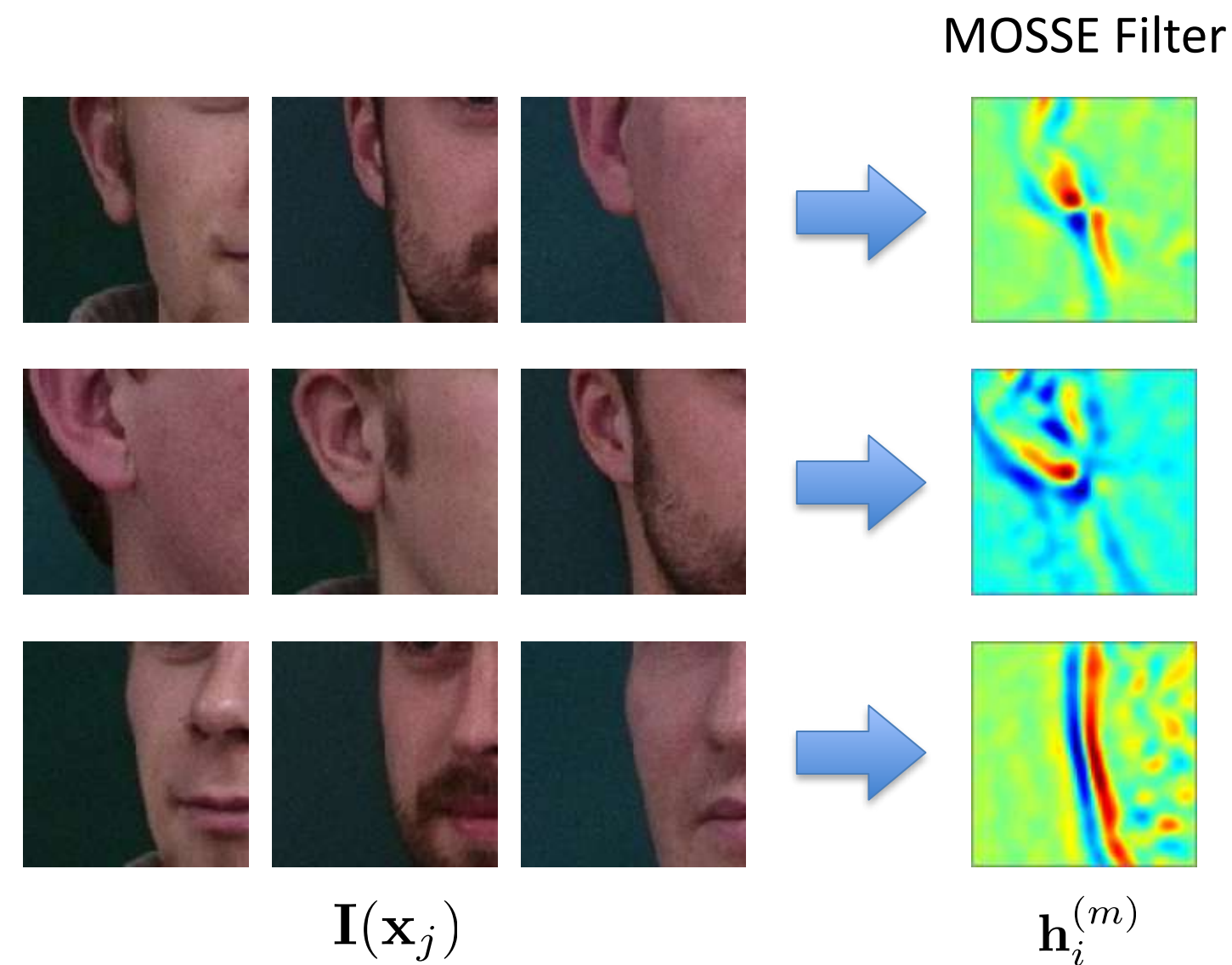


# Multiple Detectors per Landmark

Training examples for a given landmark:



Clustering of training examples

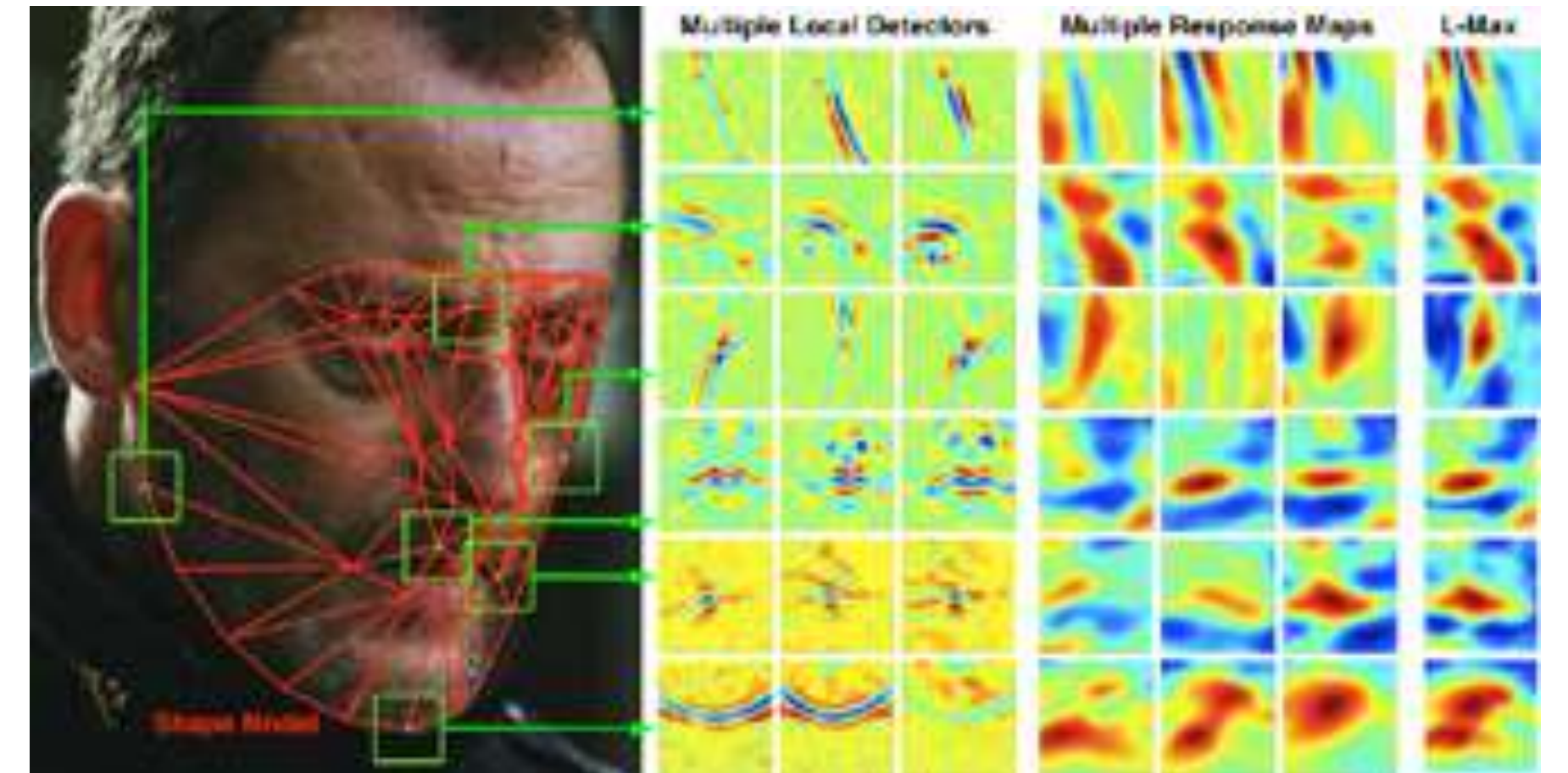


Unsupervised Clustering

$$\arg \max_{\mathbf{h}_i^{(m)}} \sum_{j=1}^N \sum_{m=1}^M \mathbf{I}(\mathbf{x}_j) * \mathbf{h}_i^{(m)}$$

M - clusters  
N - examples

- Solve (for each landmark  $i$ ) using a two step approach:
- Initial clustering by k-means
  - ① Build basic detectors using the current clustering estimate
  - ② Move samples to the cluster with highest correlation
  - Repeat until no more samples change



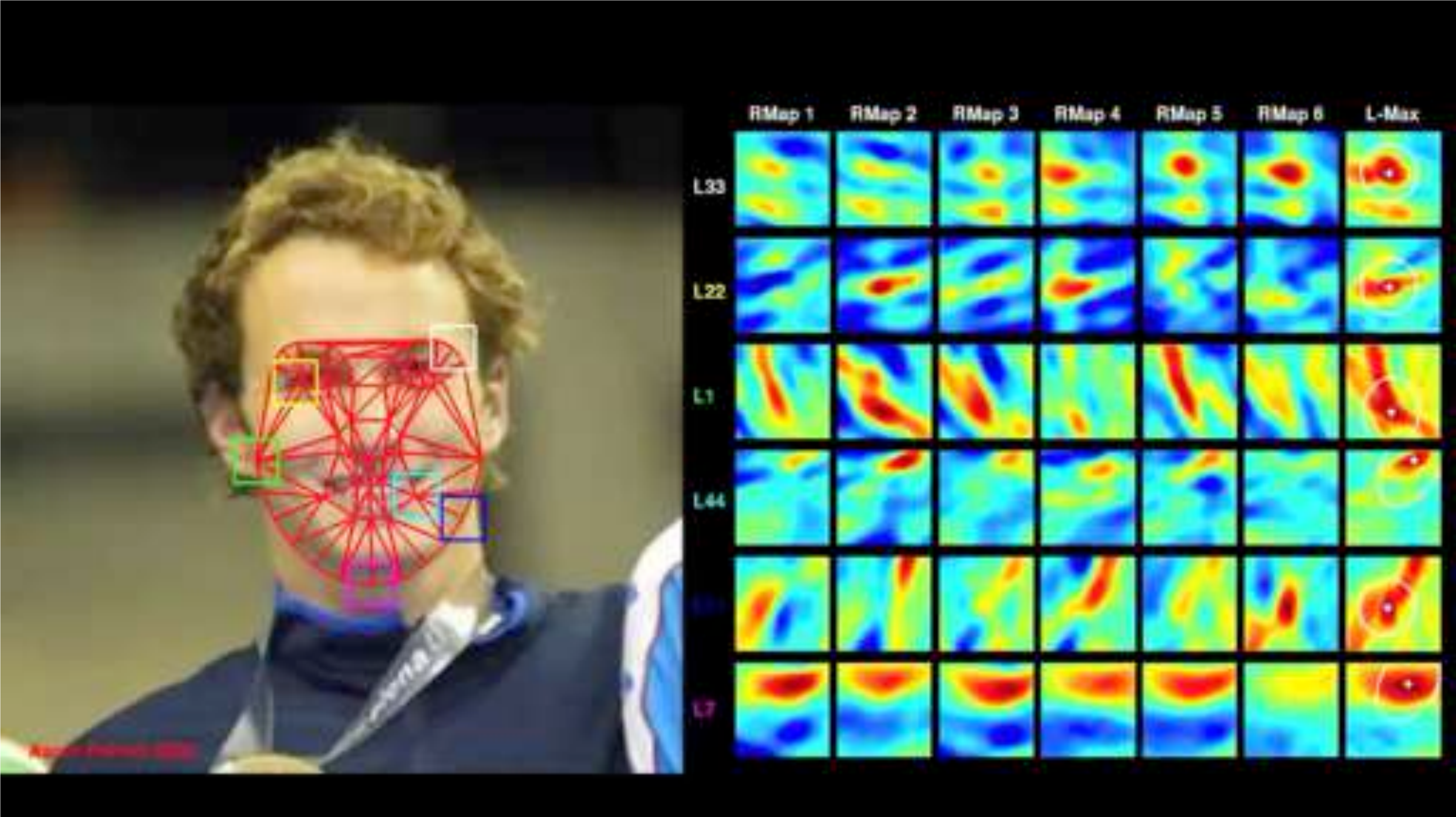
Multiple Response Maps

$$p_i(\mathbf{z}_i)^{(m)} = \frac{1}{1 + e^{-a_i \beta_1 \mathcal{D}_i(\mathbf{I}(\mathbf{z}_i)) + \beta_0}}$$

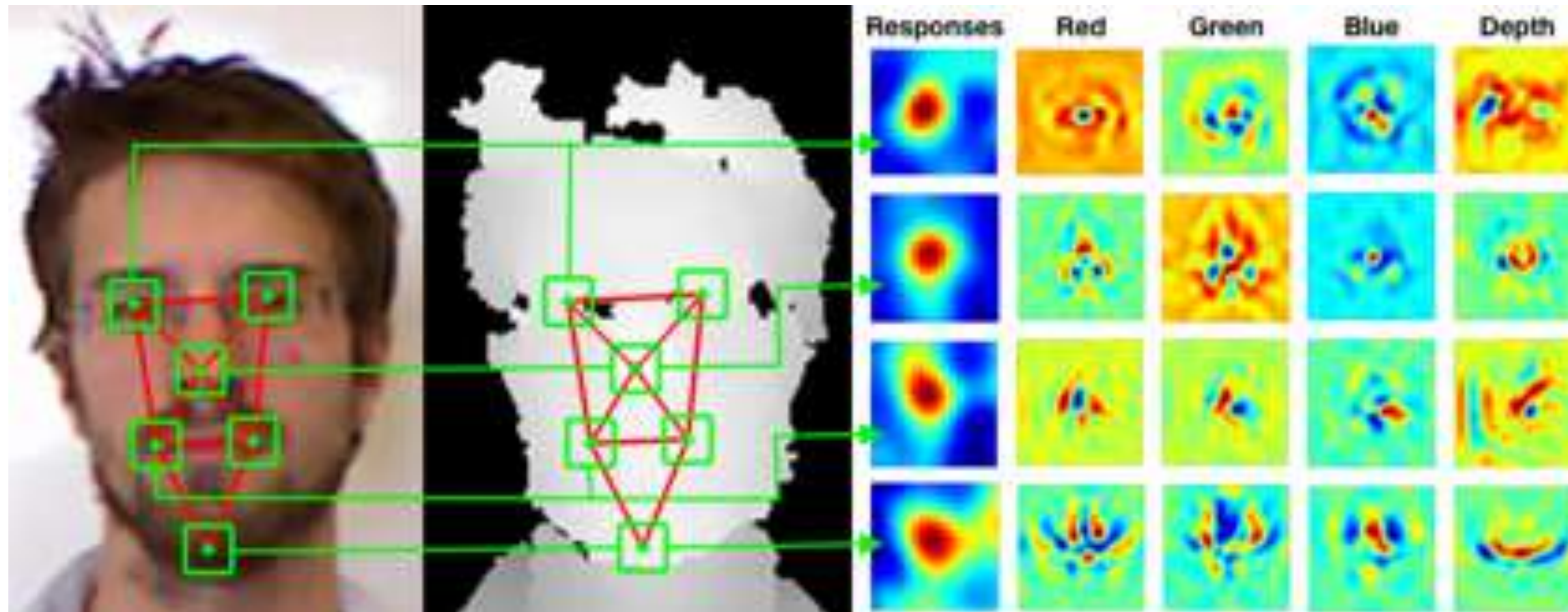
Combining Multiple Detections

$$p_i(\mathbf{z}_i)_\infty = \max_{\mathbf{z}_i} \{p_i(\mathbf{z}_i)^{(1)}, \dots, p_i(\mathbf{z}_i)^{(M)}\}$$

# Multiple Detectors por Landmark (video)

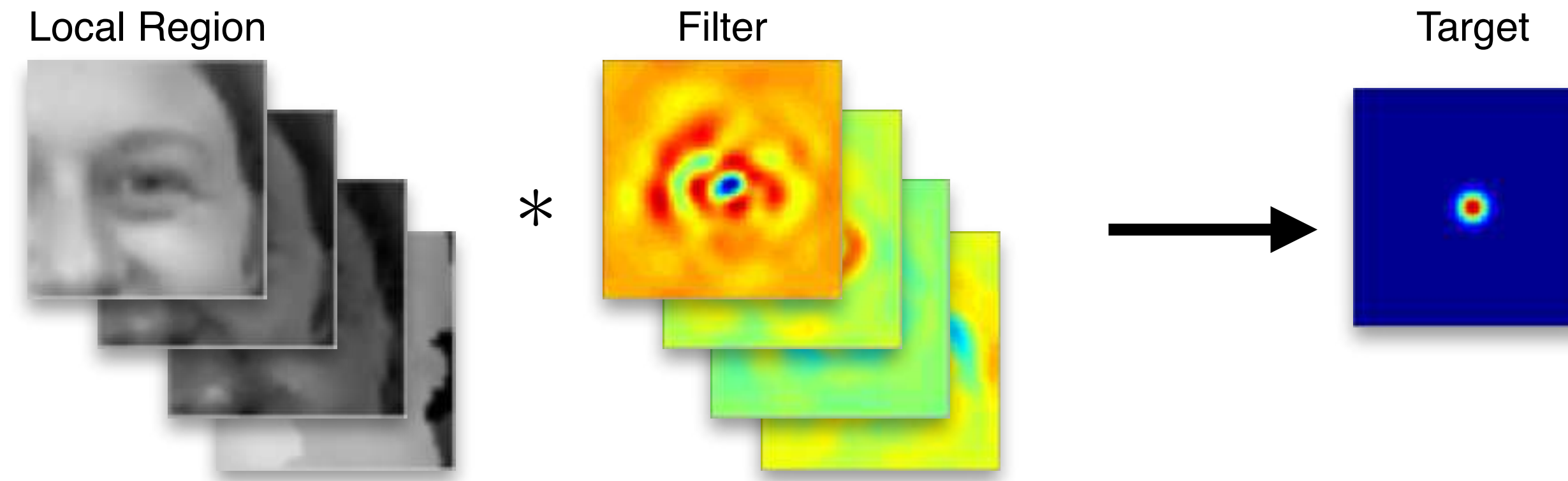


# CLM with Depth Data



- Strategy Employed:
  - Multiple Channel Local Detectors (RGBD - w/ single response map)
  - Fast CLM Inference (Gaussian)

# Multiple Channel Correlation Filters



**Spatial Domain**

$$\arg \min_{\mathbf{h}_i^{(1)}, \dots, \mathbf{h}_i^{(D)}} \sum_{j=1}^N \sum_{k=1}^D \left( \mathbf{h}_i^{(k)} * \mathbf{I}_j^{(k)} - \mathbf{g}_j \right)^2 + \lambda \sum_{k=1}^D \|\mathbf{h}_i^{(k)}\|^2$$

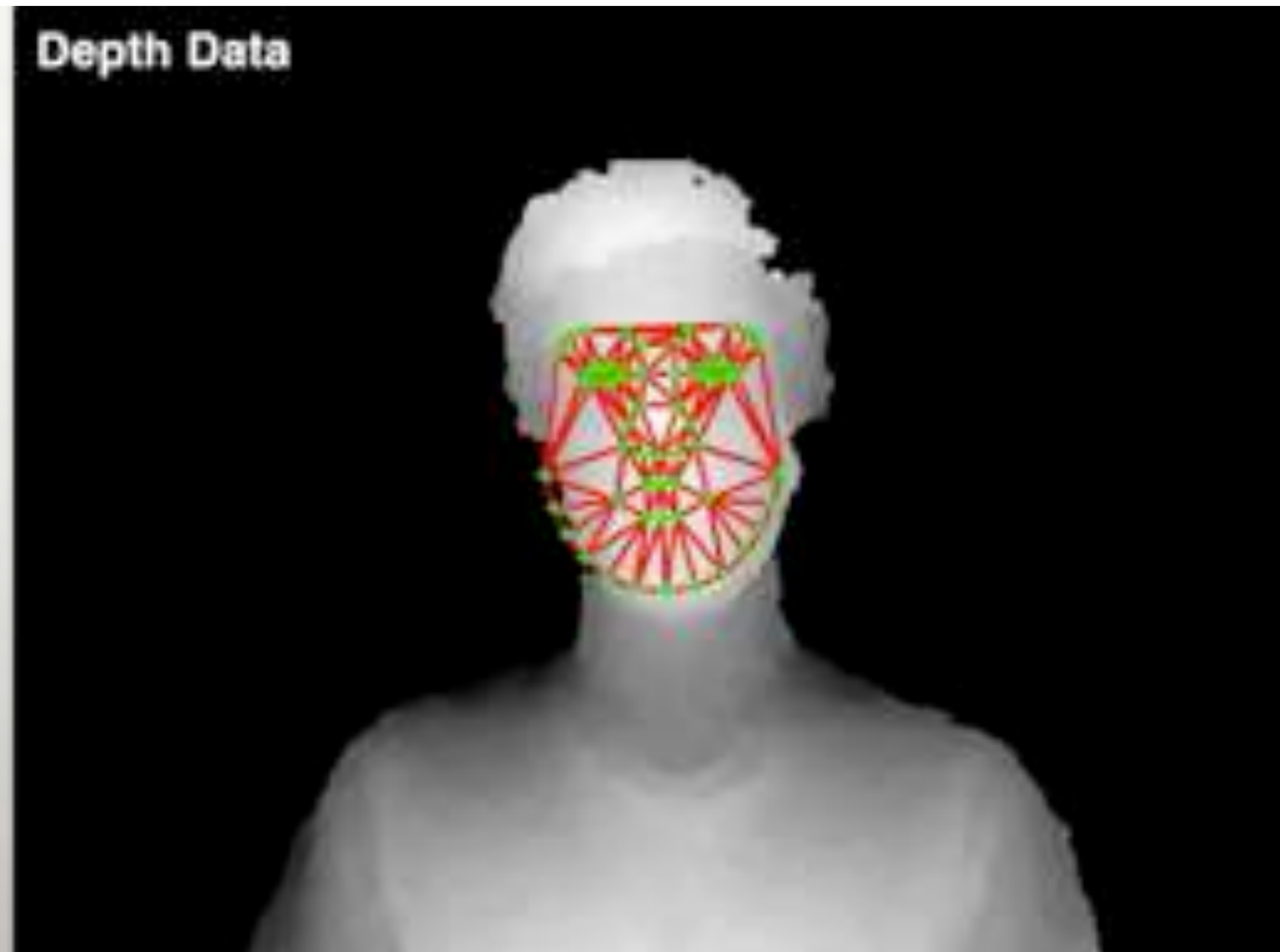
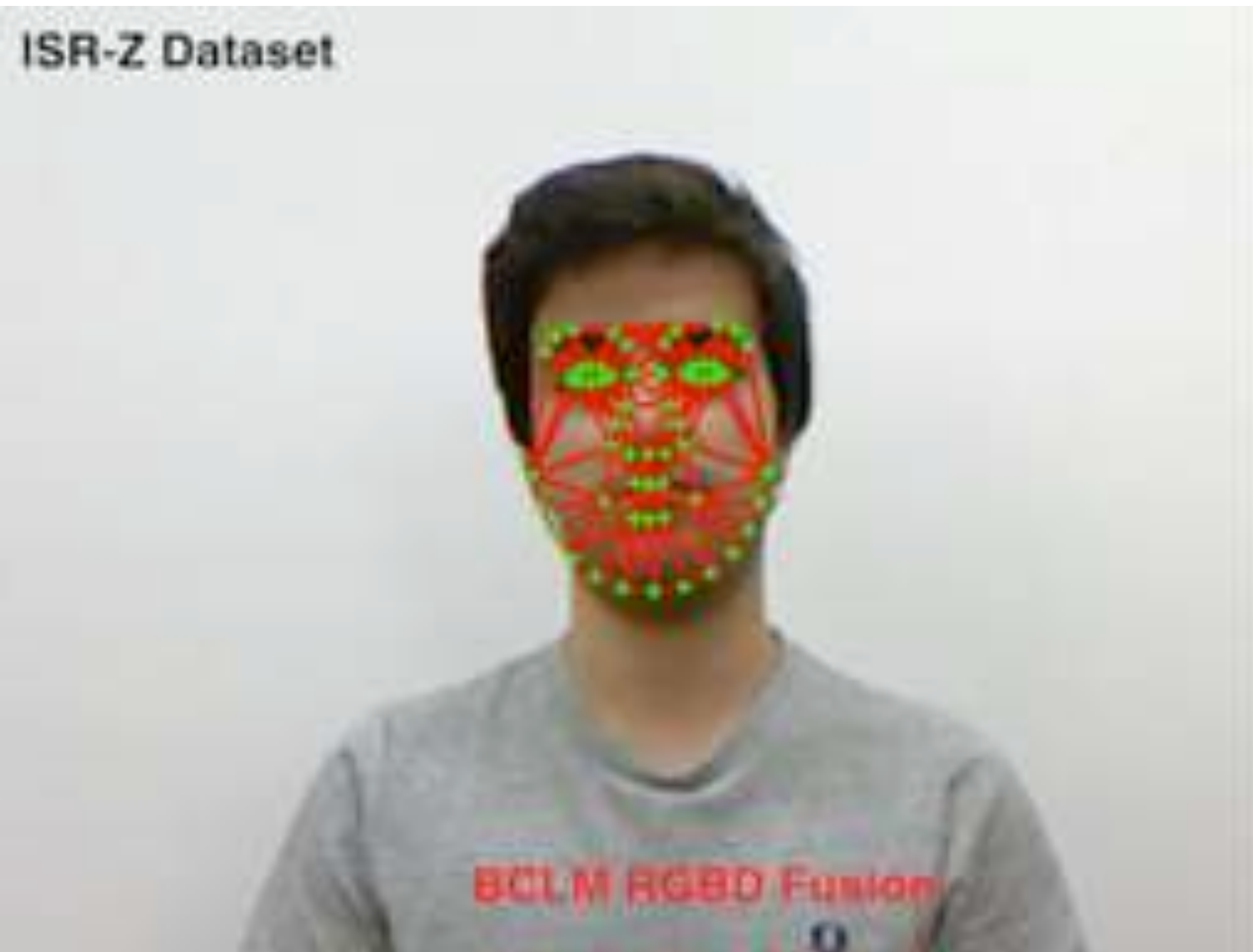
$$\arg \min_{\mathbf{h}_i^{(\dots)}} \sum_{j=1}^N \sum_{k=1}^D \left( \mathbf{h}^{(k)} * \text{Example} - \text{Gaussian} \right)^2 + \lambda \sum_{k=1}^D \|\mathbf{h}^{(k)}\|^2$$

The diagram shows a stack of brown boxes labeled  $\mathbf{h}^{(k)}$  being convolved with an 'Example' image to produce a 'Gaussian' target heatmap. The equation above shows the minimization of the squared difference between the convolution result and the Gaussian target, plus a regularization term.

Minimization across all channels

# BCLM w/ Depth Data

---

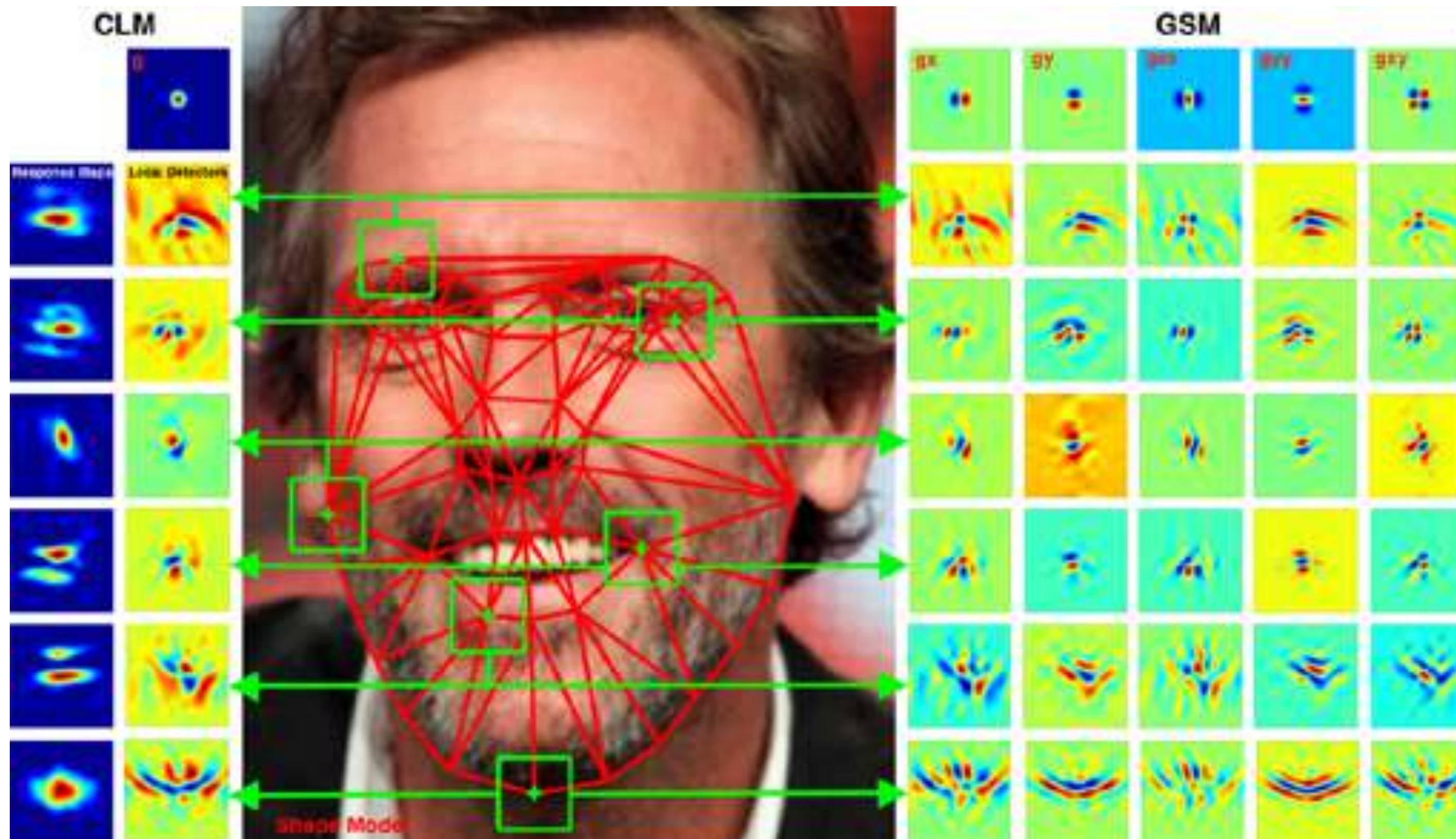


# Gradient Shape Model (GSM)

$\mathbf{s}$  - shape vector at image frame

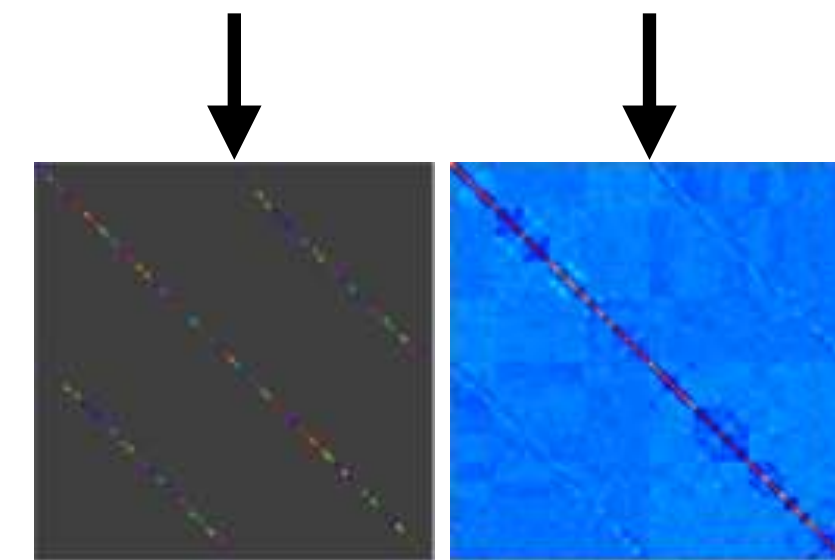
$$\arg \min_{\mathbf{s}, \boldsymbol{\theta}} - \sum_{i=1}^v \underset{\text{Data Term}}{D_i(\mathbf{I}(\mathbf{s}_i), \boldsymbol{\theta})} + \lambda_1 \underset{\text{Regularization Term}}{(\mathcal{S}(\mathbf{s}, \boldsymbol{\theta}) - \mathbf{s}_0)^T \Sigma_{\mathbf{s}}^{-1} (\mathcal{S}(\mathbf{s}, \boldsymbol{\theta}) - \mathbf{s}_0)}$$

Similarity Transform
Similarity Transform



$$\nabla_f(\mathbf{s}, \boldsymbol{\theta}) = \nabla_D(\mathbf{s}) + \lambda_1 \nabla_R(\mathbf{s}, \boldsymbol{\theta})$$

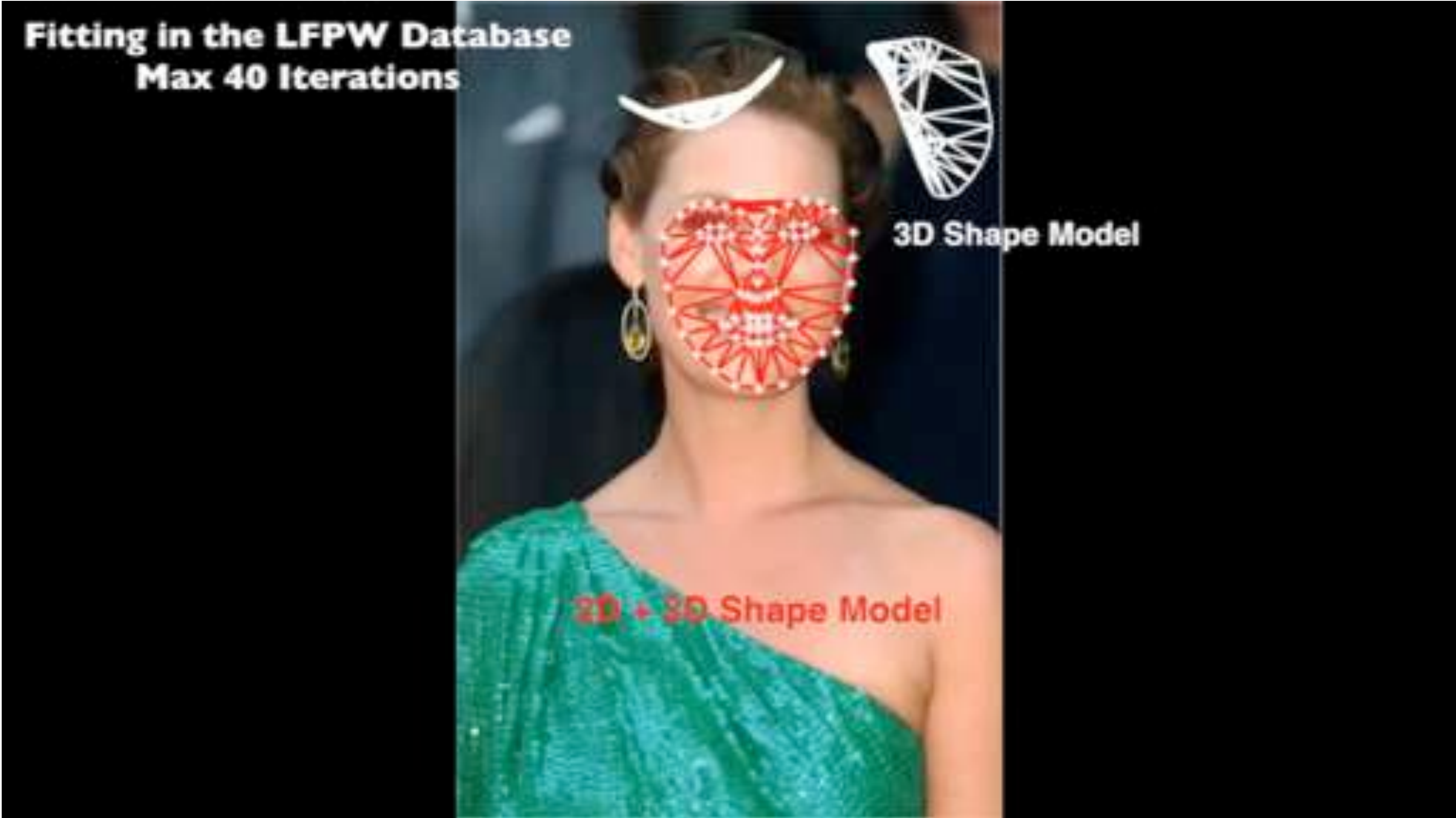
$$\mathbf{H}_f(\mathbf{s}, \boldsymbol{\theta}) = \mathbf{H}_D(\mathbf{s}) + \lambda_1 \mathbf{H}_R(\mathbf{s}, \boldsymbol{\theta})$$



$$\nabla_D(\mathbf{s}) = \left[ \mathcal{I}_1^T \frac{\partial \mathbf{h}_1}{\partial x_1} \quad \dots \quad \mathcal{I}_v^T \frac{\partial \mathbf{h}_v}{\partial x_v} \quad \mathcal{I}_1^T \frac{\partial \mathbf{h}_1}{\partial y_1} \quad \dots \quad \mathcal{I}_v^T \frac{\partial \mathbf{h}_v}{\partial y_v} \quad \mathbf{0}_4 \right]^T$$

# 2D + 3D Gradient Shape Model (GSM)

$$\arg \min_{\mathbf{s}, \boldsymbol{\theta}, \bar{\mathbf{s}}, \mathbf{P}} - \sum_{i=1}^v \overset{\text{Data Term}}{D_i(\mathbf{I}(\mathbf{s}_i), \boldsymbol{\theta})} + \lambda_1 \underset{\text{Similarity Transform}}{(\mathcal{S}(\mathbf{s}, \boldsymbol{\theta}) - \mathbf{s}_0)^T \Sigma_{\mathbf{s}}^{-1} (\mathcal{S}(\mathbf{s}, \boldsymbol{\theta}) - \mathbf{s}_0)} + \lambda_2 \underset{\text{Similarity Transform}}{(\bar{\mathbf{s}} - \bar{\mathbf{s}}_0)^T \Sigma_{\bar{\mathbf{s}}}^{-1} (\bar{\mathbf{s}} - \bar{\mathbf{s}}_0)} + \lambda_3 \|\mathbf{r}\|^2$$



↓

**Scaled Orthographic Projection**

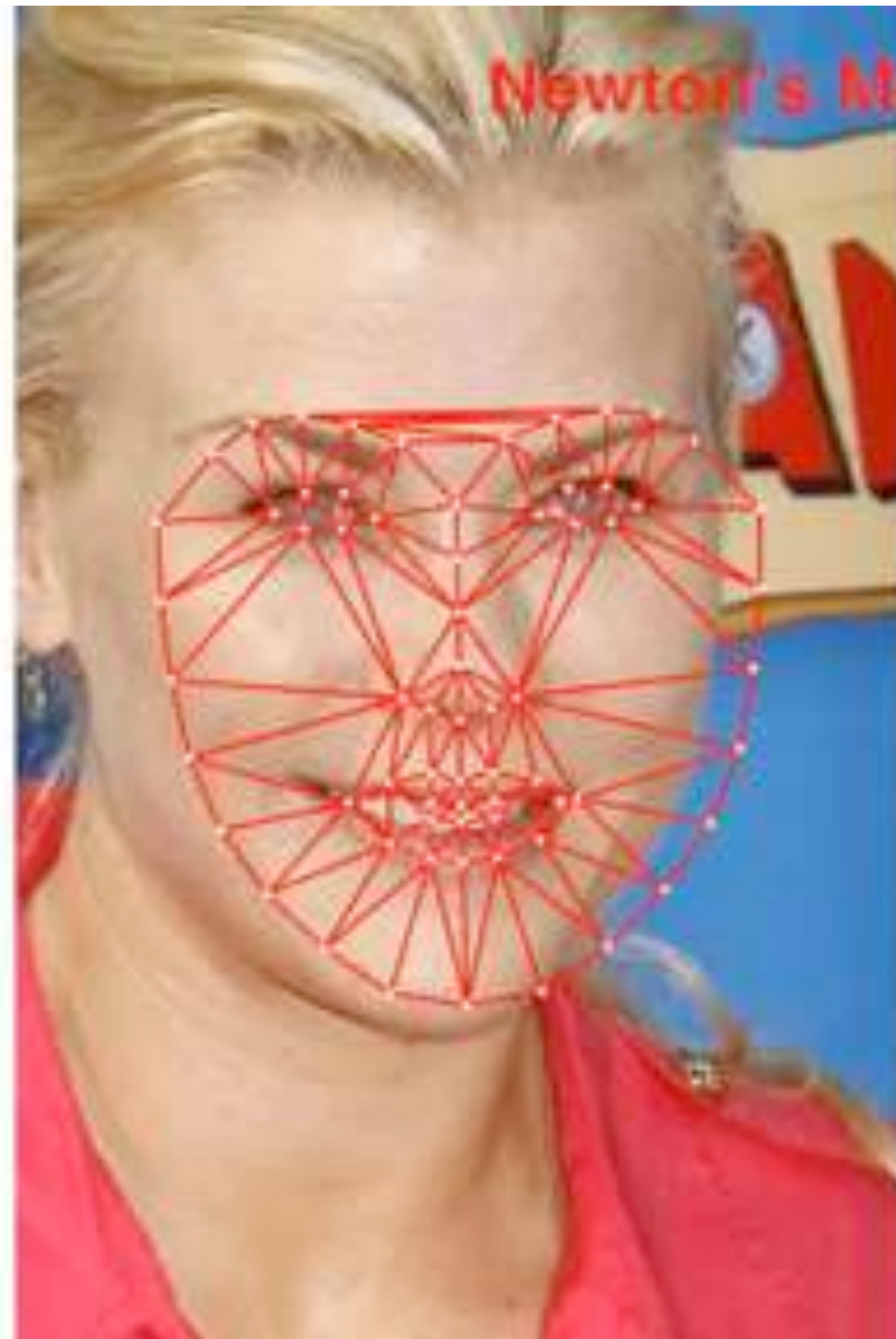
$$\mathbf{r} = \mathbf{s} - \sigma \underbrace{\begin{pmatrix} i_x & i_y & i_z \\ j_x & j_y & j_z \end{pmatrix}}_{\mathbf{R}} \otimes \mathbf{I}_v \bar{\mathbf{s}} - \begin{pmatrix} o_x \\ o_y \end{pmatrix} \otimes \mathbf{1}_v$$



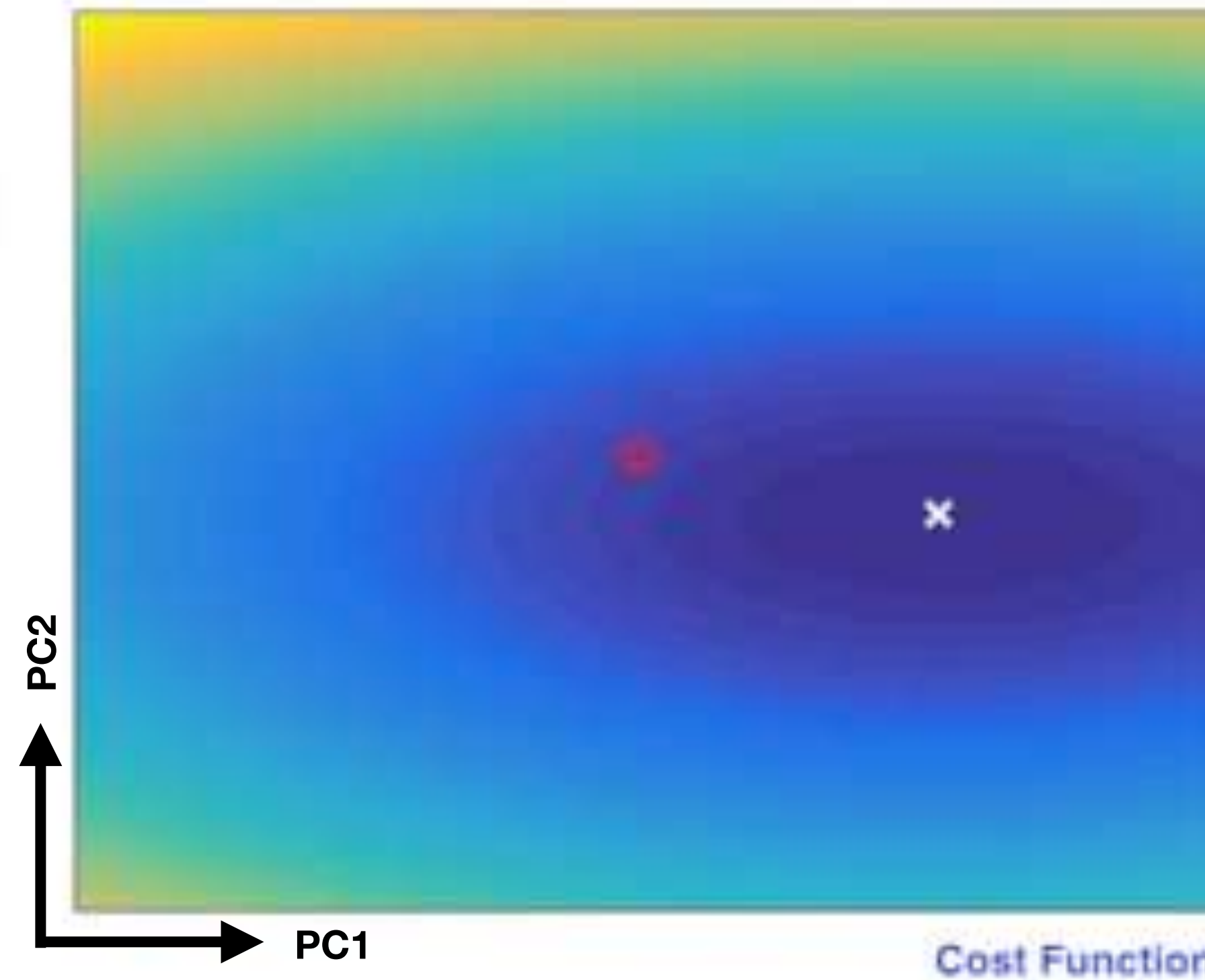
# Gradient Descent vs. Cascaded Regression

## Gradient Descent

- Requires 'good' initialization.
- In general, requires to compute the Jacobian at each iteration.
- Require to compute the Hessian and its inverse (2nd order methods).
- Learning Fast.
- Testing Slow.



Newton's Method Optimization



## Cascaded Regression

- Captures the variance of the initialization.
- Precomputed Regression matrix.
- Learning Slow.
- Testing Fast.

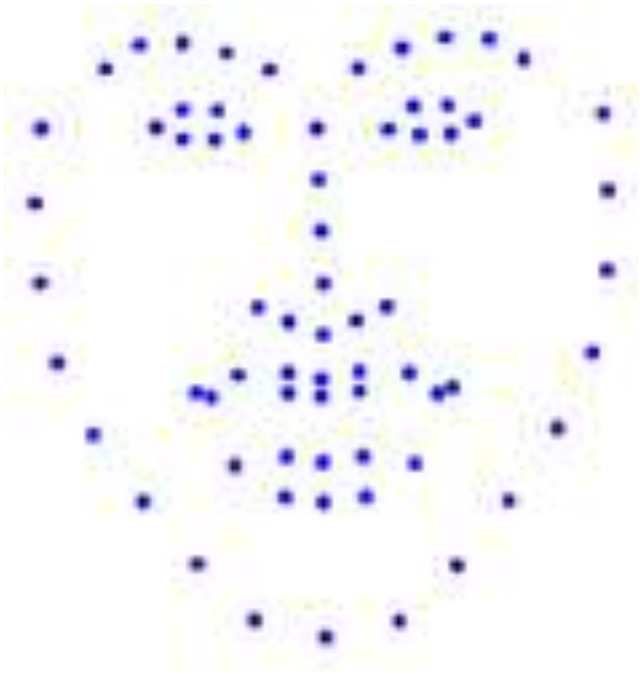
# Cascade Regression Framework



$$\mathbf{s}^k = \mathbf{s}^{k-1} + \mathbf{R}^{k-1} \mathcal{F}(\mathbf{I}, \mathbf{s}^{k-1})$$

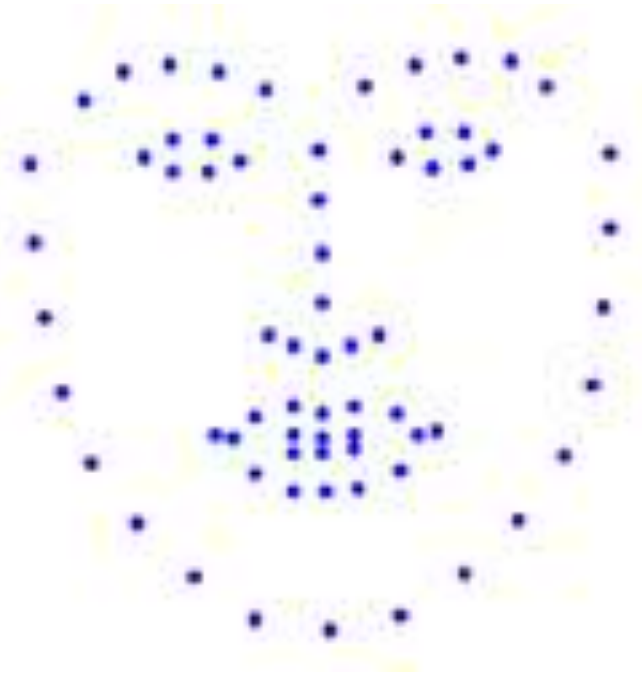
$k$  - cascade level

Updated shape vector



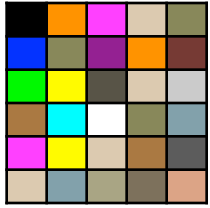
$2v \times 1$

Previous shape vector



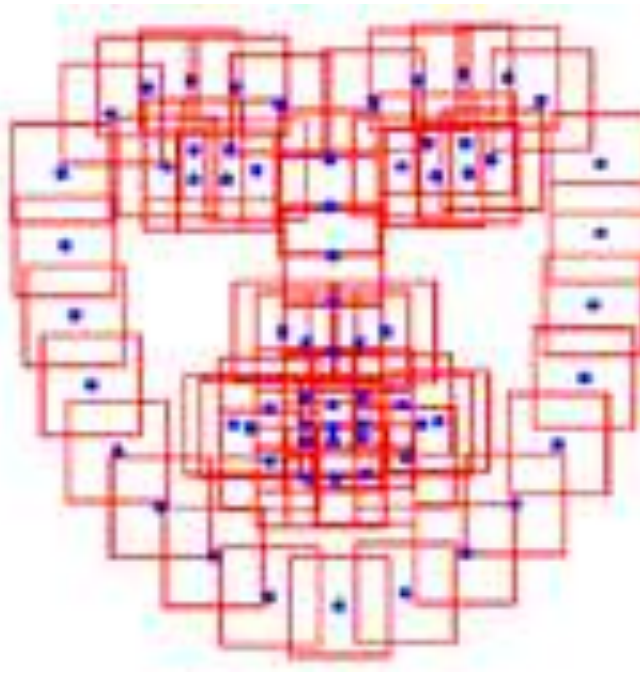
$2v \times 1$

Regression Matrix



$2v \times d$

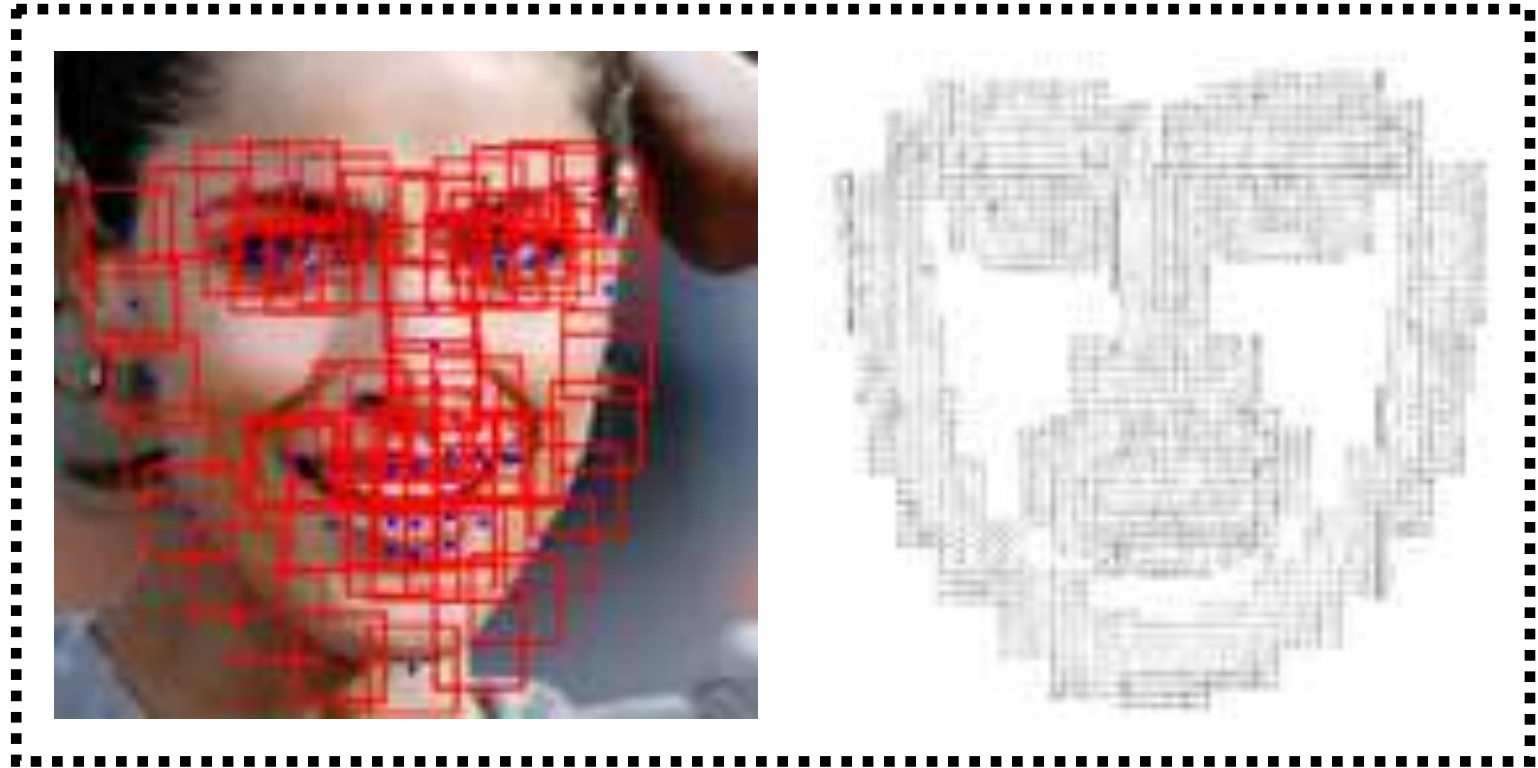
Feature Extraction



$d \times 1$

$$\mathbf{s} = \begin{pmatrix} x_0 \\ \vdots \\ x_v \\ y_0 \\ \vdots \\ y_v \end{pmatrix}$$

$v$  - landmarks

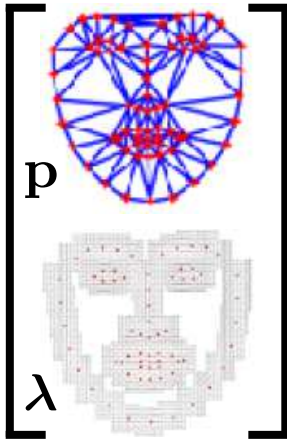


RGB

HoG

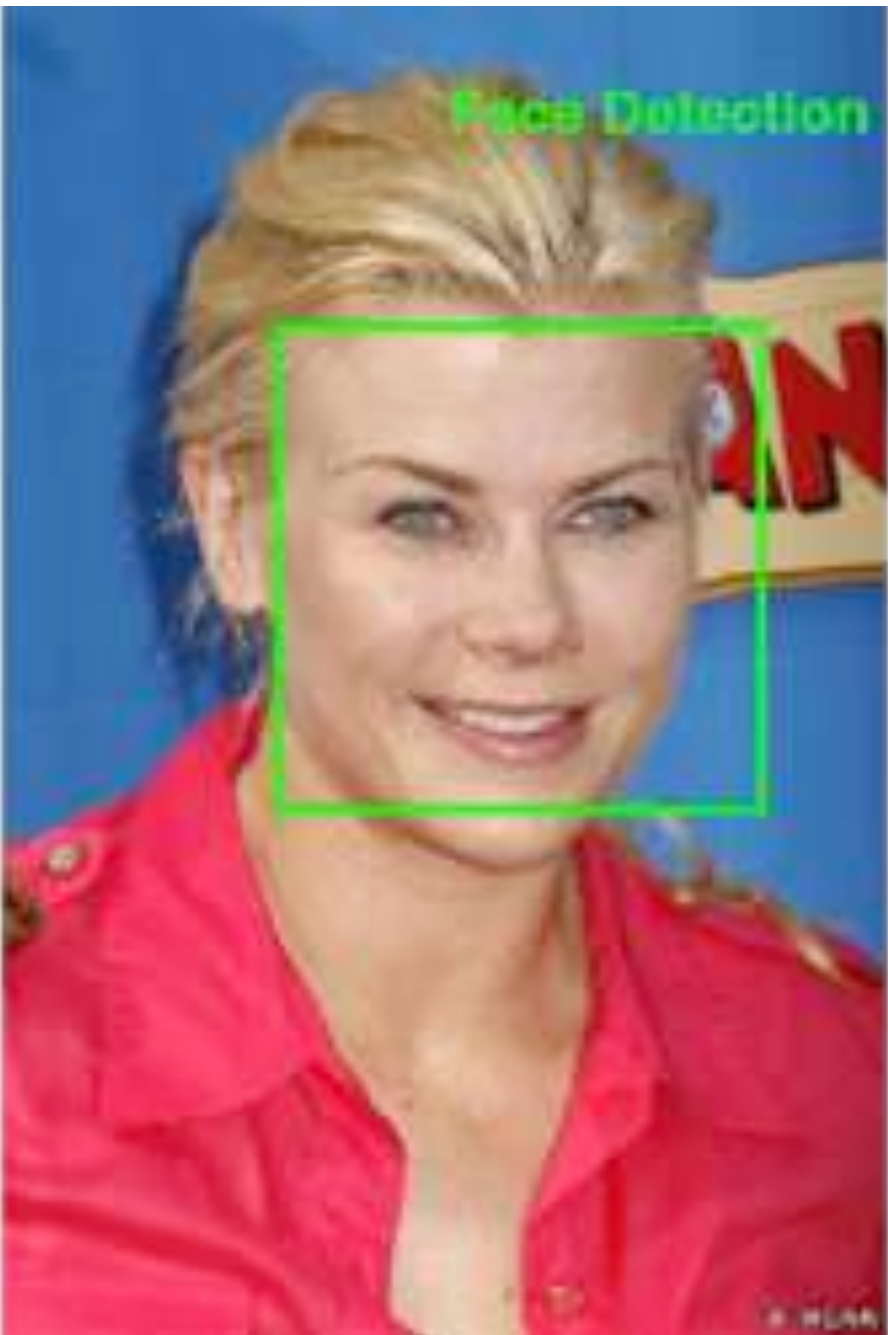
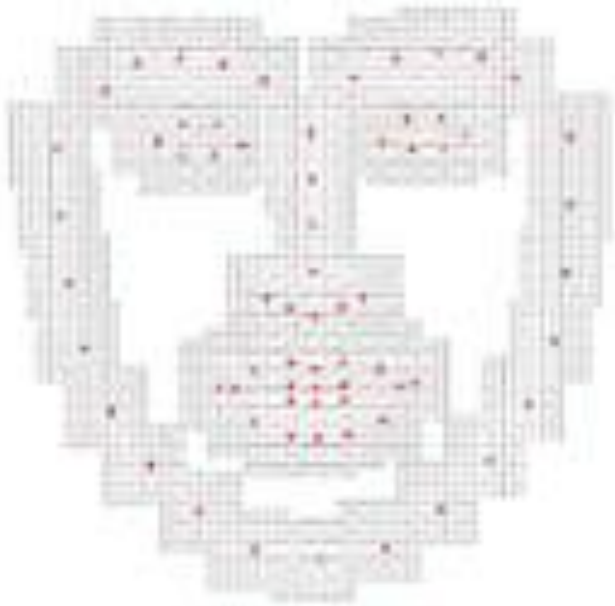
# Simultaneous Cascaded Regression (SCR)

Regression with both shape and appearance structure

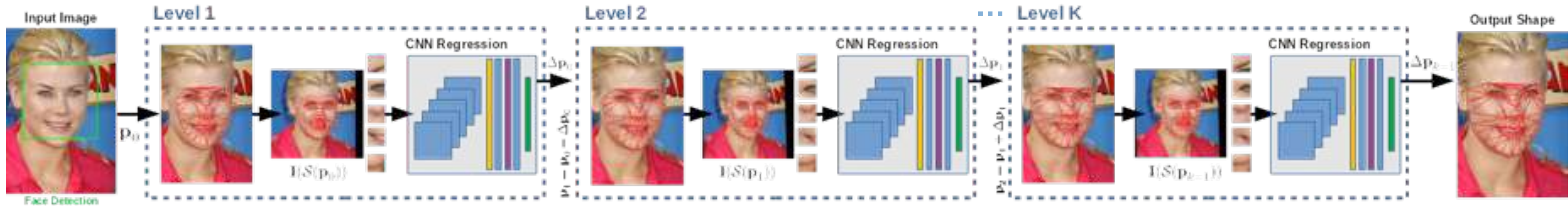


$$\begin{bmatrix} \mathbf{p} \\ \lambda \end{bmatrix}^k = \begin{bmatrix} \mathbf{p} \\ \lambda \end{bmatrix}^{k-1} + \mathbf{R}^{k-1} \left( \mathbf{I}(\mathcal{W}(\mathbf{p}^{k-1})) - \mathbf{A}_0 - \mathbf{A}\lambda^{k-1} \right), \quad k = 1, \dots, K$$

Shape + Appearance parameters
Features extracted at previous level
Features generated by the Model



# Nonlinear Cascade Regression



Combined shape + pose parameters

$$\mathbf{p} = \begin{bmatrix} \mathbf{b} \\ \mathbf{q} \end{bmatrix} \in \mathbb{R}^{n+4}$$

$$\mathbf{p}^k = \mathbf{p}^{k-1} + \gamma \mathcal{R}^{k-1} \{ \mathcal{L}(\mathbf{I}(\mathcal{S}(\mathbf{p}^{k-1}))) \}$$

$k$  - cascade level

Updated shape instance



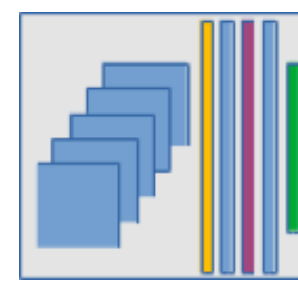
$$(n+4) \times 1$$

Previous shape instance



$$(n+4) \times 1$$

Nonlinear Mapping



$\text{CNN}^k$

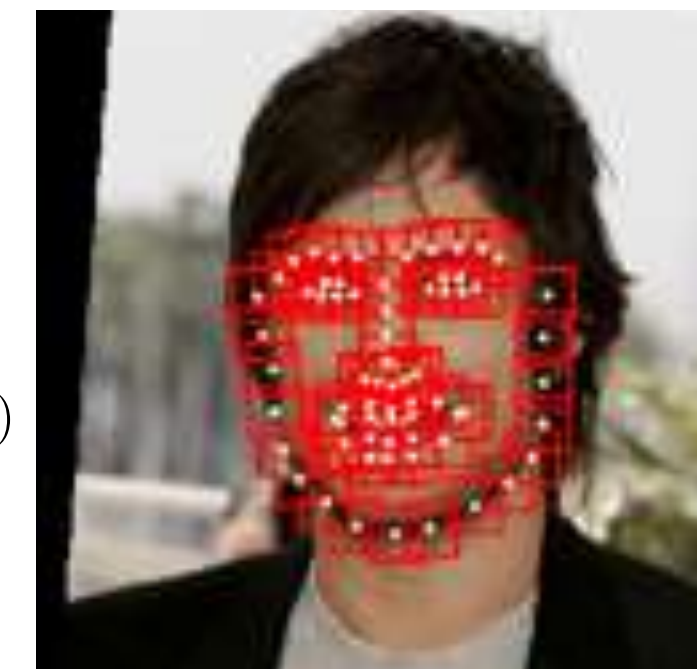
Local Feature Extraction at Normalized Frame



$\mathbf{I}(\cdot)$

Similarity Warp

$$\mathbf{p}(n+1 : n+4)$$



$\mathbf{I}(\mathcal{S}(\mathbf{p}))$

Sampled 3D Array

$$P \times P \times v$$



$\mathcal{L}(\mathbf{I}(\mathcal{S}(\mathbf{p})))$

# CNN Regression Architecture

## Nonlinear Regression

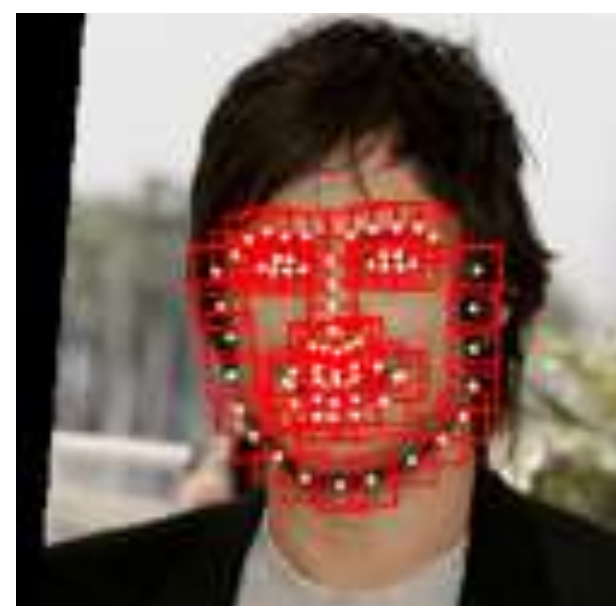
$$\arg \min_{\mathcal{R}^k} \sum_{i=1}^N \sum_{j=1}^M \|\Delta \mathbf{p}_{ij}^k - r_L(\dots r_1(\mathcal{L}(\mathbf{I}_i(\mathcal{S}(\mathbf{p}_j^k))))\|_{\Sigma^k}^2$$

↓ CNN Topology

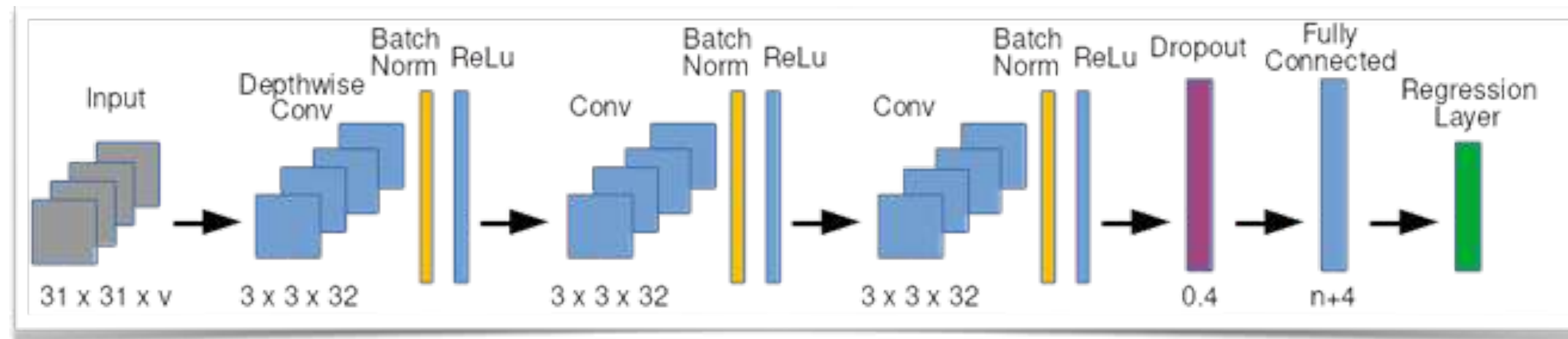
Input



$\mathcal{L}(\mathbf{I}(\mathcal{S}(\mathbf{p})))$



Pose Normalized Image



**Depthwise Convolution**  
32 filters (3x3) for each local patch

**Convolution**  
32 filters (3x3)

**Convolution**  
32 filters (3x3)

**Dropout**  
0.4

**Regression Layer**  
(n+4)

Output

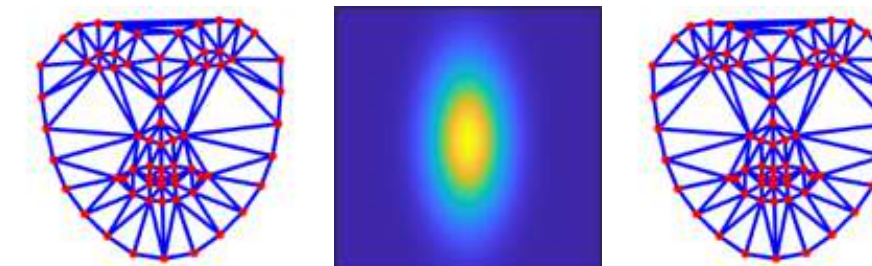


shape parameters update  
 $\Delta \mathbf{p}$

## Loss function

$$L_r = \frac{1}{N} \sum_{j=1}^N \Delta \mathbf{p}_j^T \Sigma_{\mathbf{p}}^{-1} \Delta \mathbf{p}_j$$

Mahalanobis Distance



# CNN Learning - Data Collection

$$\arg \min_{\mathcal{R}^k} \sum_{i=1}^N \sum_{j=1}^M \|\Delta \mathbf{p}_{ij}^k - \text{CNN}^k(\mathcal{L}(\mathbf{I}_i(\mathcal{S}(\mathbf{p}_j^k))))\|_{\Sigma^k}^2$$

*k* - cascade level  
*i* - training image  
*j* - virtual sample

Estimate noise

$$\Sigma^k = \text{cov}(\mathbf{p}_* - \mathbf{p}_{ij})$$

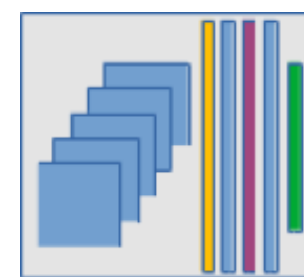
Deviation from Ground Truth

$$\Delta \mathbf{p}_{ij} = \mathbf{p}_* - \mathbf{p}_{ij}$$

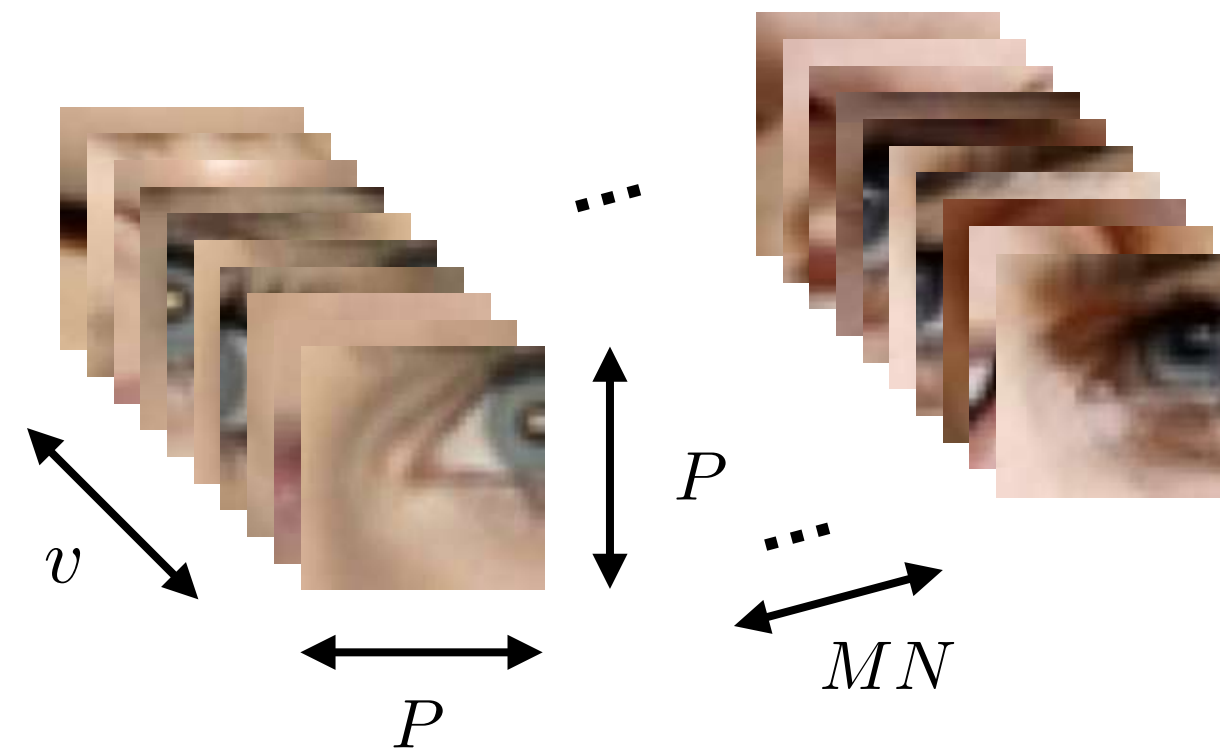
Data Matrix (local normalized patches)

$$\mathbf{D}_{ij} = \mathcal{L}(\mathbf{I}_i(\mathcal{S}(\mathbf{p}_j)))$$

Regression Labels

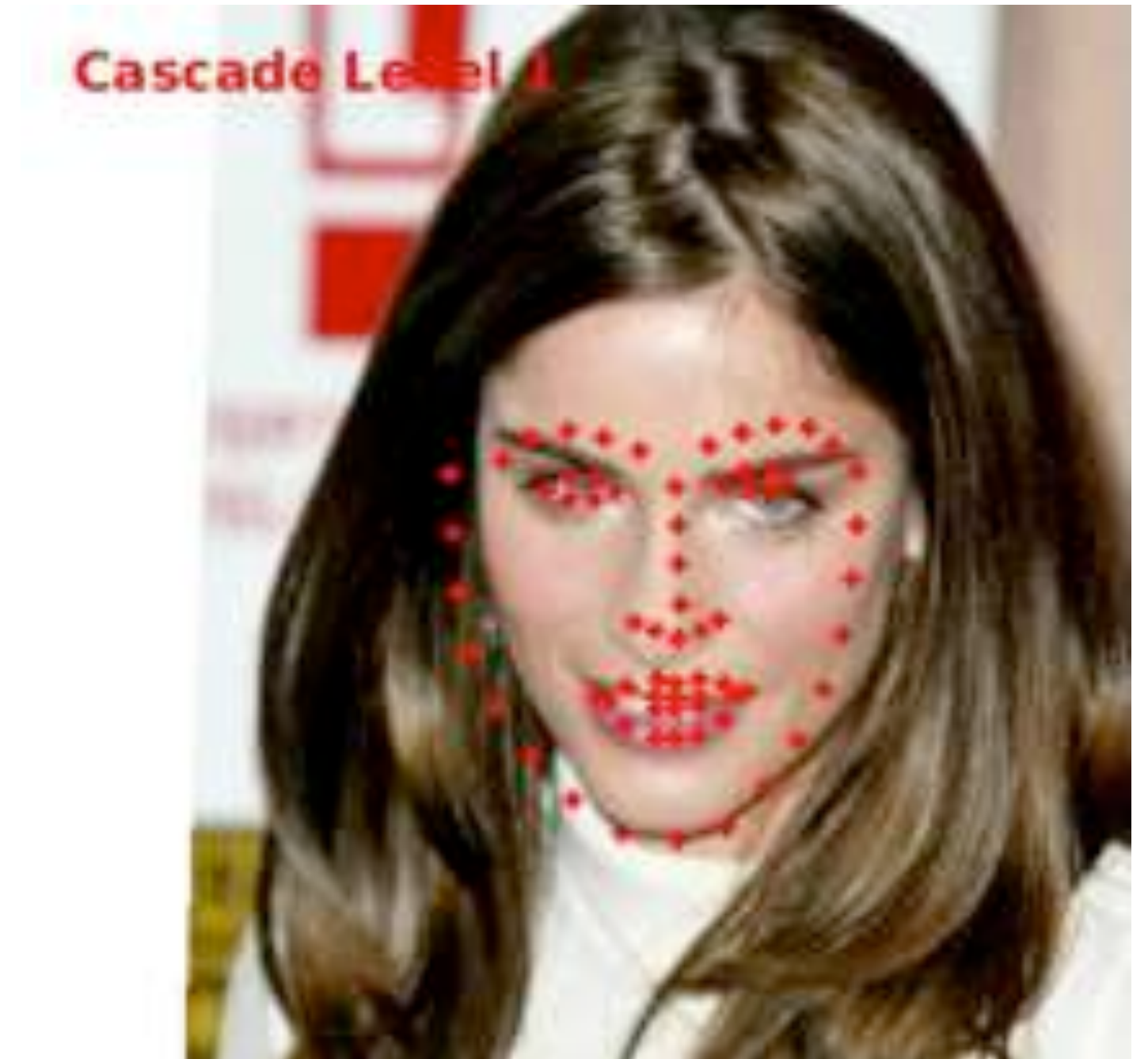


CNN<sup>k</sup>



M - augmented examples  
 N - real examples

Data Matrix: 4D Array  
 (P x P x v x N.M)

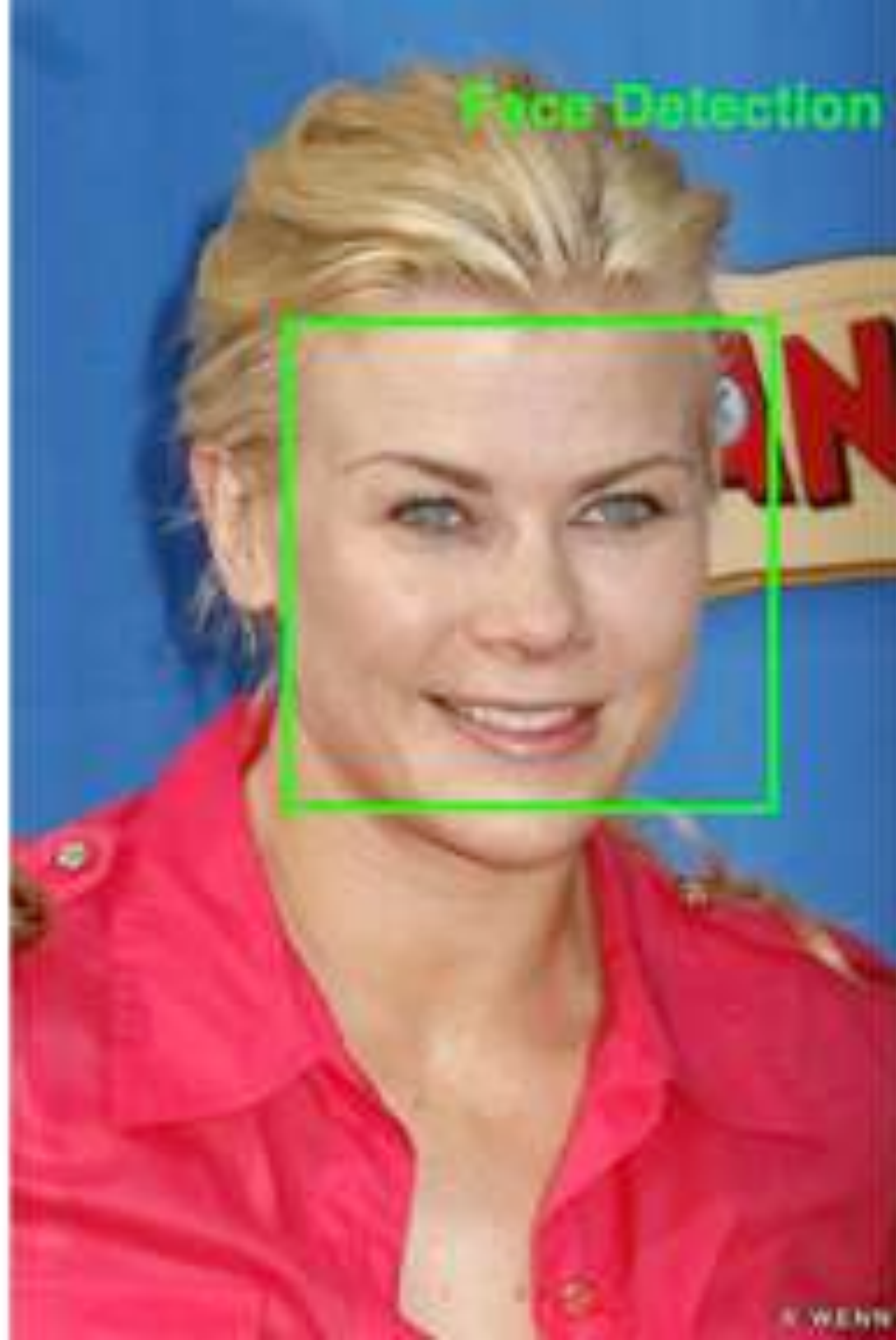


Data Collection (D matrix)

$$\mathbf{p}_{ij} \sim \mathcal{N}(\mathbf{p}_i, \Sigma^k)$$

↑  
 virtual shape sample

Face Detection

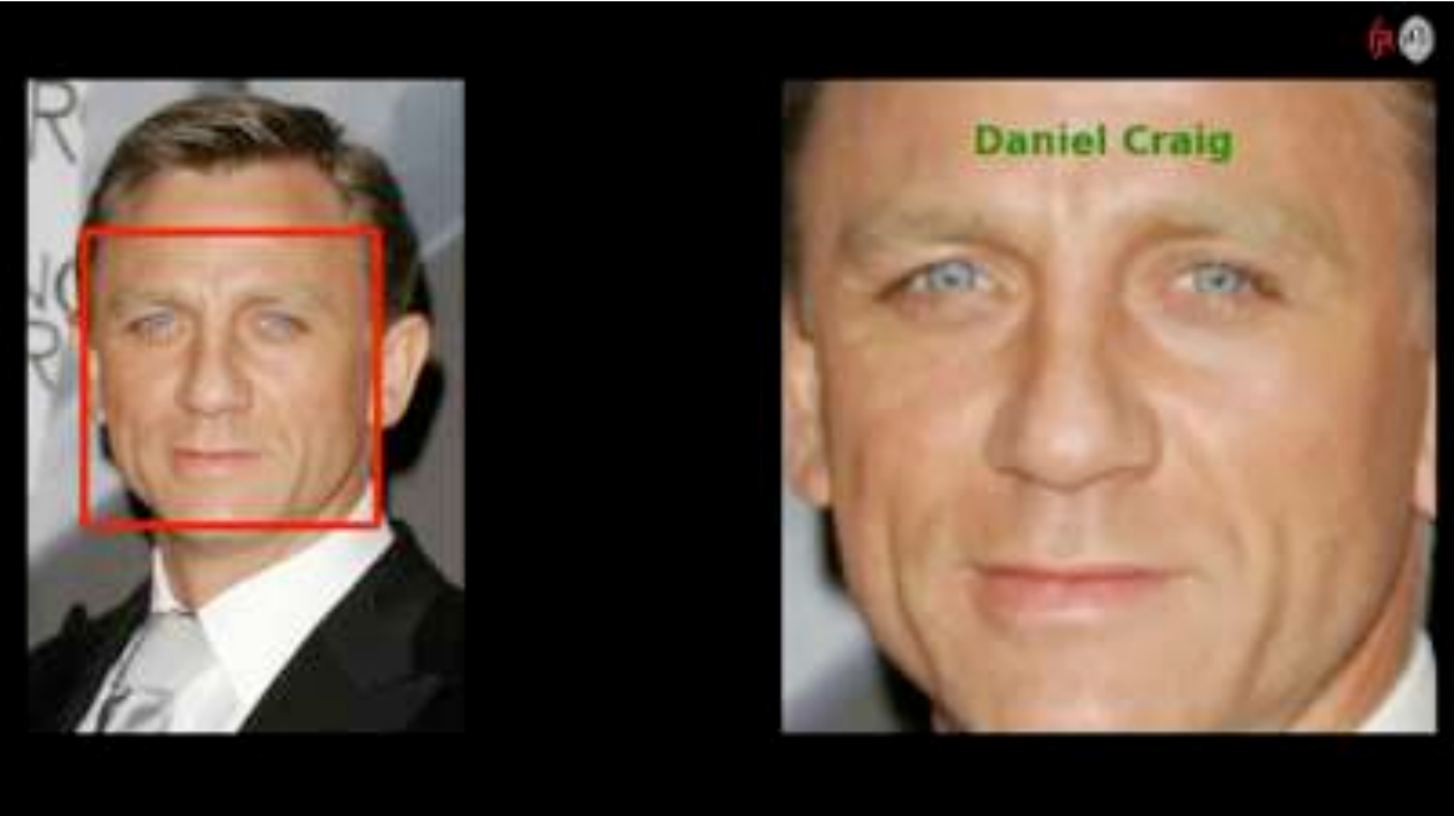
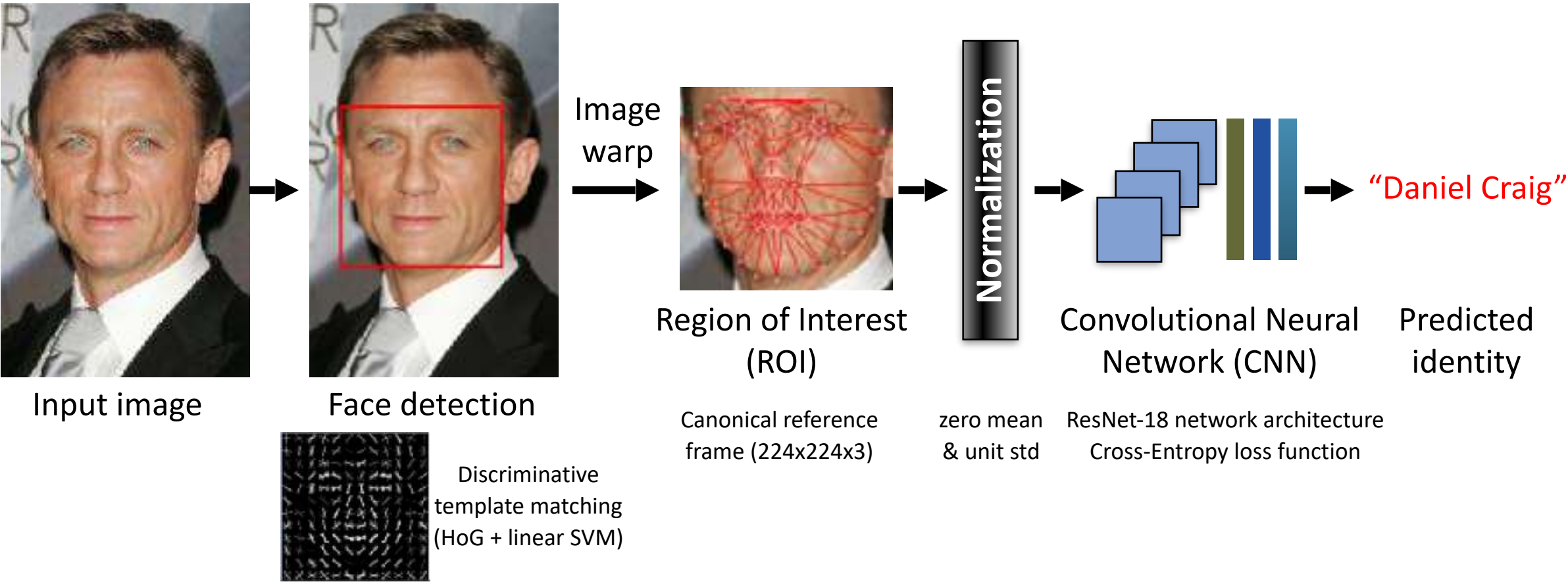


# Demo Applications

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# Face Recognition

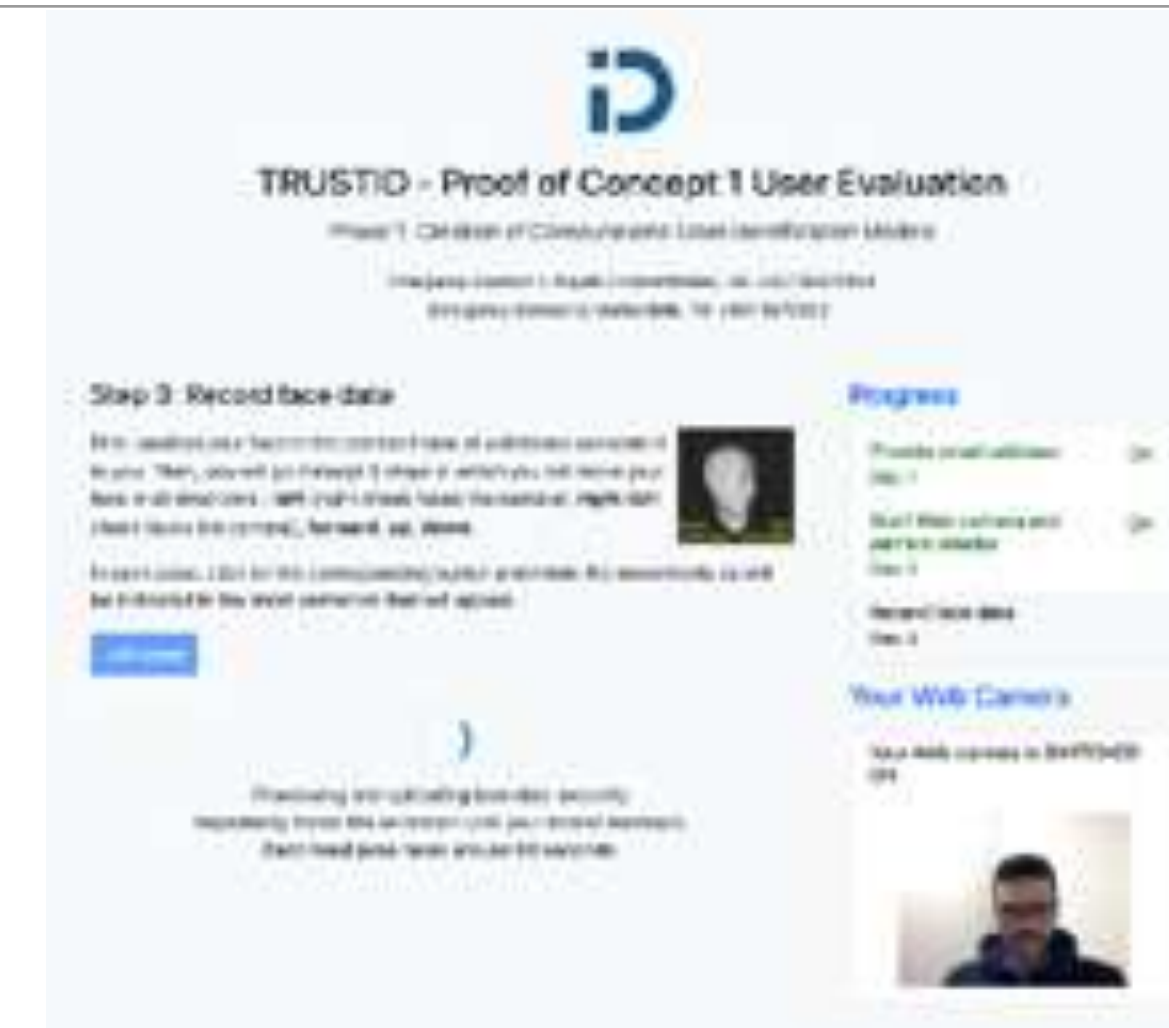


Basic Face Recognition Demo

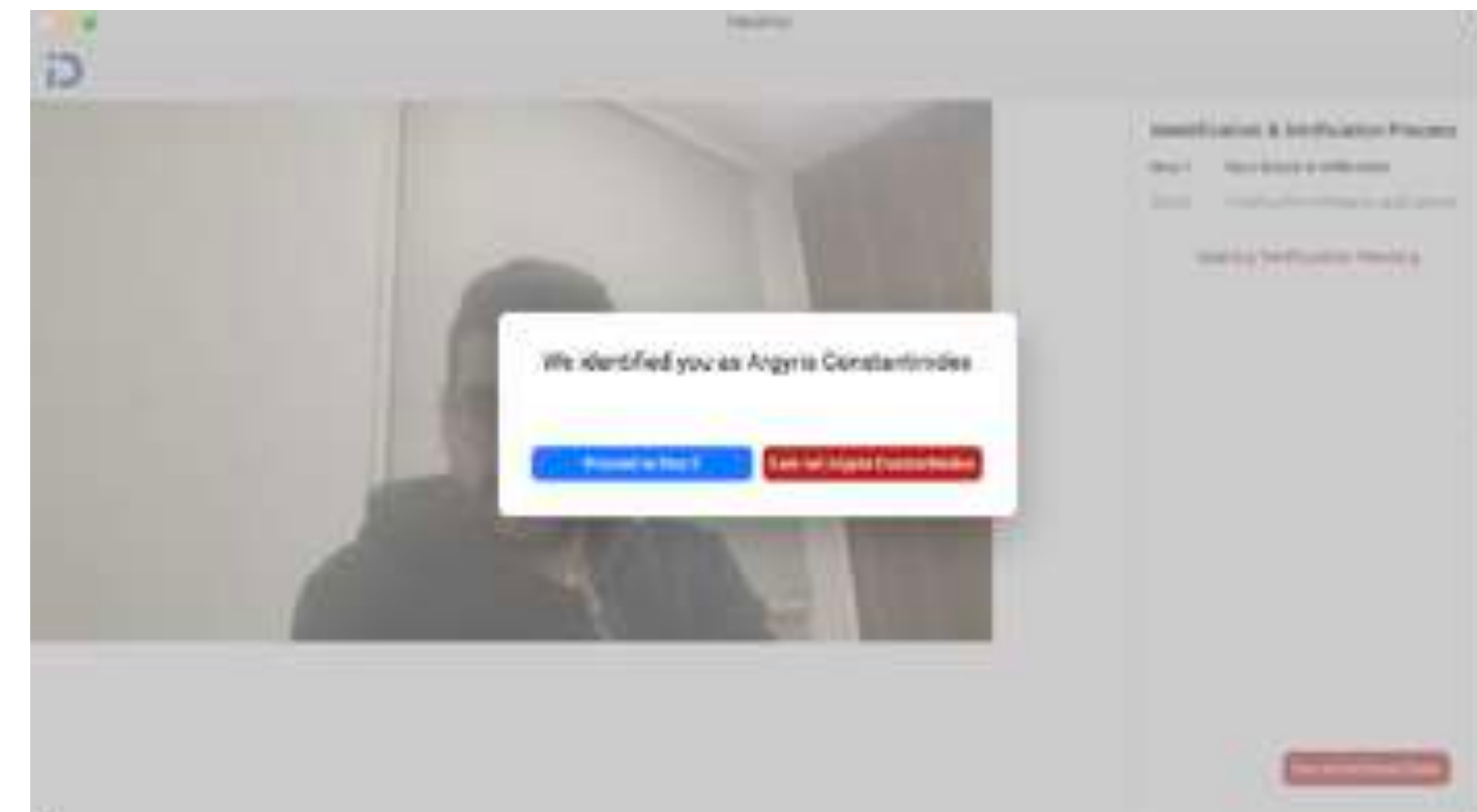
- Face detection: (HoG + linear SVM)
- CNN classification: ResNET18

# TrustID Project

- Intelligent and Continuous Online Student Identity Management for Improving Security and Trust in European Higher Education Institutions.
- <https://trustid-project.eu/>
- Project approved by the European Commission under the Erasmus+ 2020 program, with a total funding of €291K and two years duration (June/2021 - May/2023).
- Partners:
  - University of Patras (Greece) [coordination]
  - University of Cyprus (Cyprus)
  - **Institute of Systems and Robotics, University of Coimbra (Portugal)**
  - Cognitive UX GmbH (Germany).



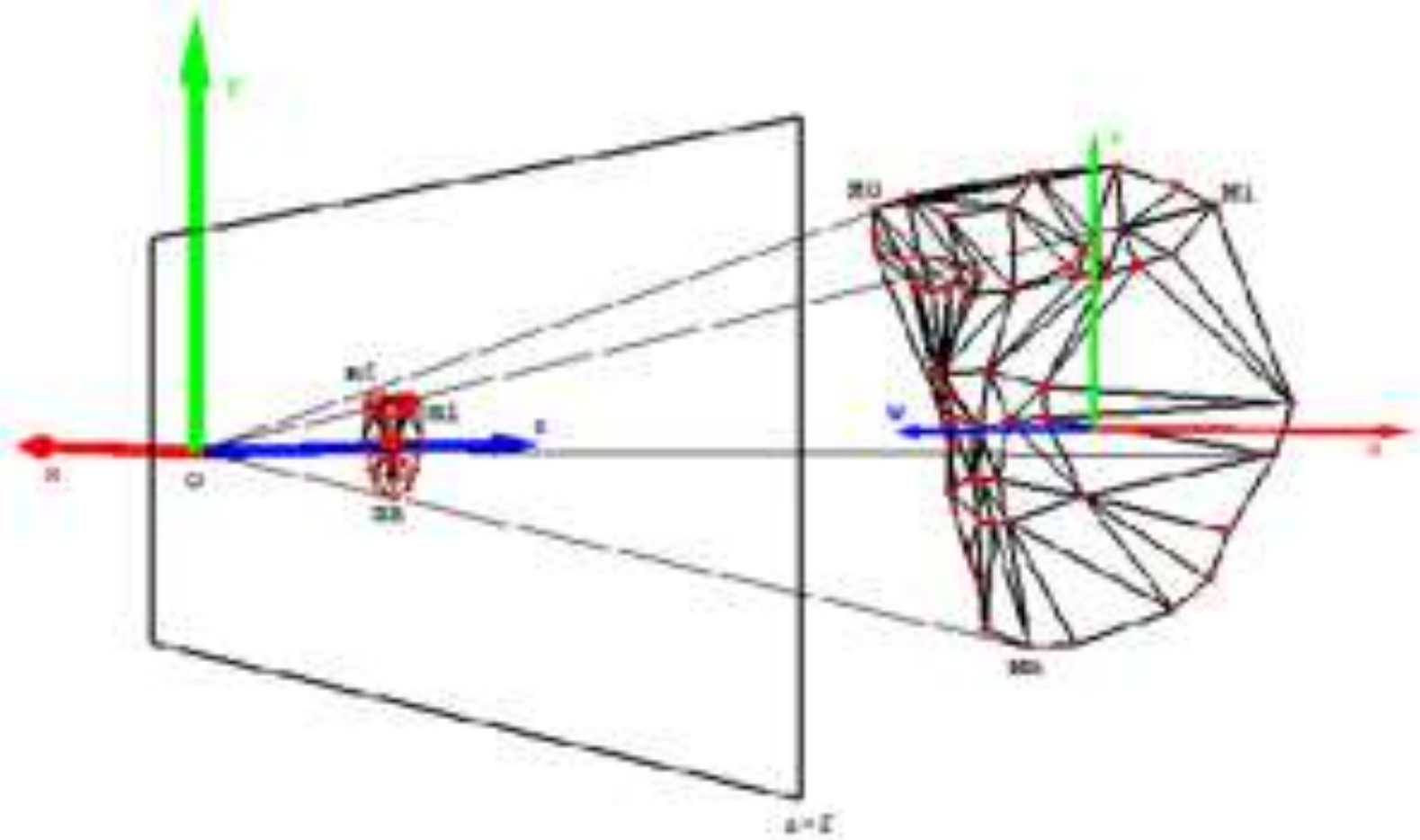
Enrol users web page.



User interface.



# 3D Head Pose Estimation



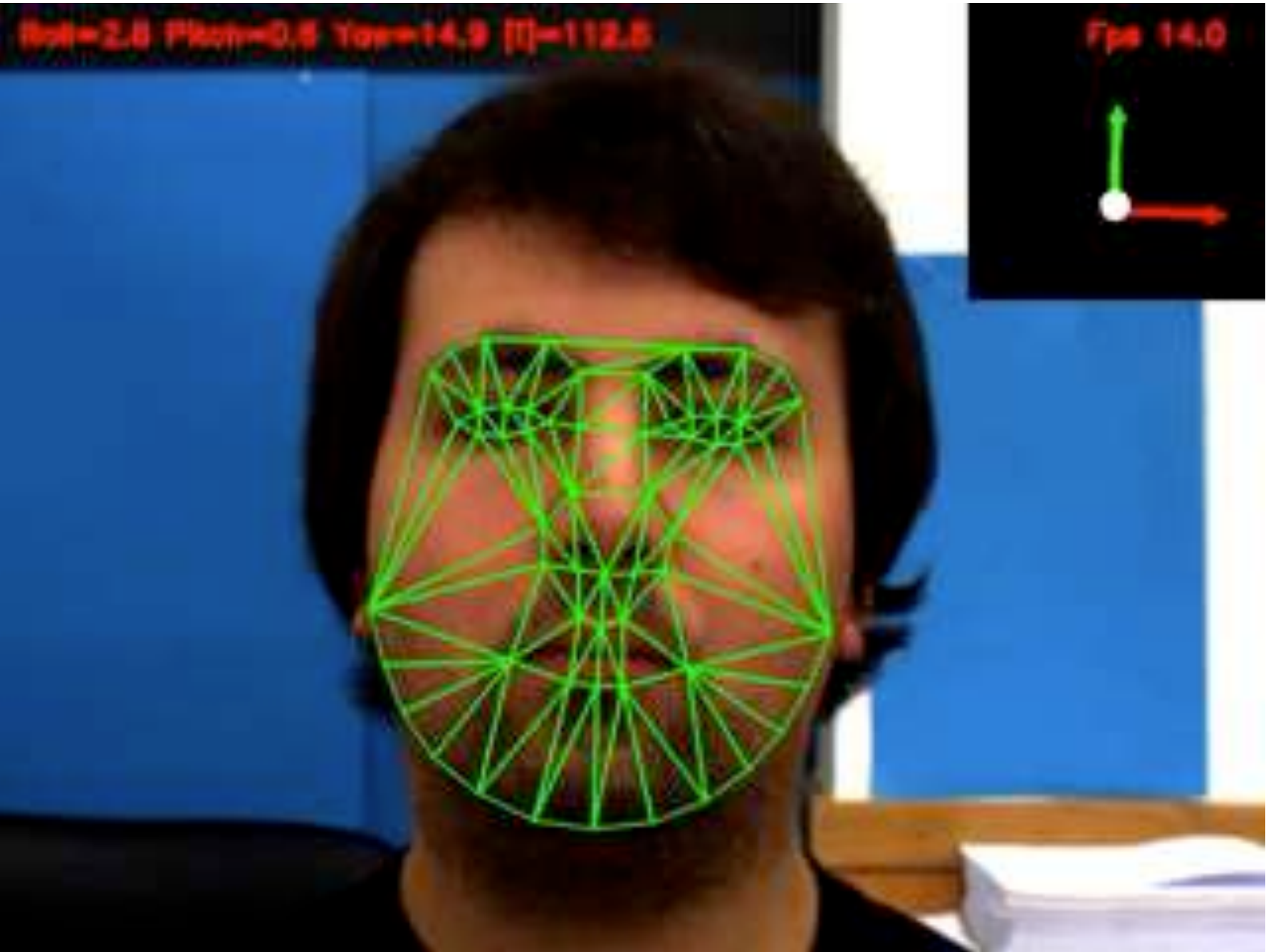
(old) 3D Model



Improved 3D Model



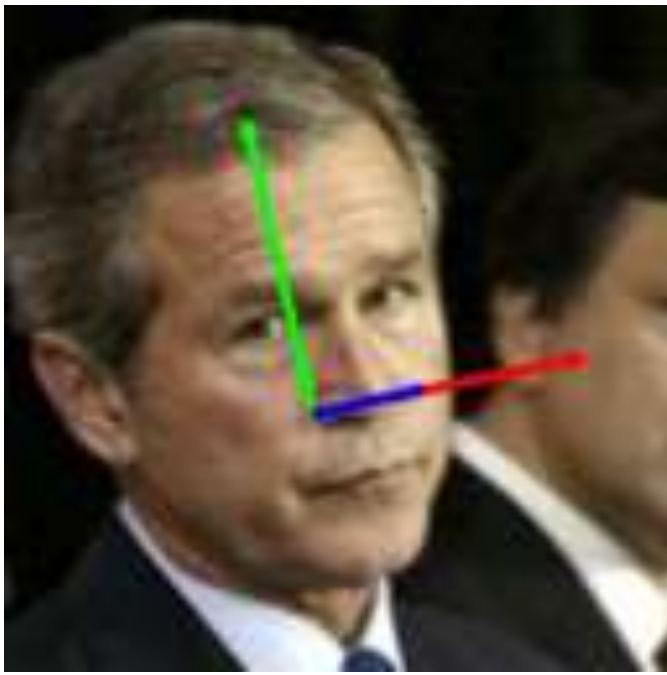
Roll=2.8 Pitch=0.8 Yaw=14.9 [I]=112.5



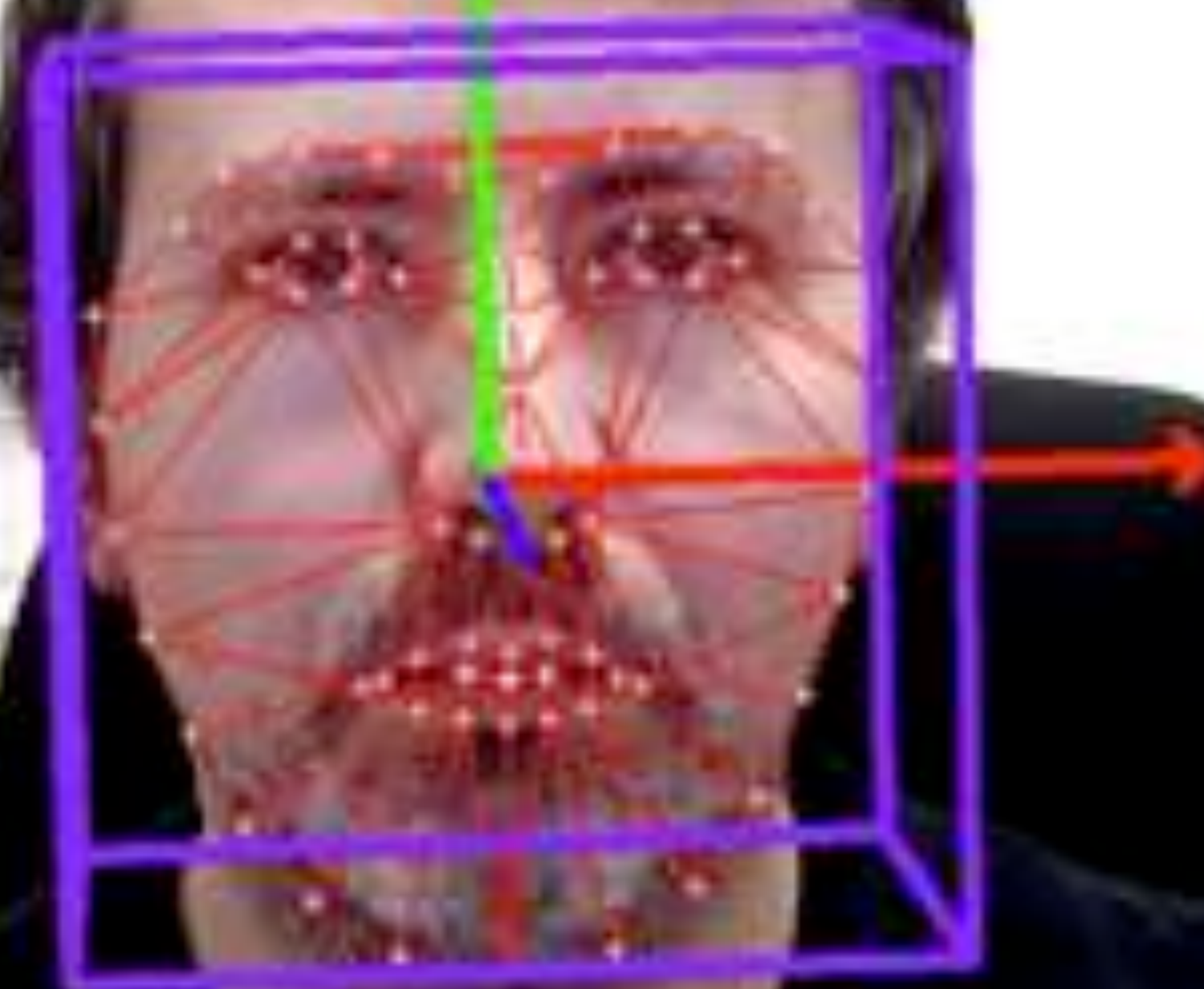
2D landmarks



3D model projection

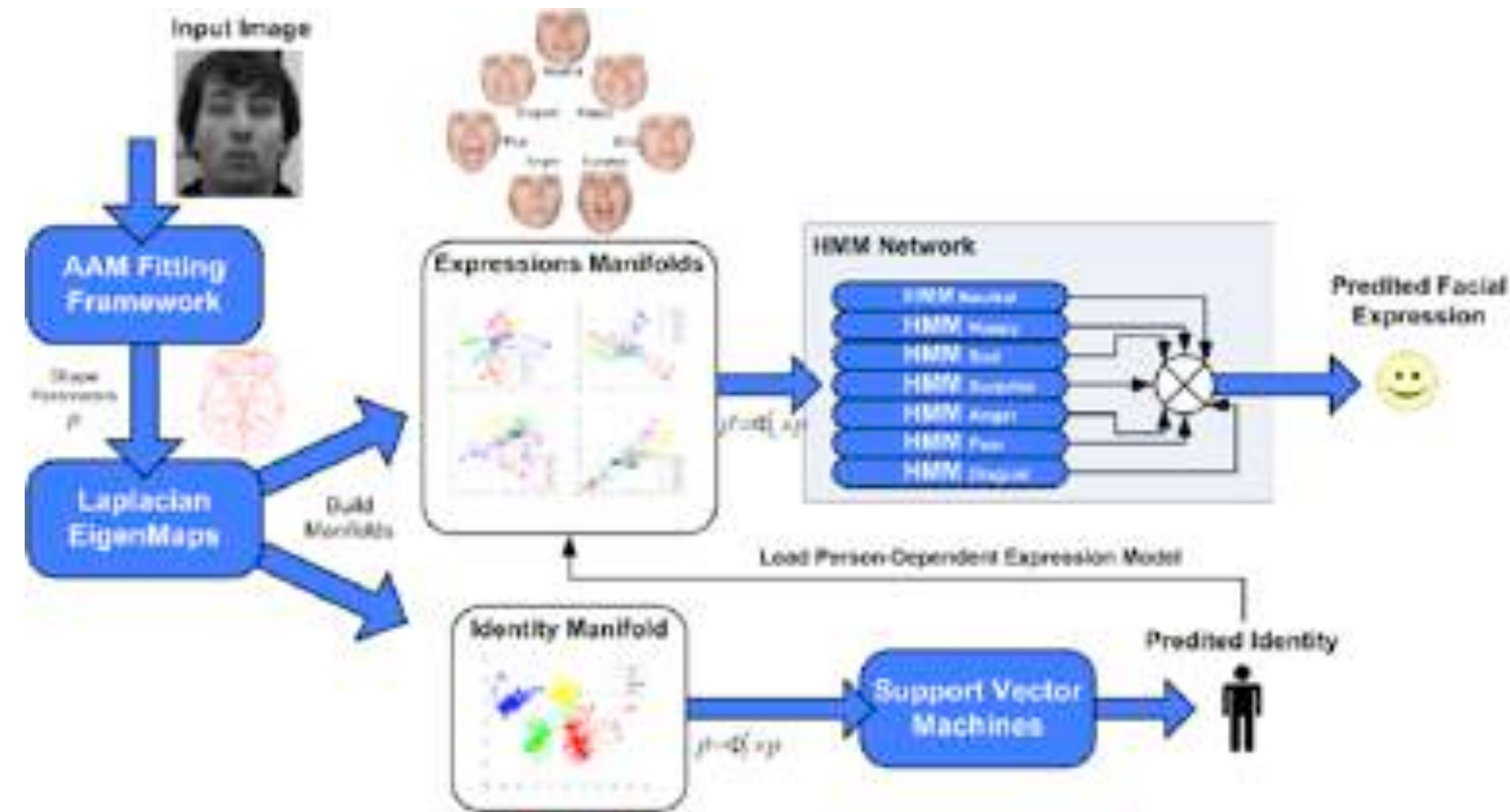


Pose representation



$R_x=8.3$   $R_y=-0.1$   $R_z=-1.7$   $d=50.9$

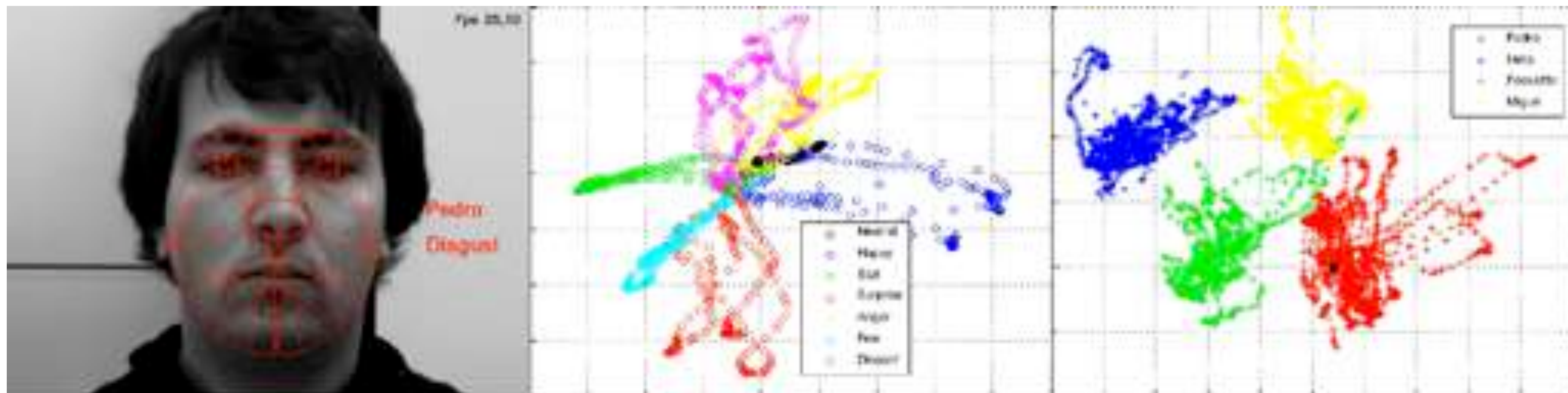
# Facial Expression Recognition



Input (SIC Fitting)

Expression (HMM)

Identity (SVM)



# Face Swapping w/ Blending

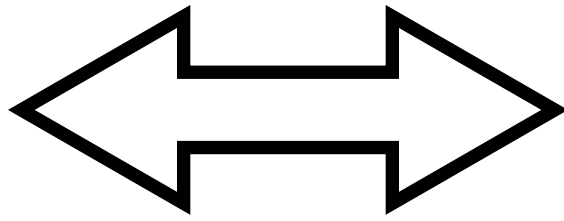


source image A



source image B

Swap Appearances



swap(A,B)



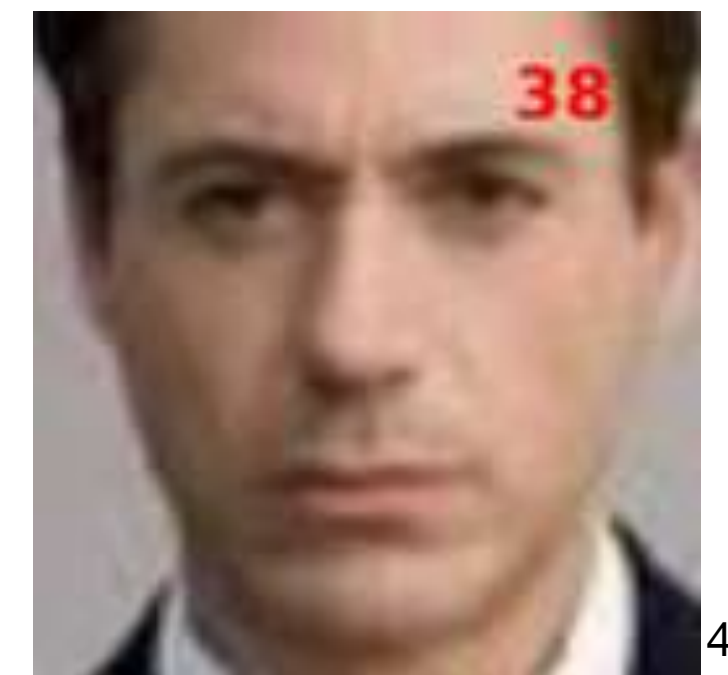
swap(B,A)



# Age Estimation



Age



- UTK Faces Database.
- 20K+ images of faces in the wild
- 200x200 RGB images
- CNN Regression (ResNet18)

# Demo 3D Head Pose Estimation - Super Mario World





# Thank you

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<https://www.isr.uc.pt/~pedromartins>  
[pedromartins@isr.uc.pt](mailto:pedromartins@isr.uc.pt)

